

# Computer Vision

Doctoral Program in Computer Science (MAPI)

***Hélder Filipe Pinto de Oliveira***

***Faculdade de Ciências da Universidade do Porto***  
***Departamento de Ciência de Computadores***

# Teacher Background

## Academic Background

- BSc (Licenciatura) - Eng. Eletrotécnica e de Computadores, FEUP (1999 – 2004)
- MSc - Automação, Instrumentação e Controlo, FEUP (2005 – 2008)
  - Robotics
- PhD - Eng. Eletrotécnica e de Computadores, FEUP (2008 – 2013)
  - Medical Image Analysis (Breast Cancer)

# Teacher Background

## Faculty Experience

- **Faculdade de Ciências da Universidade do Porto**
  - Departamento de Ciência de Computadores
  - Invited Assistant Professor (2016 – ...)
- **Faculdade de Engenharia da Universidade do Porto**
  - Departamento de Engenharia Informática
  - Invited Assistant Professor (2014 – 2016)
  - Invited Assistant (2008 – 2011)

# Teacher Background

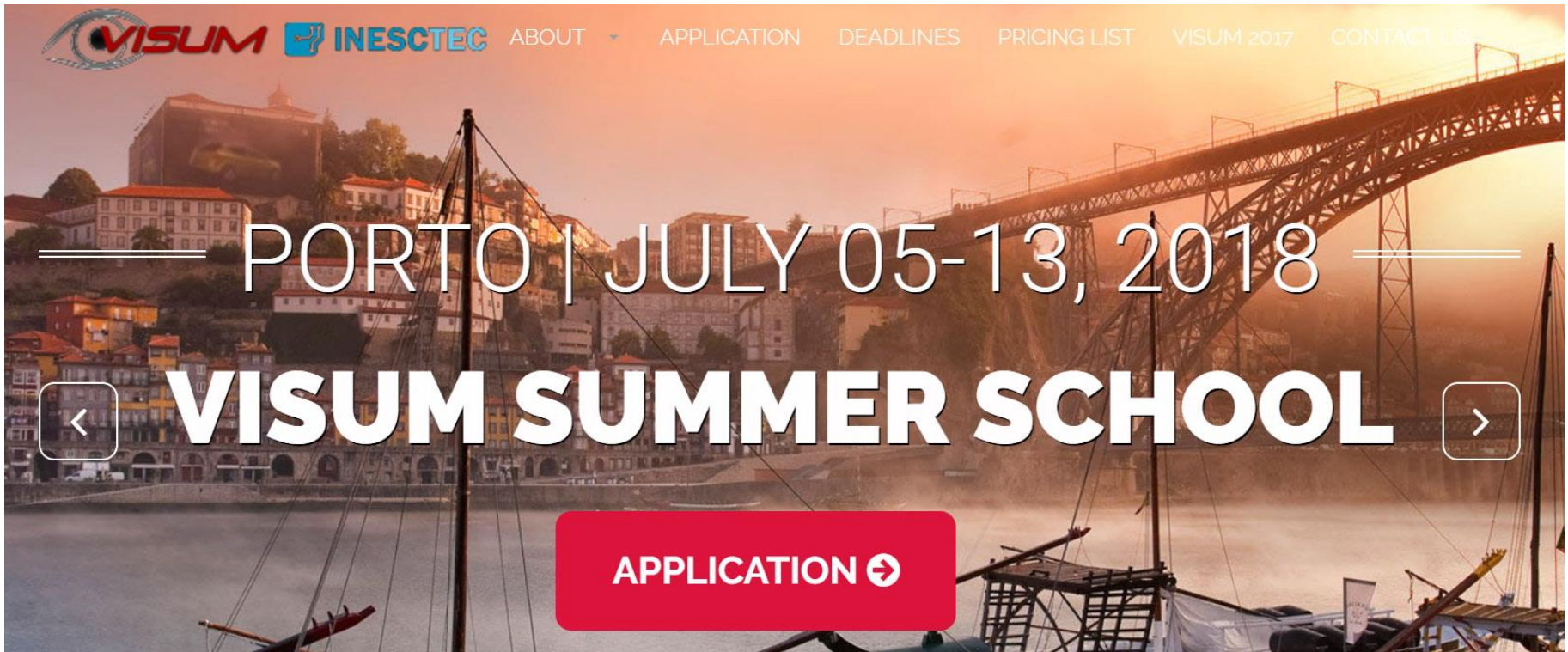
## Research Experience

- INESC TEC (2008 - ...)
- Politecnico di Milano (april – june 2011)
- FEUP (2004 – 2005) (2007 – 2008)
- ISR-Porto (2005 – 2007)
- **Projects**
  - BCCT.plan (PT 2020) – Breast Cancer (2016 – 2019)
  - NanoSTIMA (PT 2020) – Medical Image Analysis (2015 – 2018)
  - PICTURE (UE) – Breast Cancer (2013 – 2016)
  - 3dBCT (FCT) – Breast Cancer (2011 – 2014)
  - 5DPO (FCT) – Robotics (2005 – 2007)
  - IVLAB (ADI) – Cork stoppers image analysis (2004 – 2005)

# Teacher Background

## VISUM Summer School

- <http://visum.inesctec.pt/>



**VISUM** **INESCTEC** ABOUT APPLICATION DEADLINES PRICING LIST VISUM 2017 CONTACT US

PORTO | JULY 05-13, 2018

**VISUM SUMMER SCHOOL**

APPLICATION →

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# Teacher Background

## Personal webpage

- <http://www.inescporto.pt/~hfpo/>

### Hélder P. Oliveira's home page

Researcher at INESC TEC and Invited Assistant Professor at FCUP

Main Menu
Home
Education
Publications
Research
Students
Projects
Teaching



#### Hélder Filipe Pinto de Oliveira

Invited Assistant Professor at Departamento de Ciência de Computadores ([DCC](#)) at Faculdade de Ciências da Universidade do Porto ([FCUP](#))  
Senior Researcher at Instituto de Engenharia de Sistemas e Computadores, Tecnologia e Ciência ([INESC TEC](#))

#### Short Curriculum Vitae

PhD in Electrical and Computers Engineering, [FEUP](#), 2013  
MSc in Automation, Instrumentation and Control, [FEUP](#), 2008  
BSc (Licenciatura) in Electrical and Computers Engineering, [FEUP](#), 2004

#### Research Groups

Active member of the Visual Computing and Machine Intelligence Group ([VCMi](#))  
Active member of the Breast Research Group ([GIMPA](#))

If you are interested in pursuing a MSc or PhD in Computer Vision, Image Processing and Analysis, Medical Imaging or Bio-related Imaging, you are invited to email me.

#### **NEWS:**

I'm involved in the organization of VISION Understanding and Machine intelligence school - ([visum2017](#)). Applications are now opened! Participate!

#### Contacts:

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Campus ds FEUP, Rua Dr. Roberto Frias, room 3.19  
4200-465 Porto, Portugal  
Tel: +351 222094306

helder.f.oliveira@inesctec.pt

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# Motivation

Every image tells a story...



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# Motivation

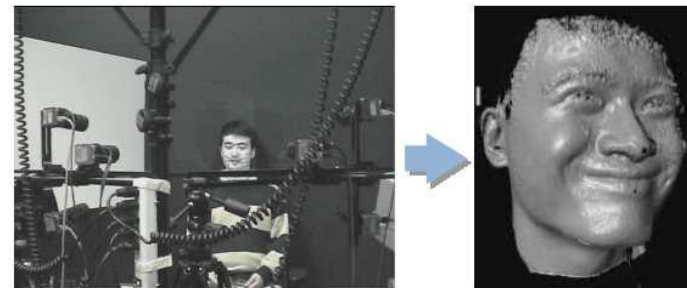
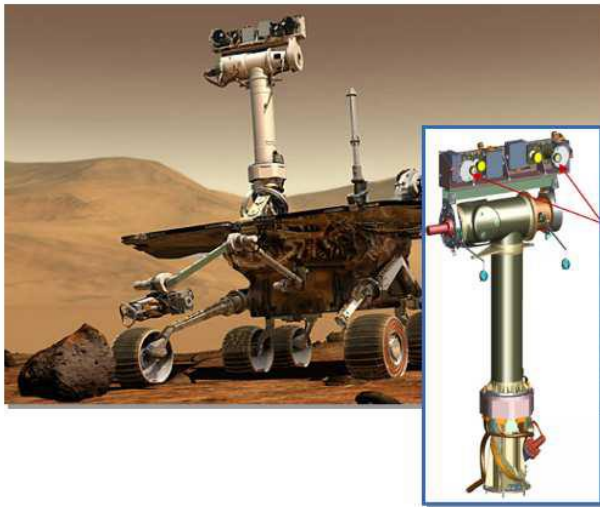
- Goal of computer vision: perceive the “story” behind the picture.
- Compute properties of the world: 3D shape, names of people or objects, what happened?

## **Can the computer match human perception?**

- Yes and no (mainly no): computers can be better at easy things; humans are much better at hard things.
- But huge progress has been made in the last years: what is considered hard keeps changing.



# Compute 3D shape of the world

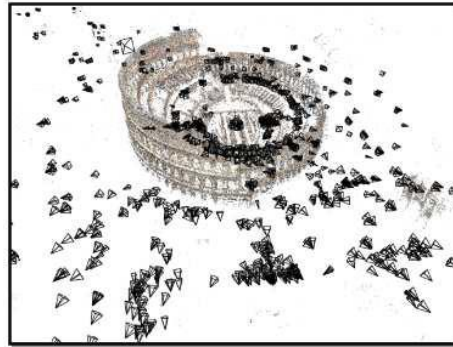


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# Compute 3D shape of the world



Internet Photos ("Colosseum")



Reconstructed 3D  
cameras and points



Dense 3D model

# Optical character recognition (OCR)



Digit recognition, AT&T labs



License plate readers



Automatic check processing

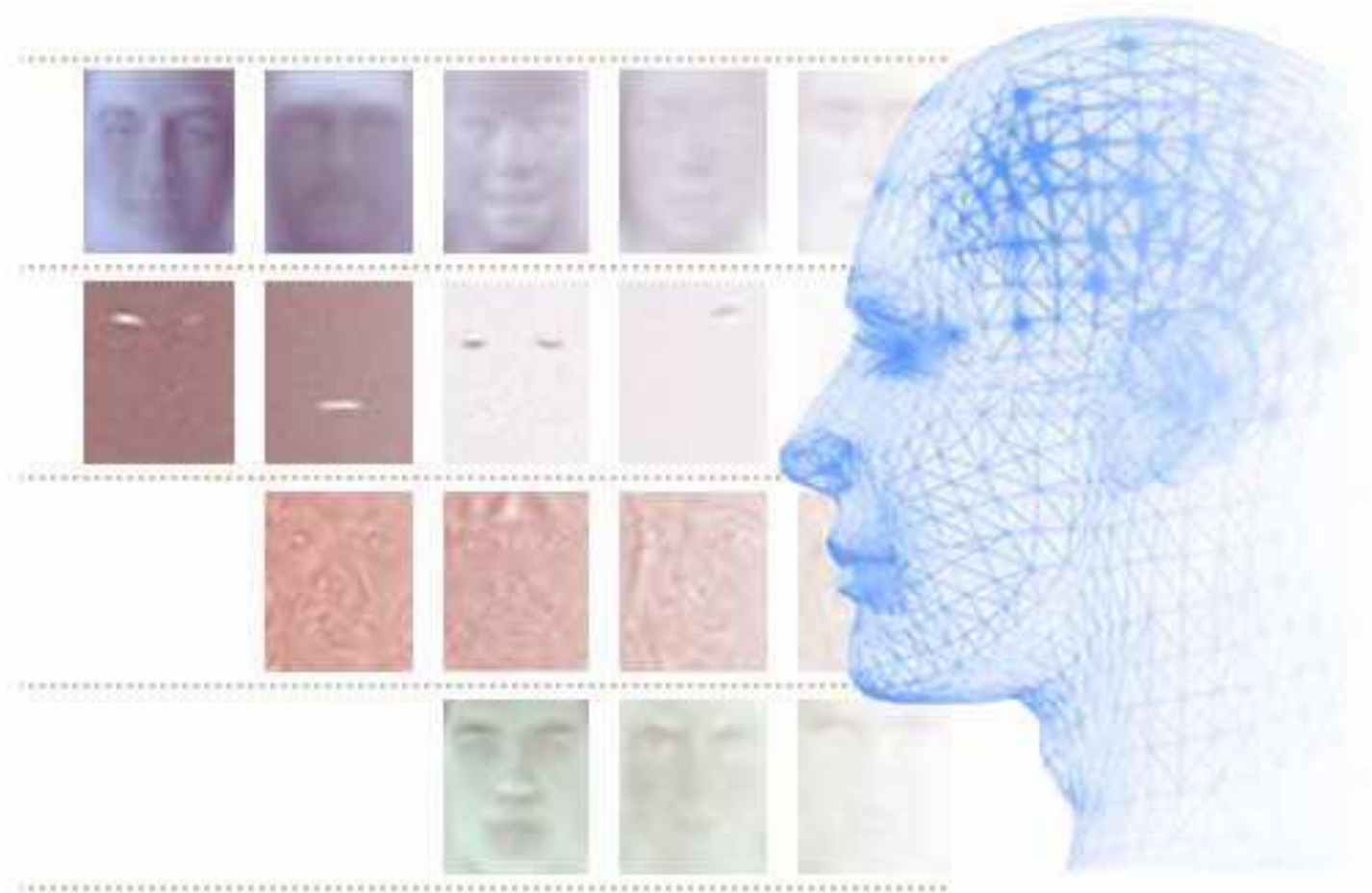


Sudoku grabber

# Forensics



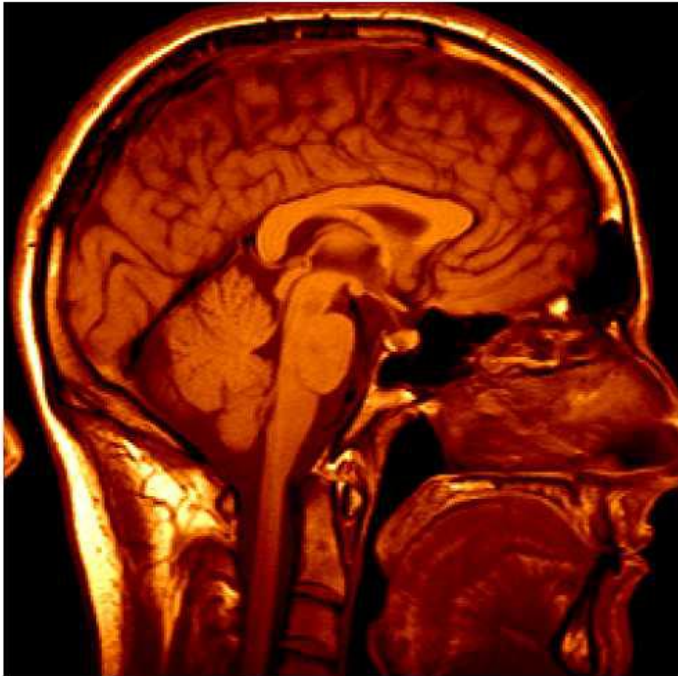
# Face detection / recognition



<http://www.face-rec.org/>

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# Medical image analysis



3D imaging  
MRI, CT



Image guided surgery  
Grimson et al., MIT

# Space



The Heights of Mount Sharp

[http://www.nasa.gov/mission\\_pages/msl/multimedia/pia16077.html](http://www.nasa.gov/mission_pages/msl/multimedia/pia16077.html)

Panorama captured by Curiosity Rover, August 18, 2012 (Sol 12)

## Vision systems (JPL) uses for several tasks

- Panorama stitching
- 3D terrain modeling
- Obstacle detection, position tracking

# Smart Cars

▶ manufacturer products    consumer products ◀

## Our Vision. Your Safety.

rear looking camera    forward looking camera

side looking camera

▶ **EyeQ** Vision on a Chip [read more](#)

▶ **Vision Applications** Road, Vehicle, Pedestrian Protection and more [read more](#)

▶ **AWS** Advance Warning System [read more](#)

**News**

- ▶ Mobileye Advanced Technologies Power Volvo Cars World First Collision Warning With Auto Brake System
- ▶ Volvo: New Collision Warning with Auto Brake Helps Prevent Rear-end

[all news](#)

**Events**

- ▶ Mobileye at Equip Auto, Paris, France
- ▶ Mobileye at SEMA, Las Vegas, NV

[read more](#)

- Mobileye
  - Vision systems currently in high-end models



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# Vision based interaction



Ex: camera-based IR tracking.



Assistive technologies

# Sports



Day 5: Swimming - Men's 4X200M Final

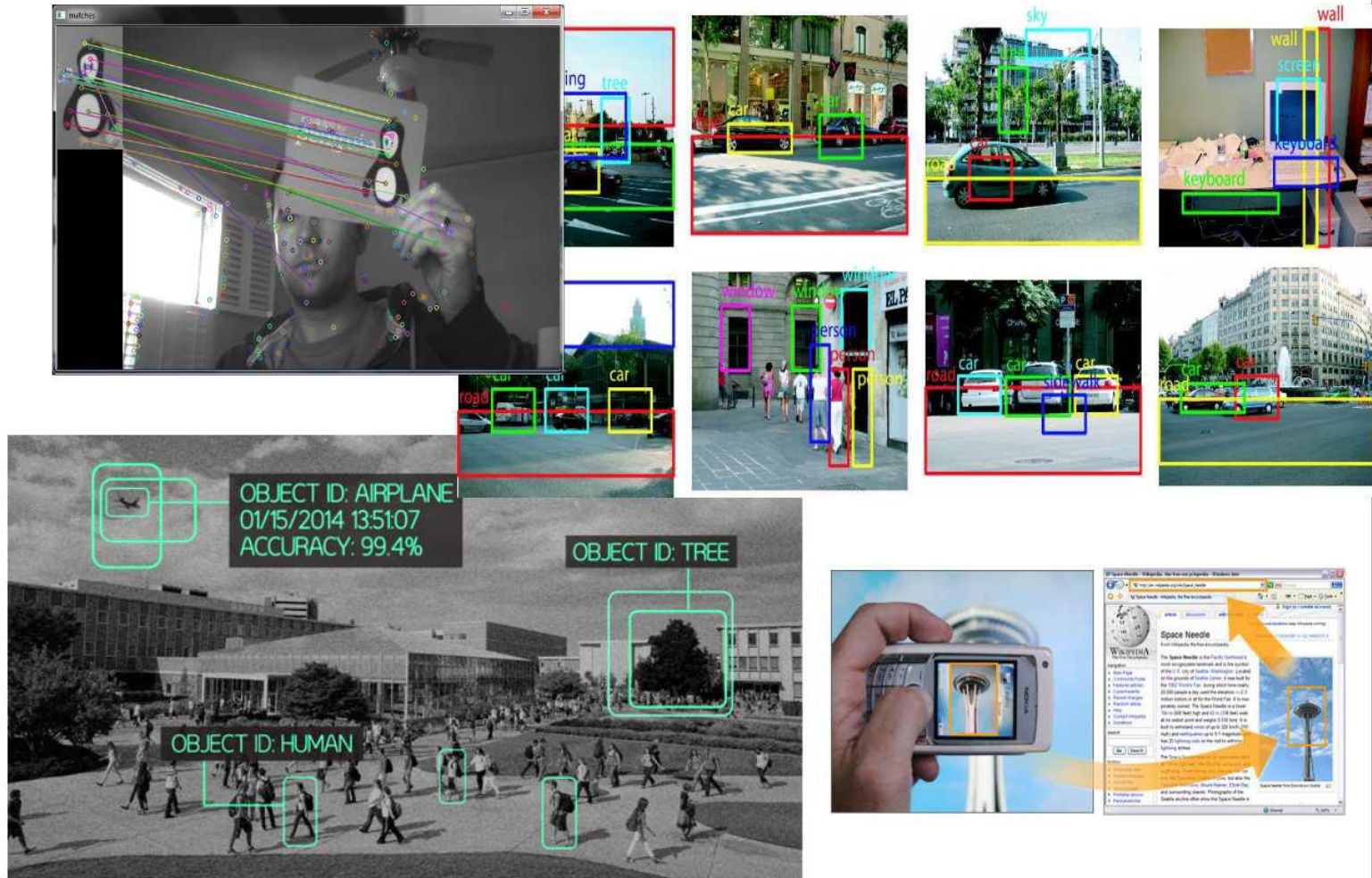


Highlights of the men's 4x200m relay final on Day 5.

# Shape and motion capture



# Object detection



# Vision as sensor in robotics



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# Human Vision

- Vision is a complex physical and intellectual human task that stands as a primary interaction tool with the world.
- It is a complex process not completely understood, even after hundreds of years of research.
- The visualization of a physical process involves an almost simultaneous interaction of the eyes and the brain.
- This interaction is performed by a network of neurons, receptors and other specialized cells.

# Human Vision

- The human eye is equipped with a variety of optical elements, including the cornea, iris, pupil, a variable lens and the retina.
- Can do amazing things like:
  - Recognize people and objects
  - Navigate through obstacles
  - Understand mood in the scene
  - Imagine stories
- But:
  - Suffers from illusions
  - Ignores many details
  - Ambiguous description of the world
  - Doesn't care about accuracy of world

# Computer Vision

- Vision is a complex physical and intellectual human task that stands as a primary interaction tool with the world.
- **Computer vision** is a field that includes methods for acquiring, processing, analyzing, and understanding images . . .
- Computer vision applications are increasing:
  - surveillance;
  - machine inspection;
  - medicine;
  - robotics;
  - entertainment;
  - media.
- The main goal: make computer vision converge towards human vision. **Can we ever accomplish that?**



# Why is computer vision difficult?



0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

- **Objective of Computer Vision:**
  - Understand the meaning of the image taken into account the value of the pixels

# Viewpoint variation



Michelangelo 1475-1564



slide credit: Fei-Fei, Fergus & Torralba

# Illumination

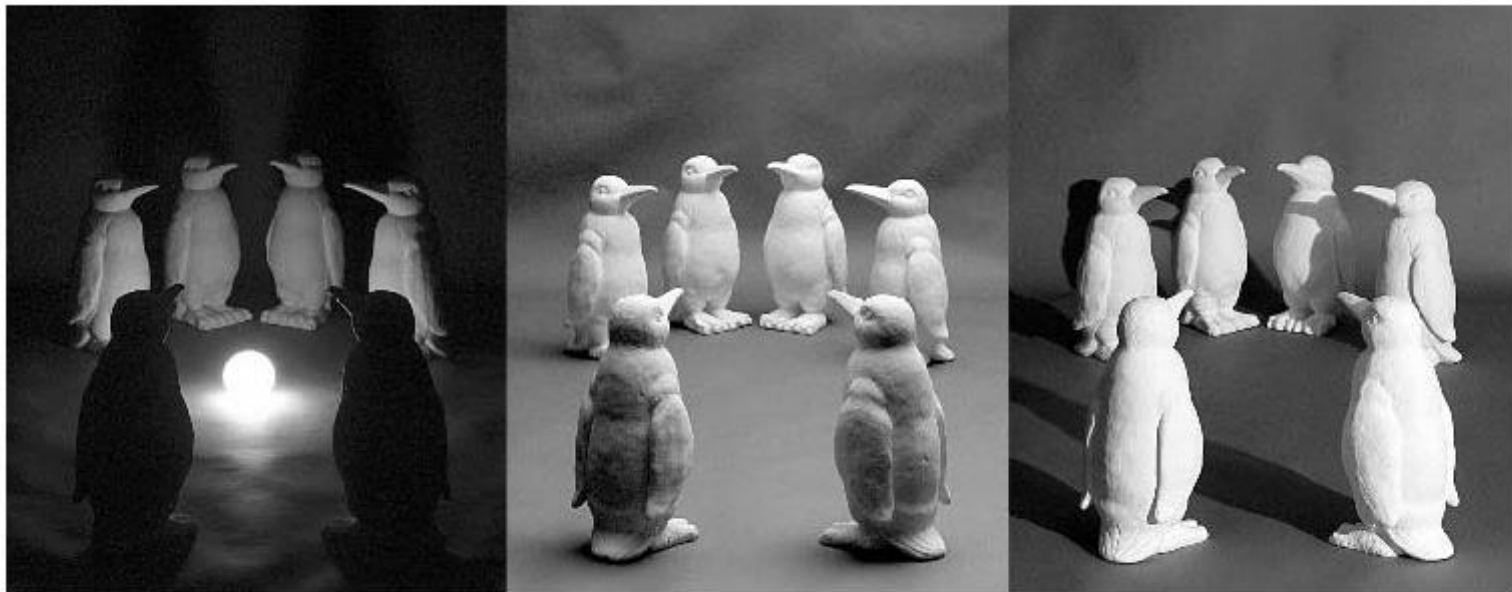


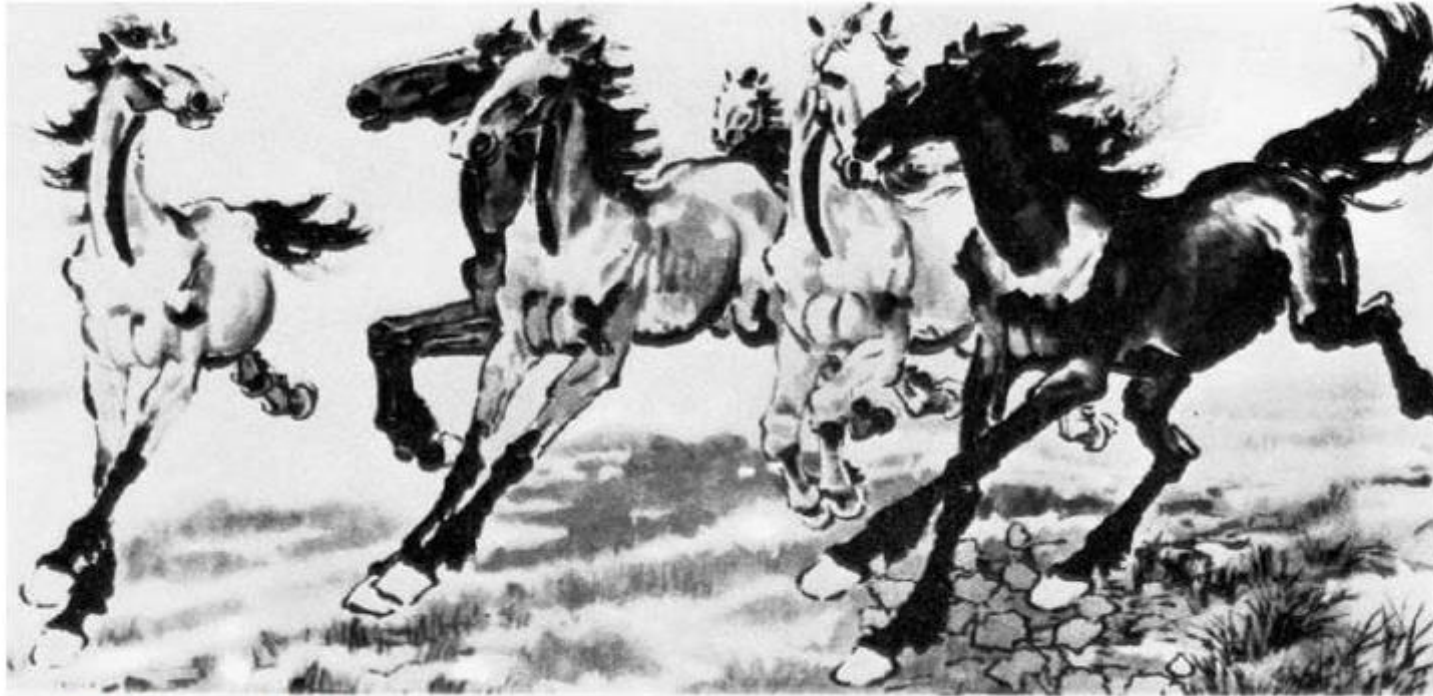
image credit: J. Koenderink

# Scale



slide credit: Fei-Fei, Fergus & Torralba

# Shape and deformations



Xu, Beihong 1943

slide credit: Fei-Fei, Fergus & Torralba

# Occlusions



Magritte, 1957

# Background clutter



slide credit: Svetlana Lazebnik

# Motion



slide credit: Svetlana Lazebnik



# Intra-class variation



# Need to understand the context

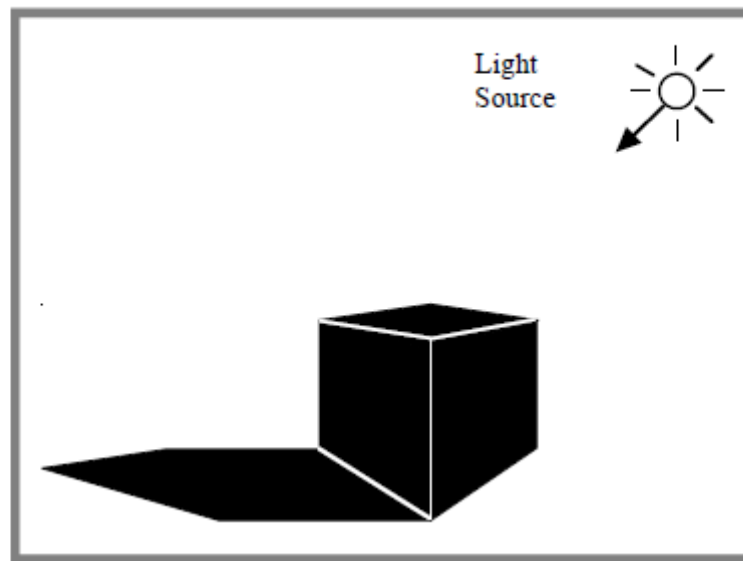
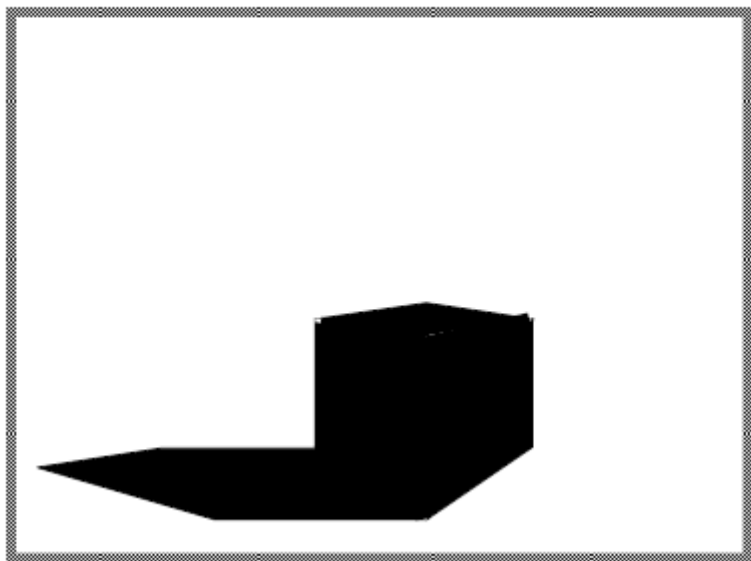
THE

THE

CHAT

CAT

# Need to understand the context



# Outline

- **Image Formation**
  - The Human Visual System
  - Image Capturing Systems
- **Digital Images**
  - Sampling
  - Data Structures
  - Histograms
- **Colour and Noise**
  - Colour spaces
  - Colour processing
  - Noise

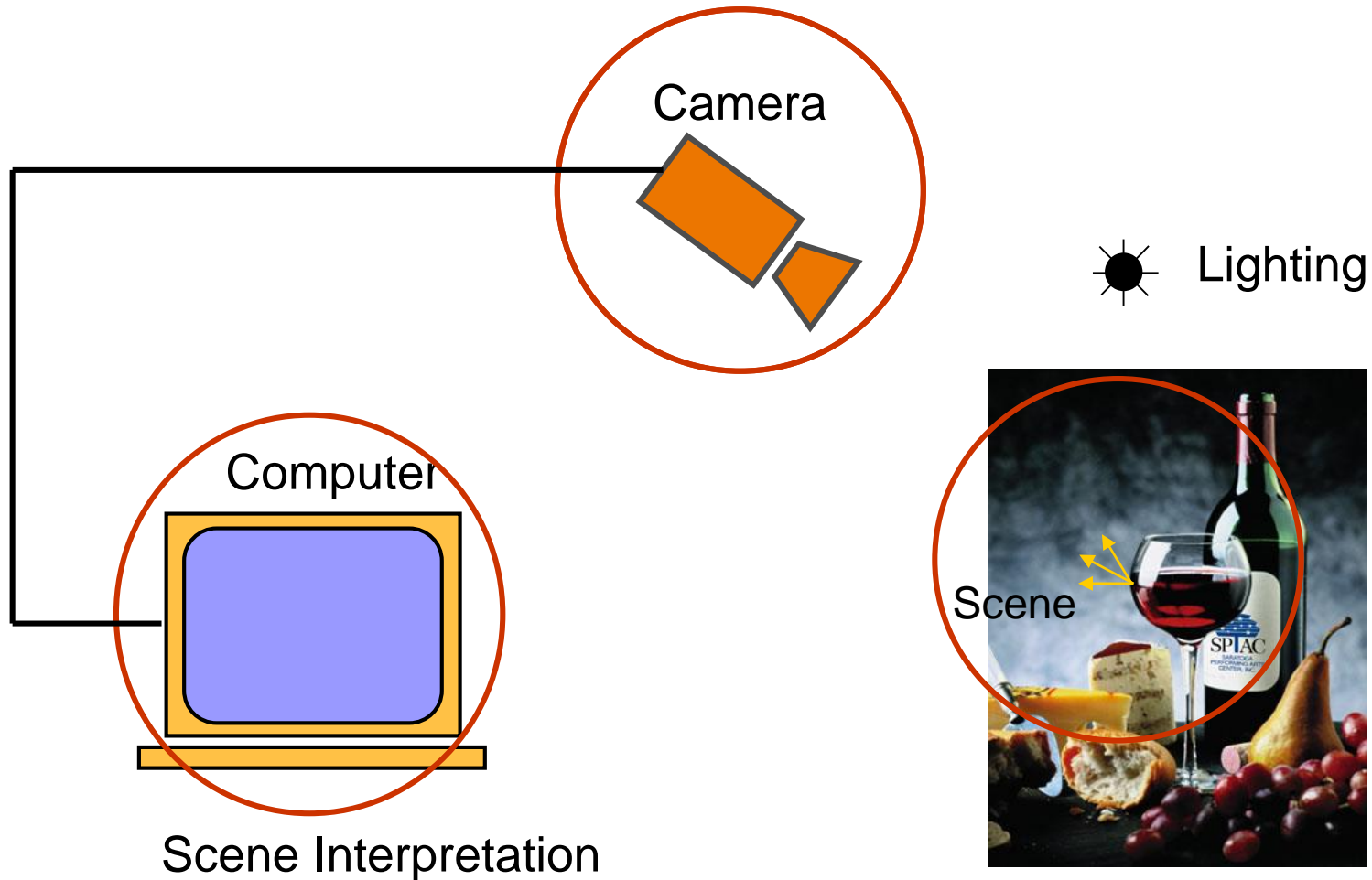
# Outline

- **Image Formation**
  - The Human Visual System
  - Image Capturing Systems
- Digital Images
- Colour and Noise

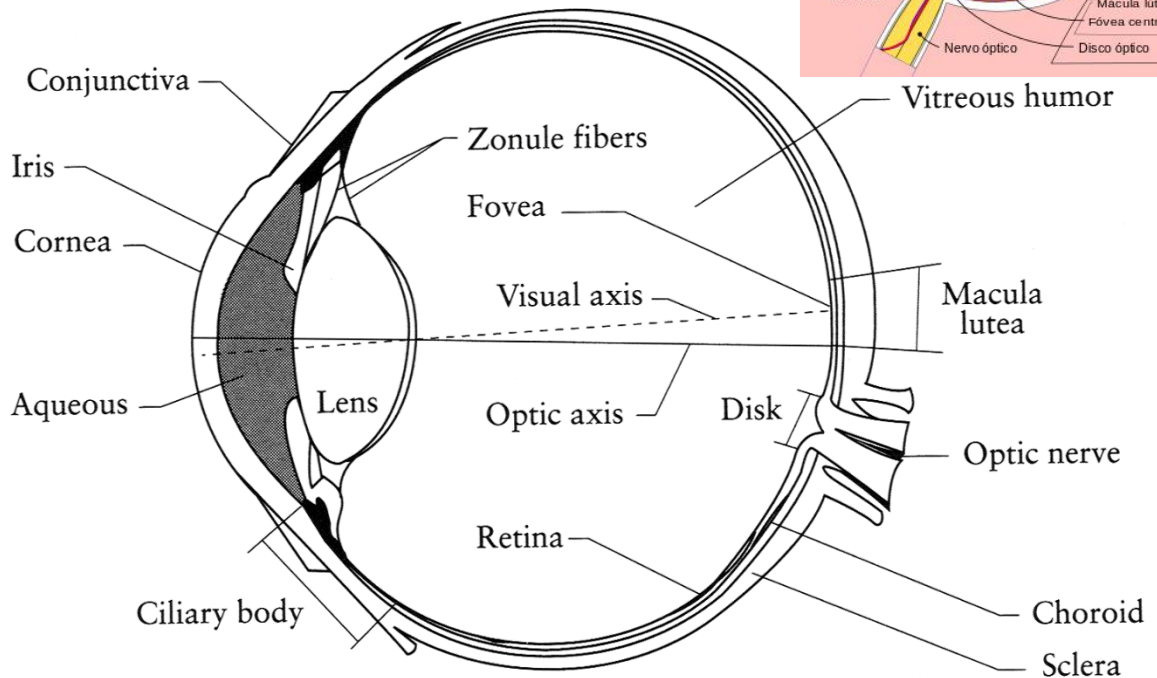
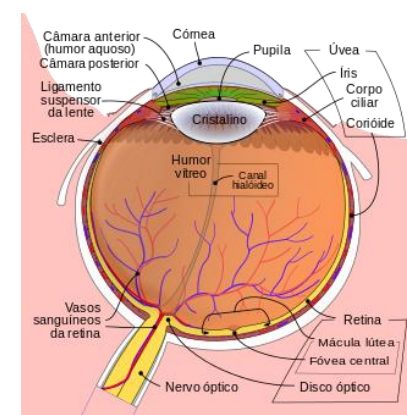
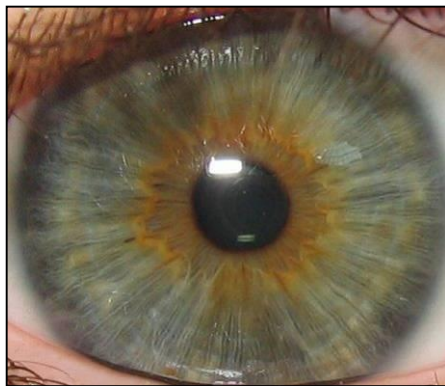
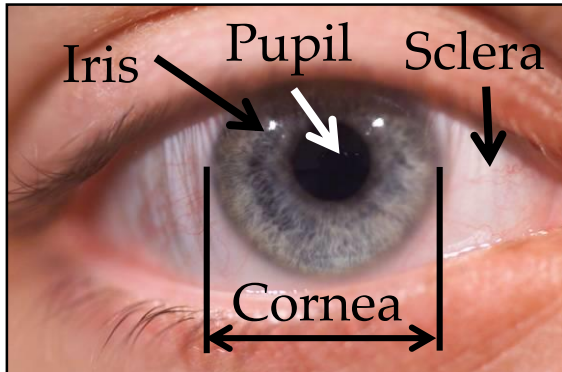
**Acknowledgements:** Most of this course is based on the excellent courses offered by Prof. Shree Nayar at Columbia University, USA and by Prof. Srinivasa Narasimhan at CMU, USA. Please acknowledge the original source when reusing these slides for academic purposes.

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# Components of a Computer Vision System



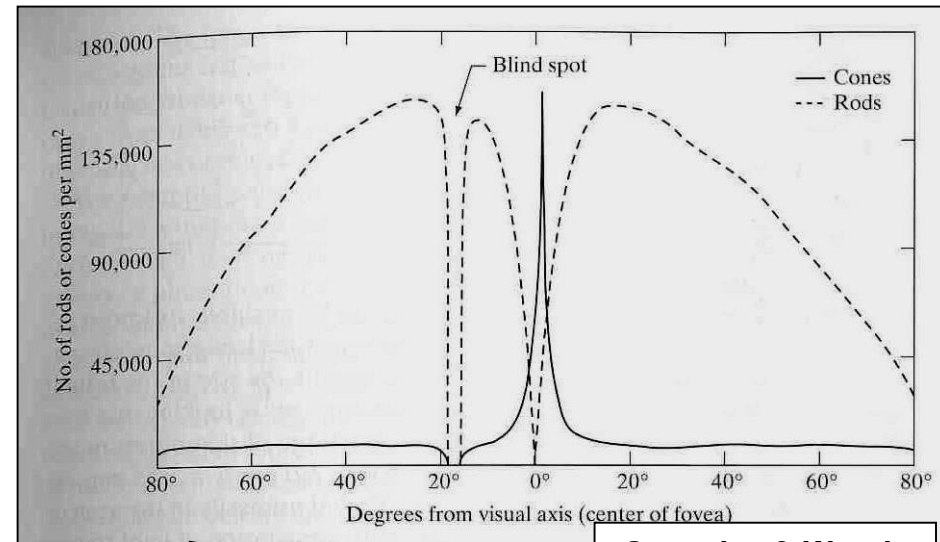
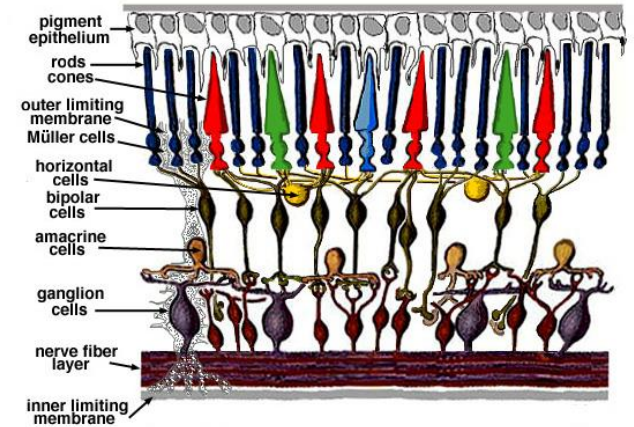
# Our Eyes



- Iris is the diaphragm that changes the aperture (pupil)
- Retina is the sensor where the fovea has the highest resolution

# Colour

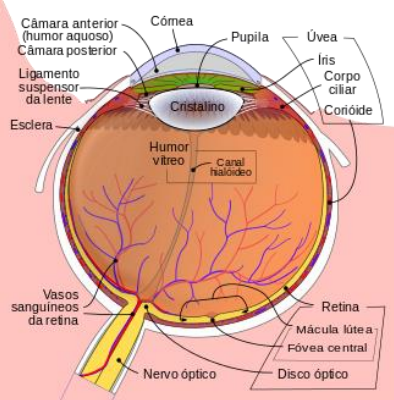
- **Our retina has:**
  - **Cones** – Measure the frequency of light (colour)
    - 6 to 7 millions
    - High-definition
    - Need high luminosity
  - **Rods** – Measure the intensity of light (luminance)
    - 75 to 150 millions
    - Low-definition
    - Function with low luminosity



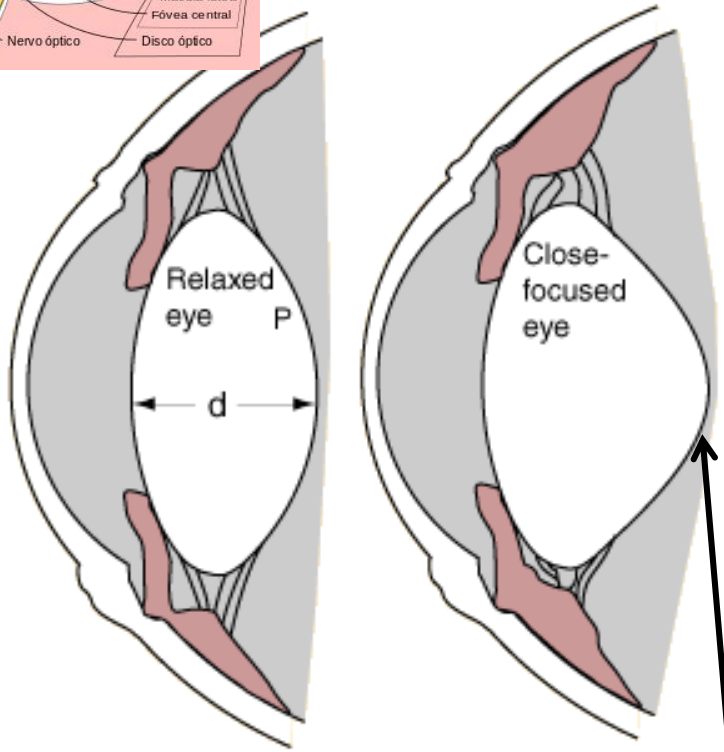
Gonzalez & Woods

We only see colour in the center of our retina!



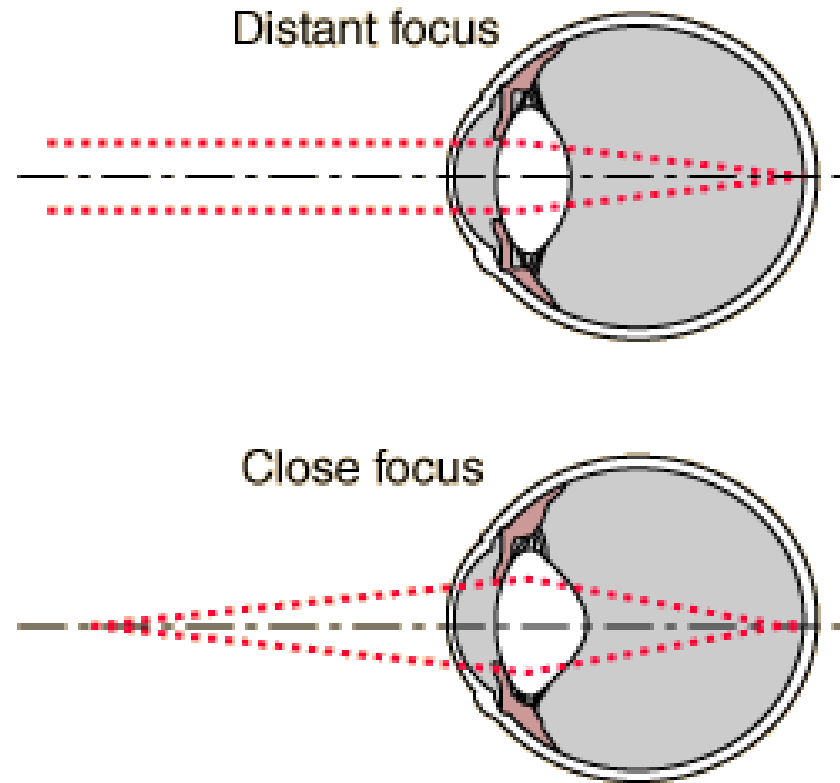


# Focusing

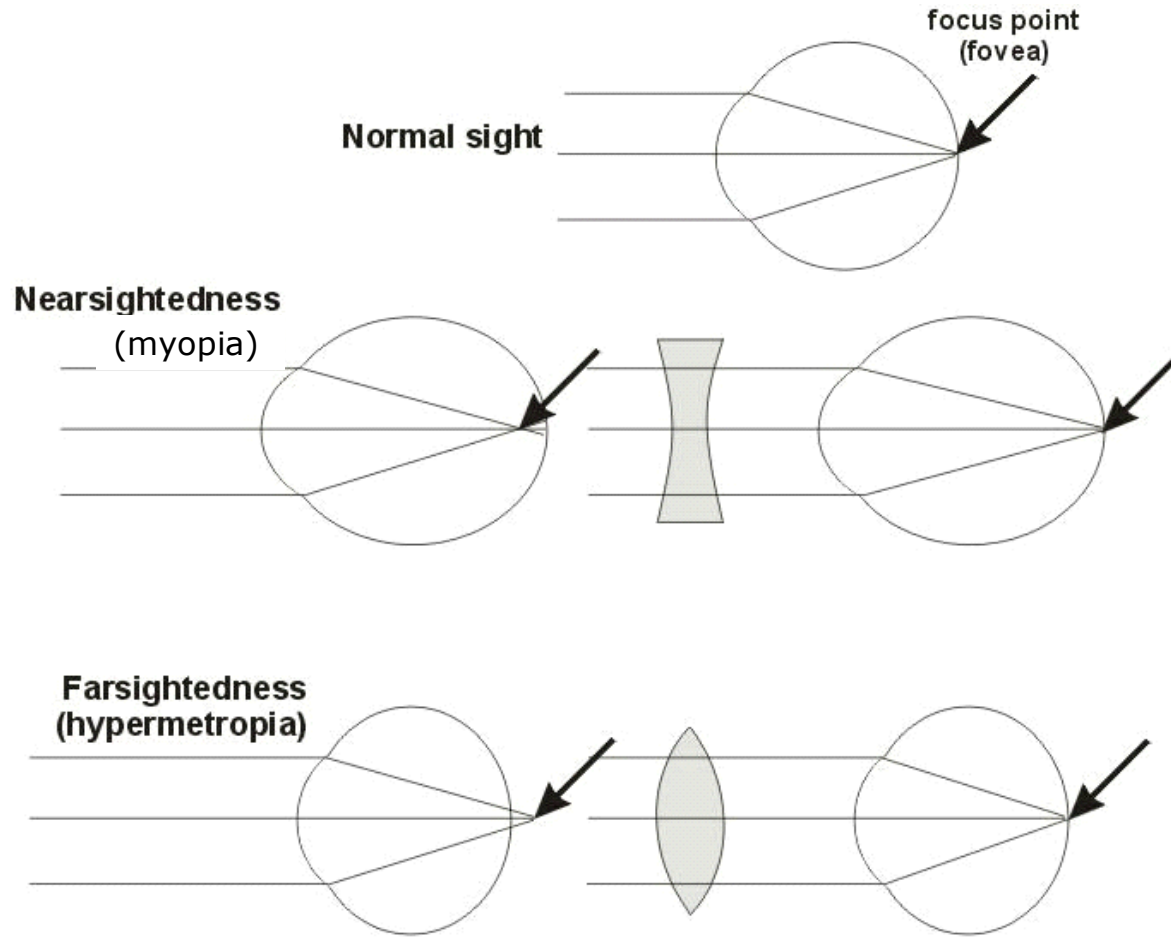


shorter focal length

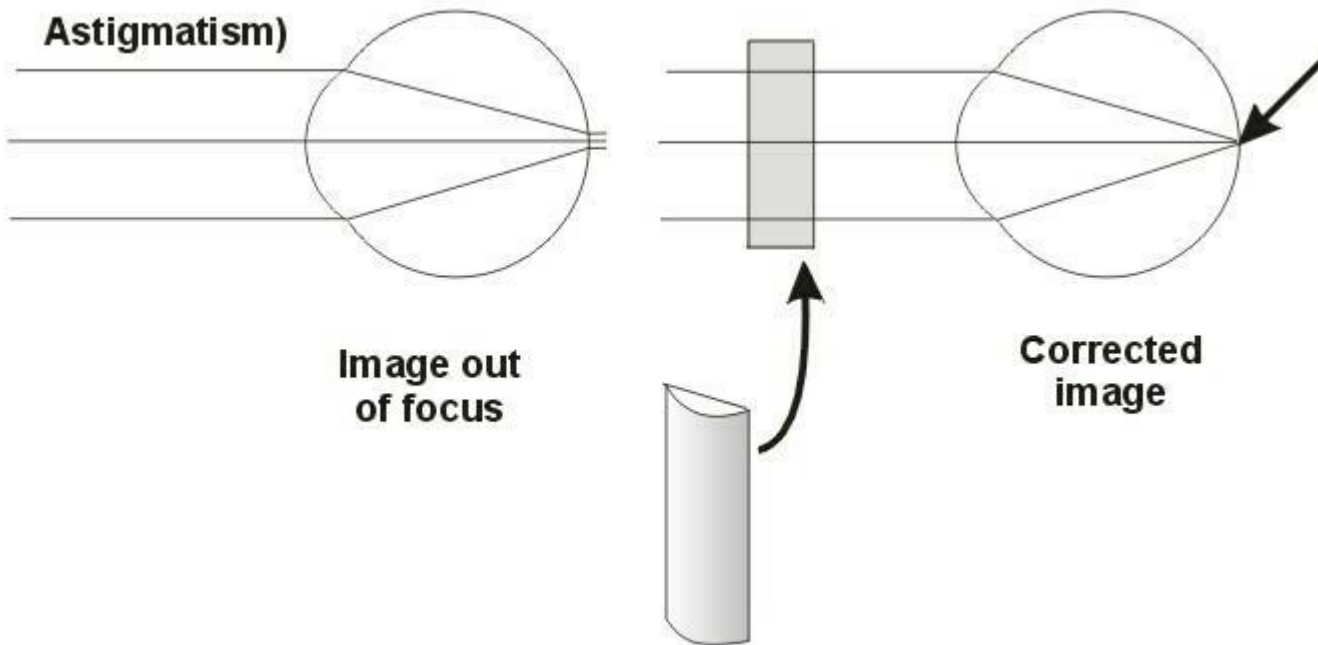
Changes the focal length of the lens



# Myopia and Hyperopia



# Astigmatism



The cornea is distorted causing images to be un-focused on the retina.

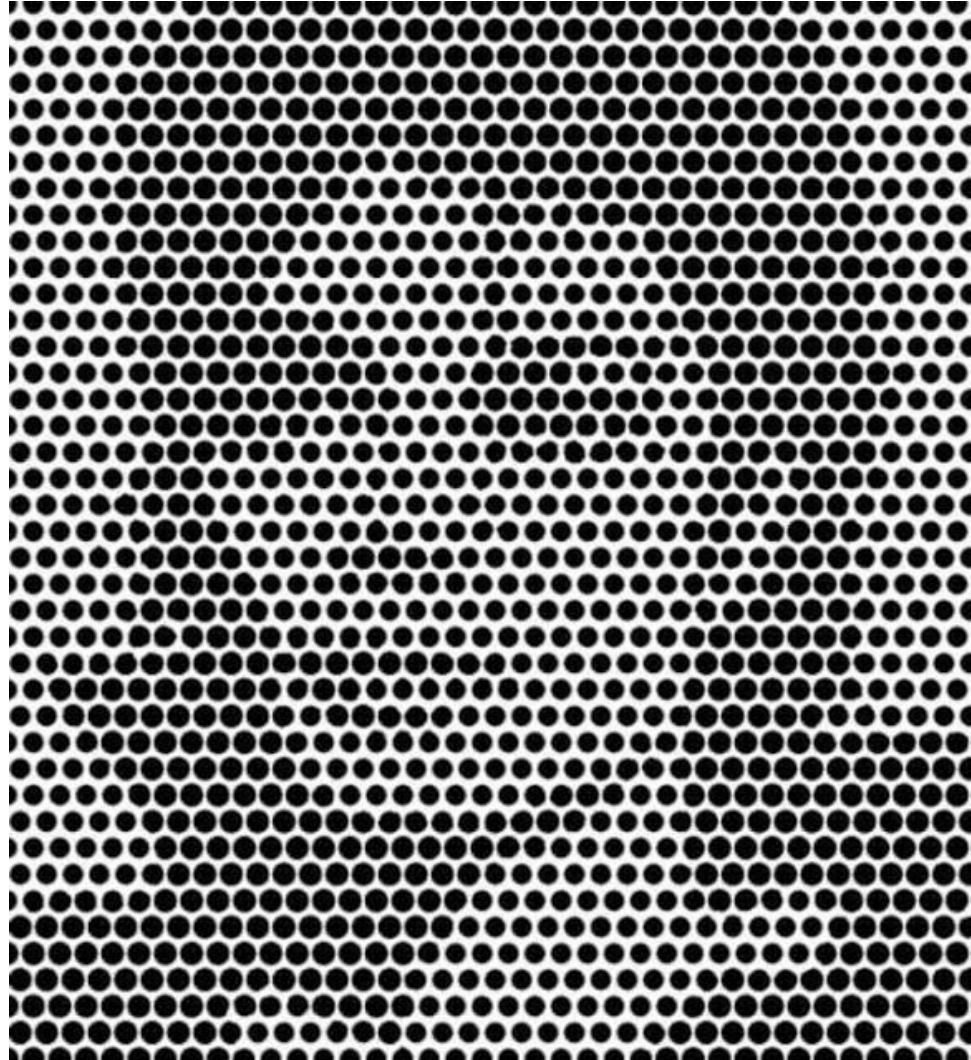
# Blind Spot in the Eye



Close your right eye and look directly at the “+”

[https://en.wikipedia.org/wiki/Blind\\_spot\\_\(vision\)](https://en.wikipedia.org/wiki/Blind_spot_(vision))

# More Illusions



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# More Illusions



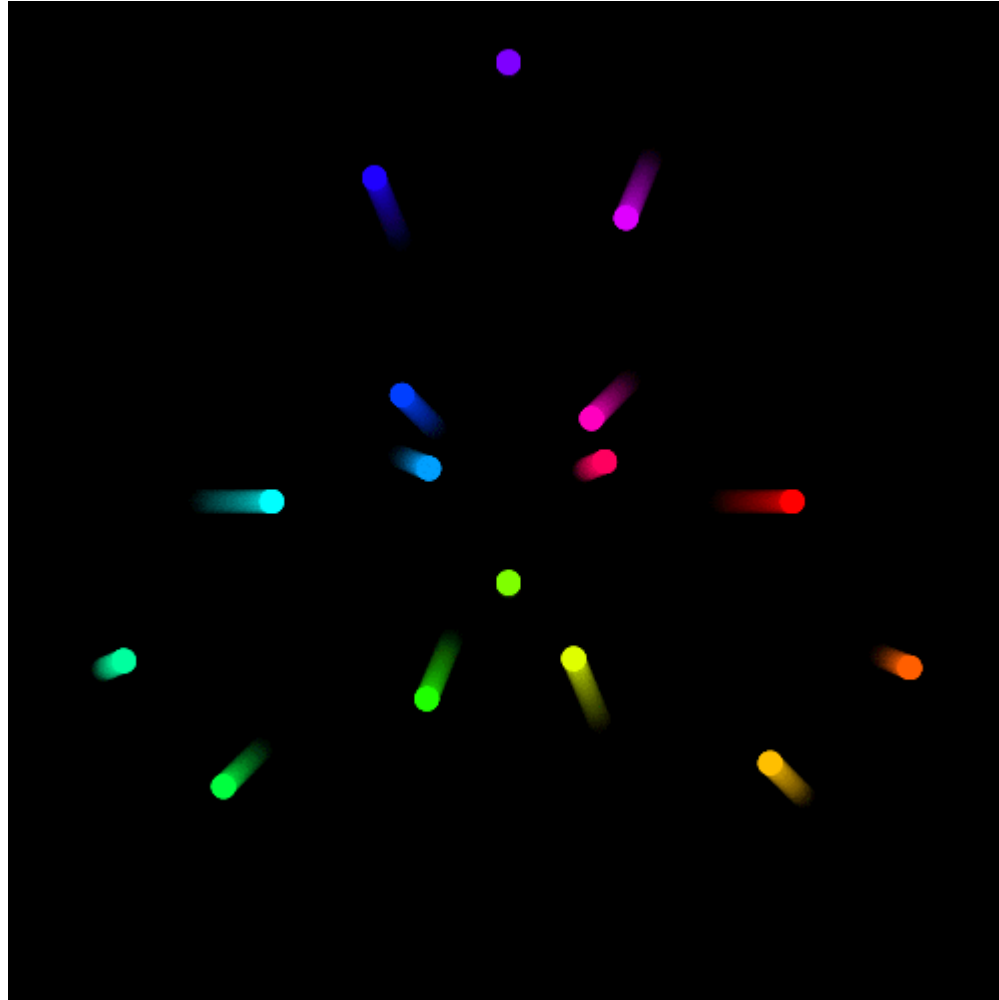
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# More Illusions



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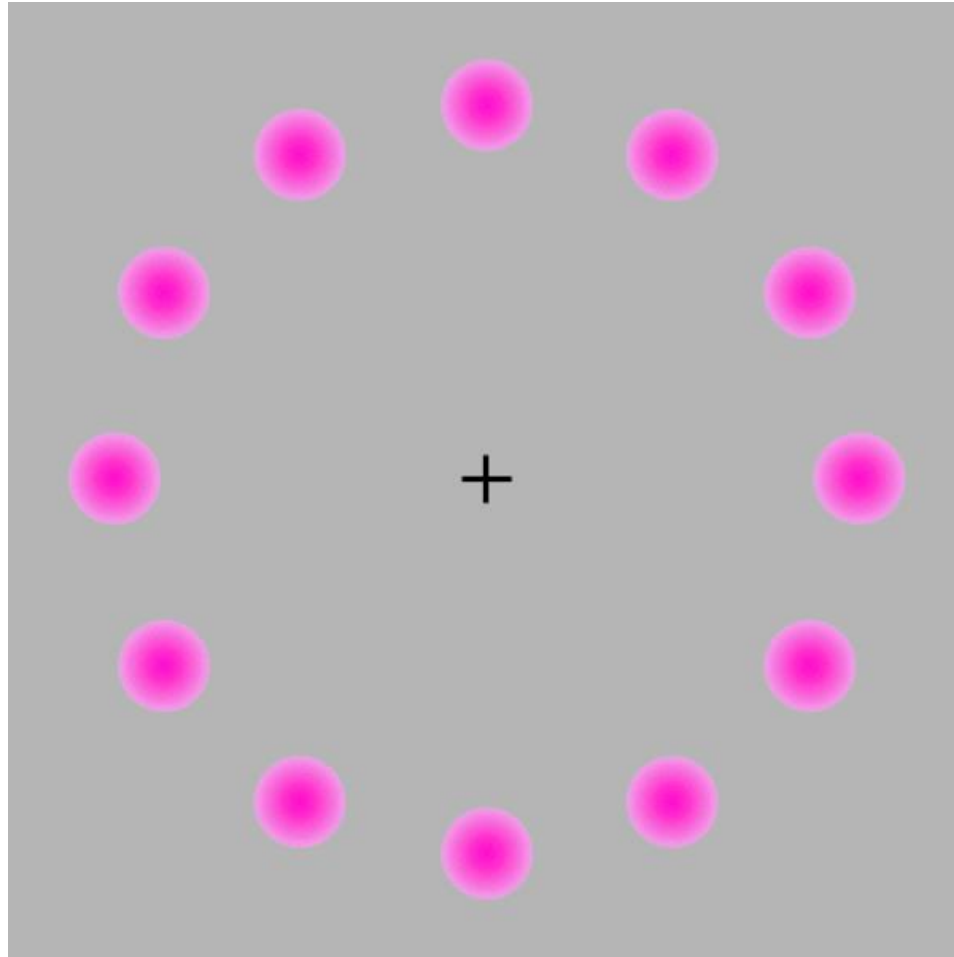
# More Illusions



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# More Illusions



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# More Illusions



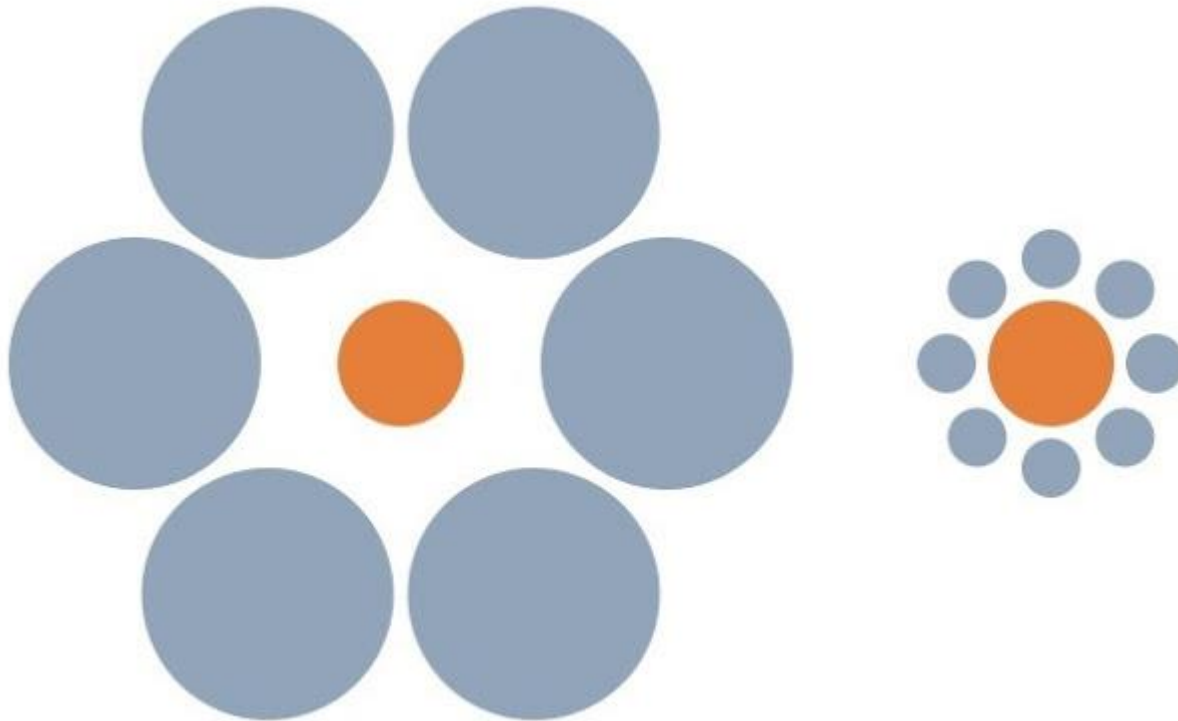
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# More Illusions

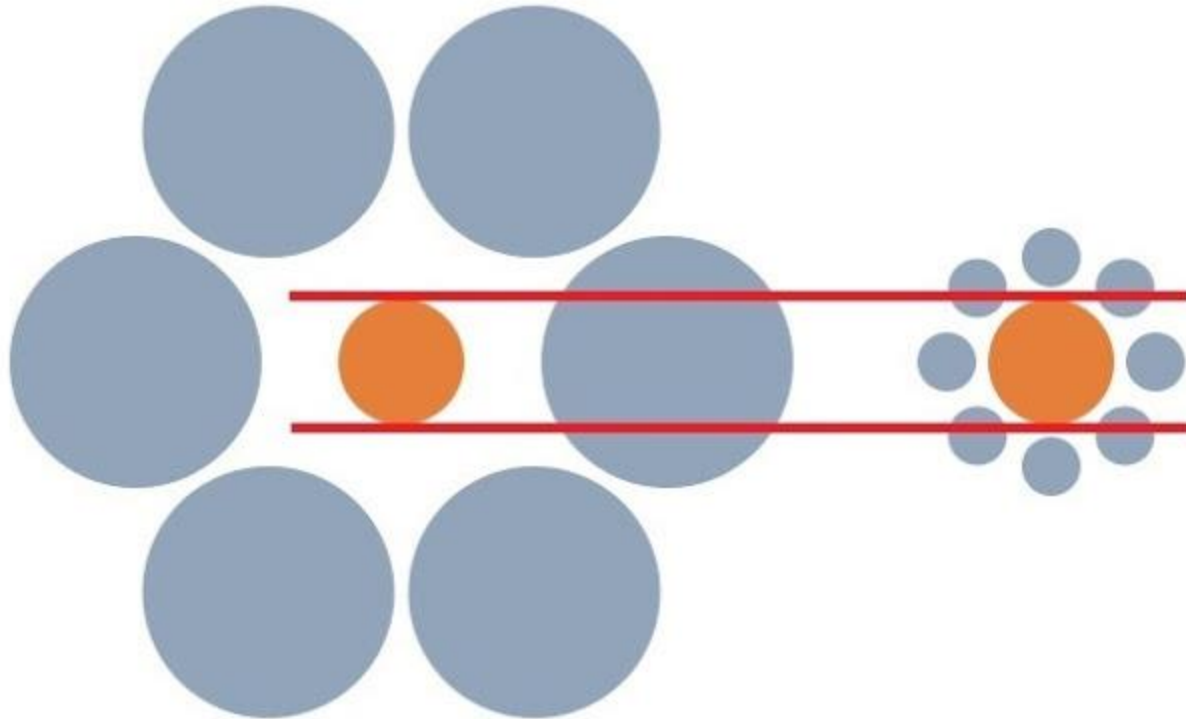


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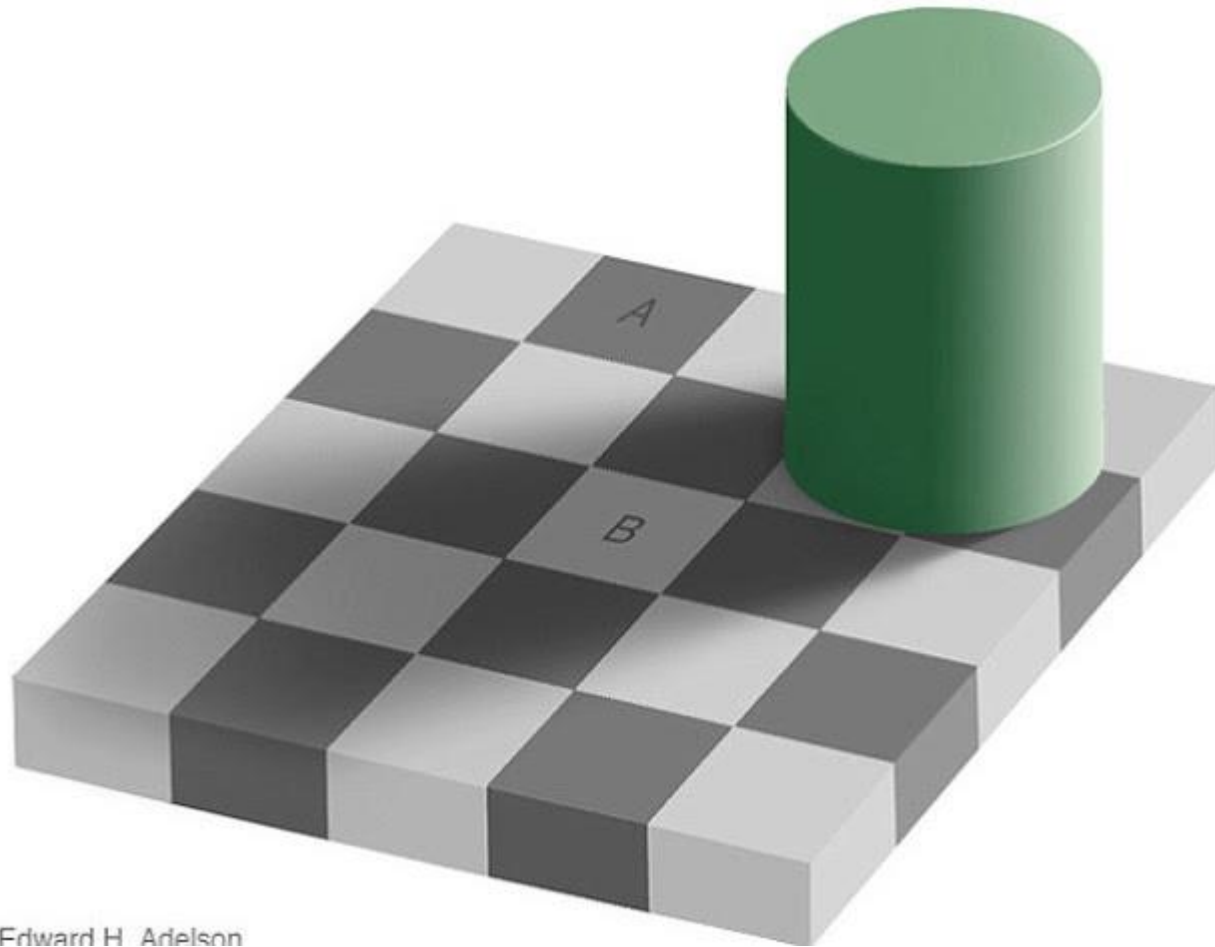
# More Illusions



# More Illusions



# More Illusions



Edward H. Adelson

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# More Illusions



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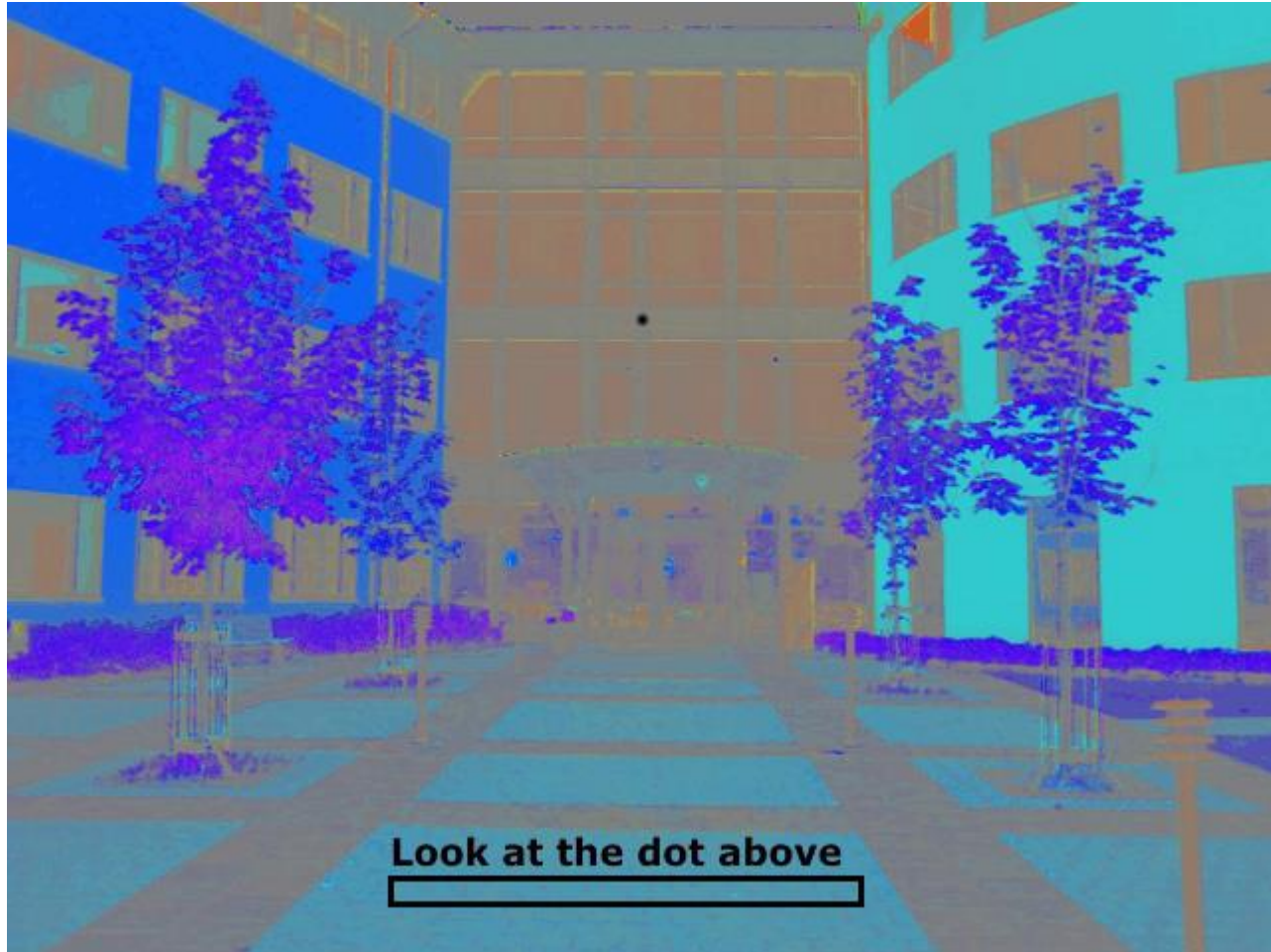
# More Illusions



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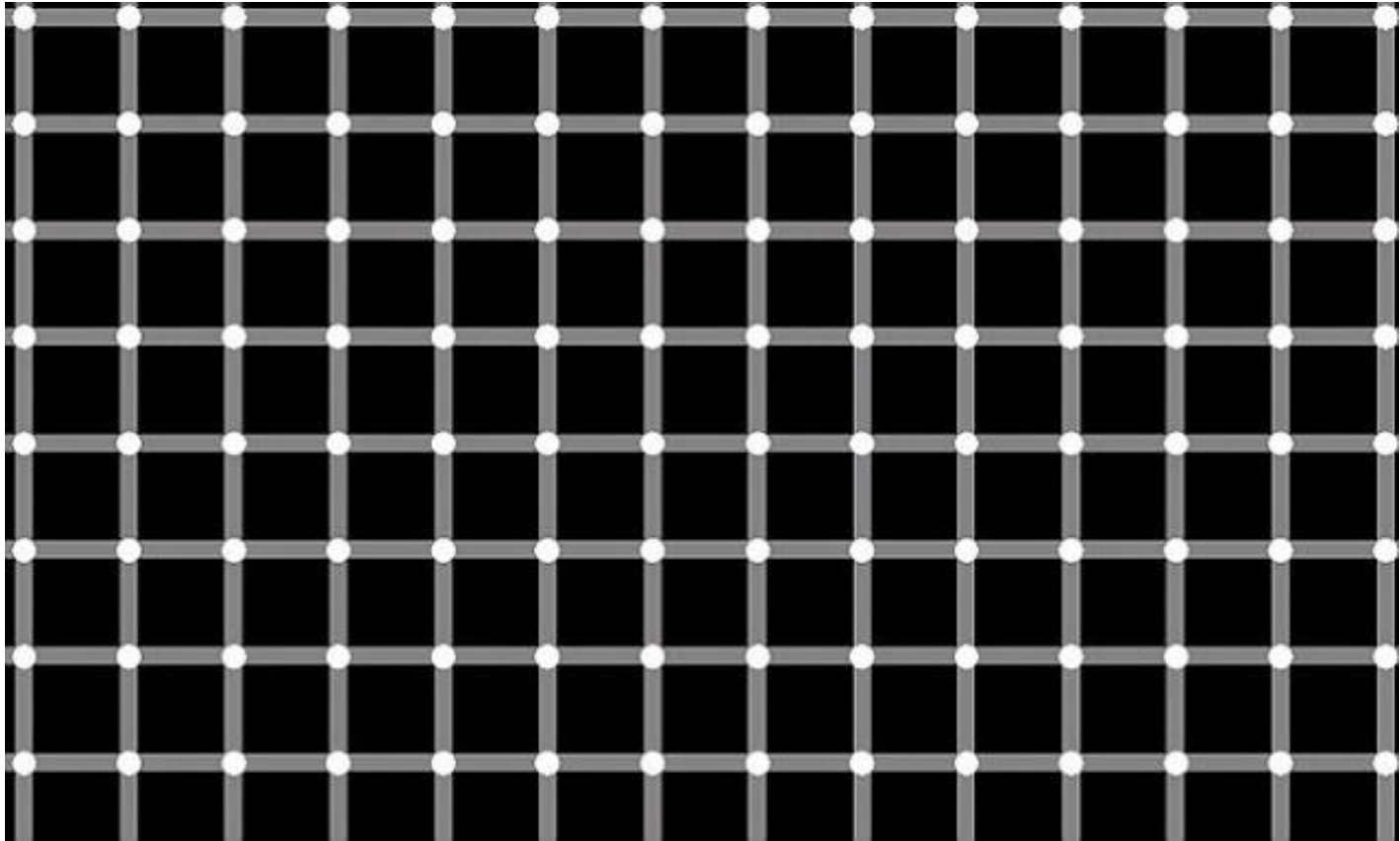


# More Illusions



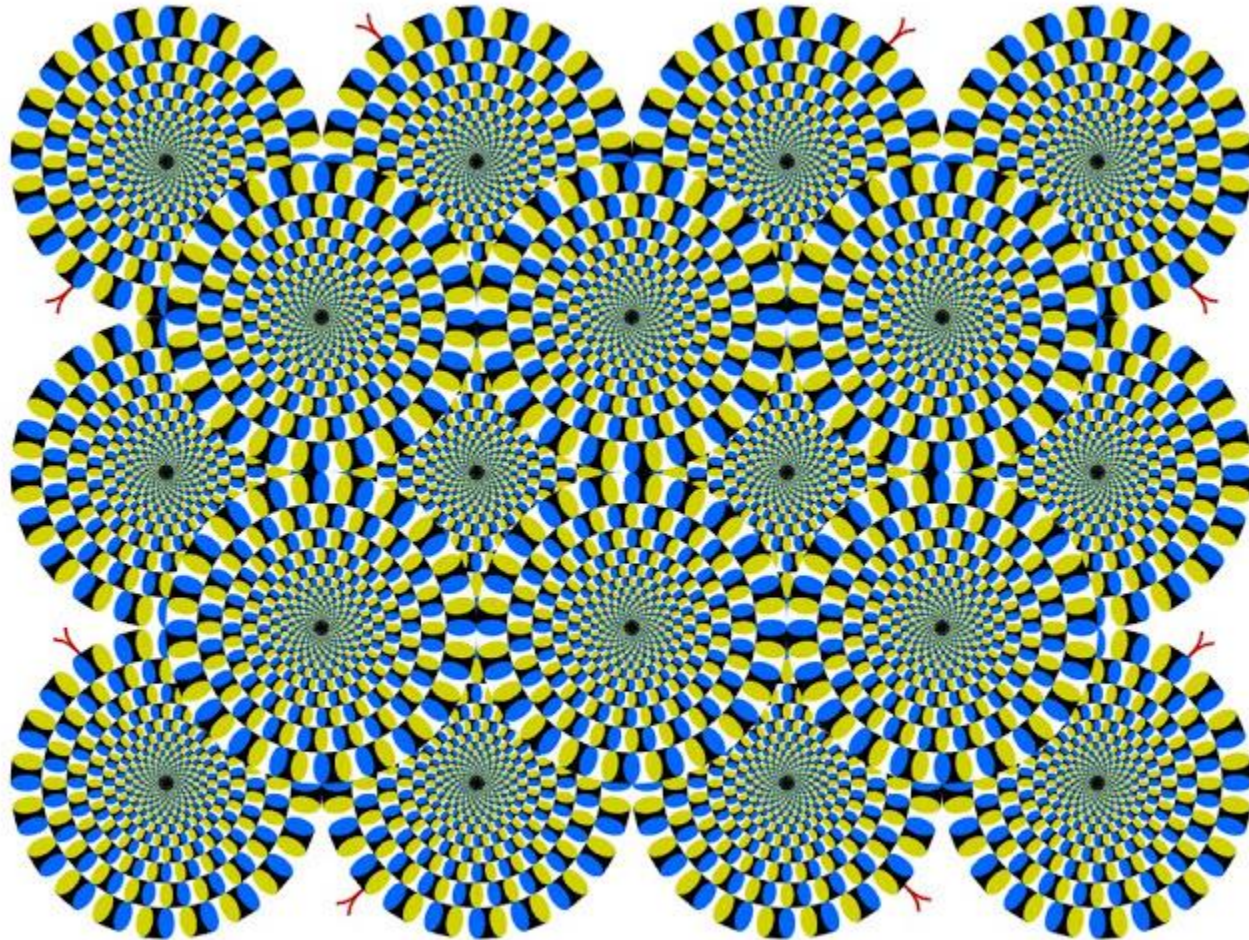
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# More Illusions



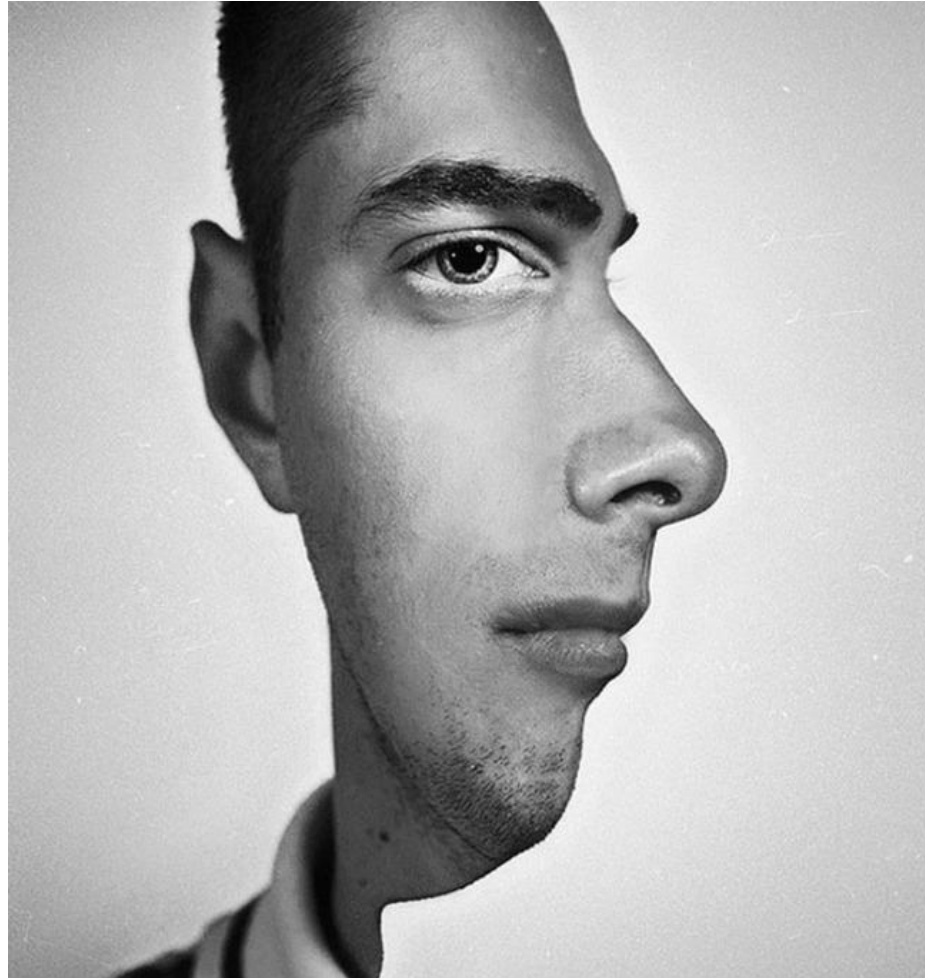
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# More Illusions



Mapi 17/18 - Computer Vision

# More Illusions



Mapi 17/18 - Computer Vision

# More Illusions



Mapi 17/18 - Computer Vision

# More Illusions



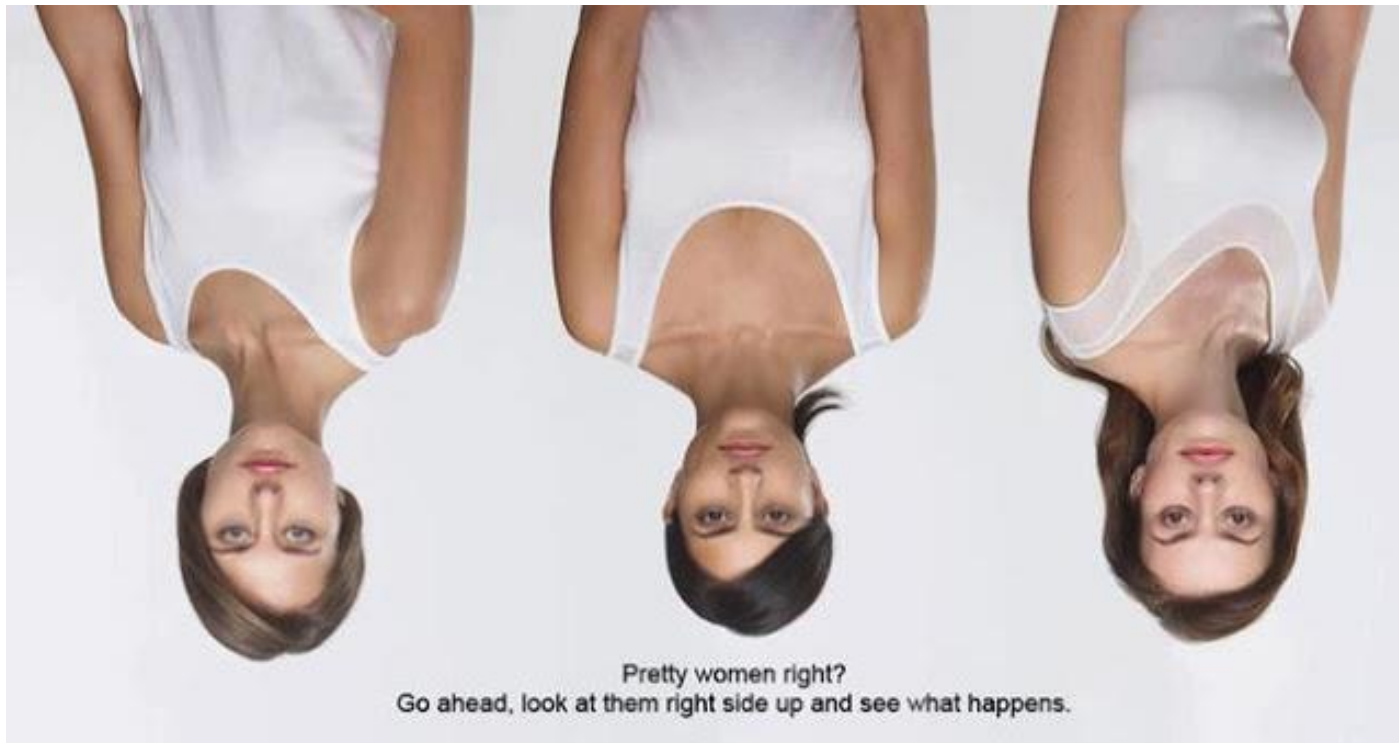
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# More Illusions



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# More Illusions

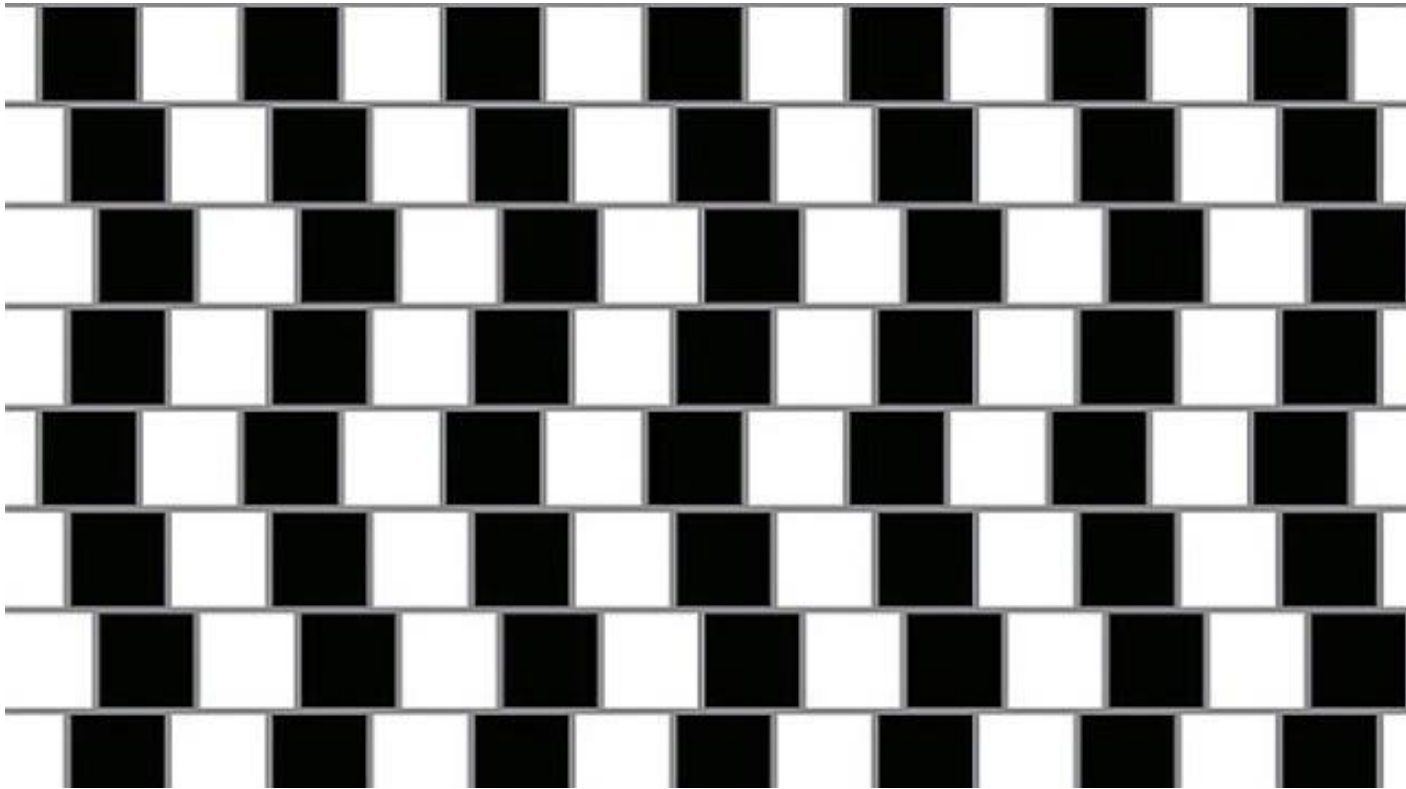




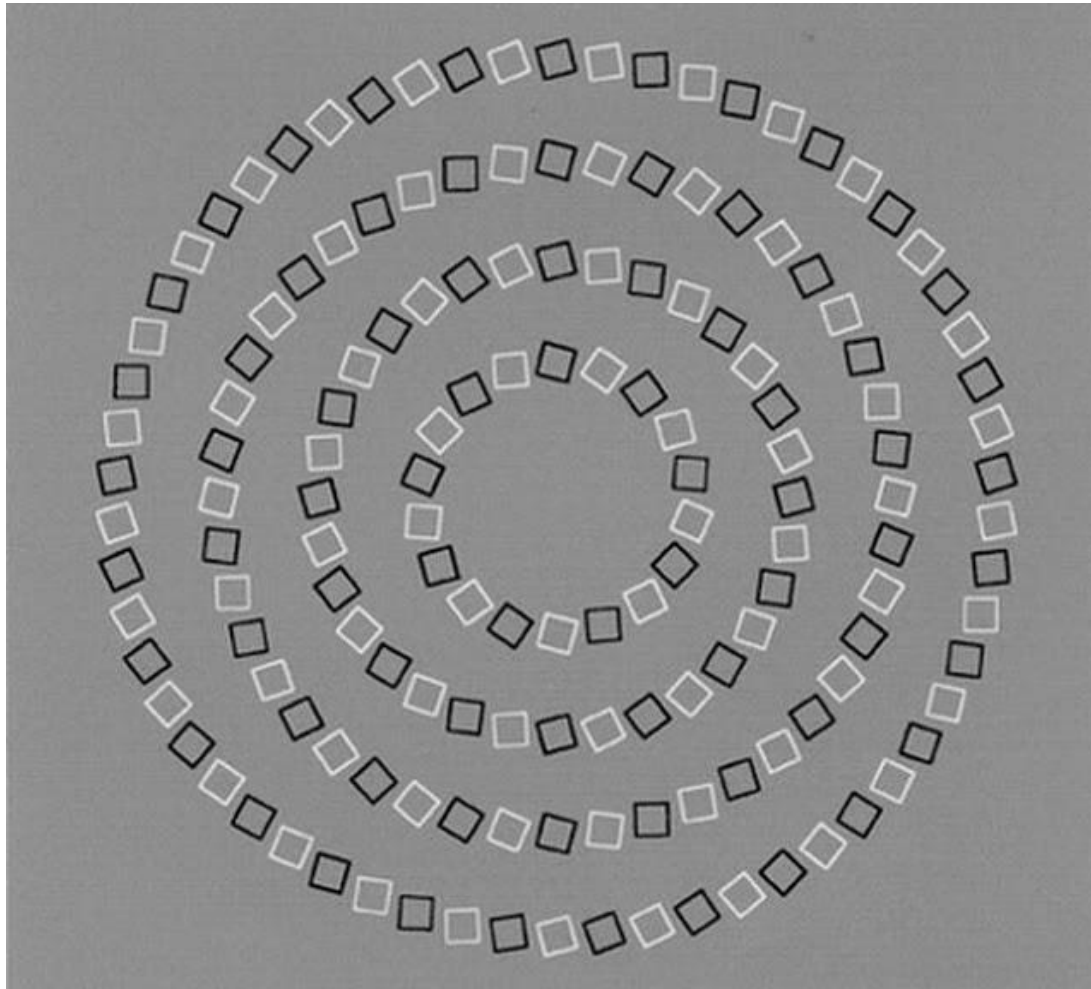
# More Illusions



# More Illusions

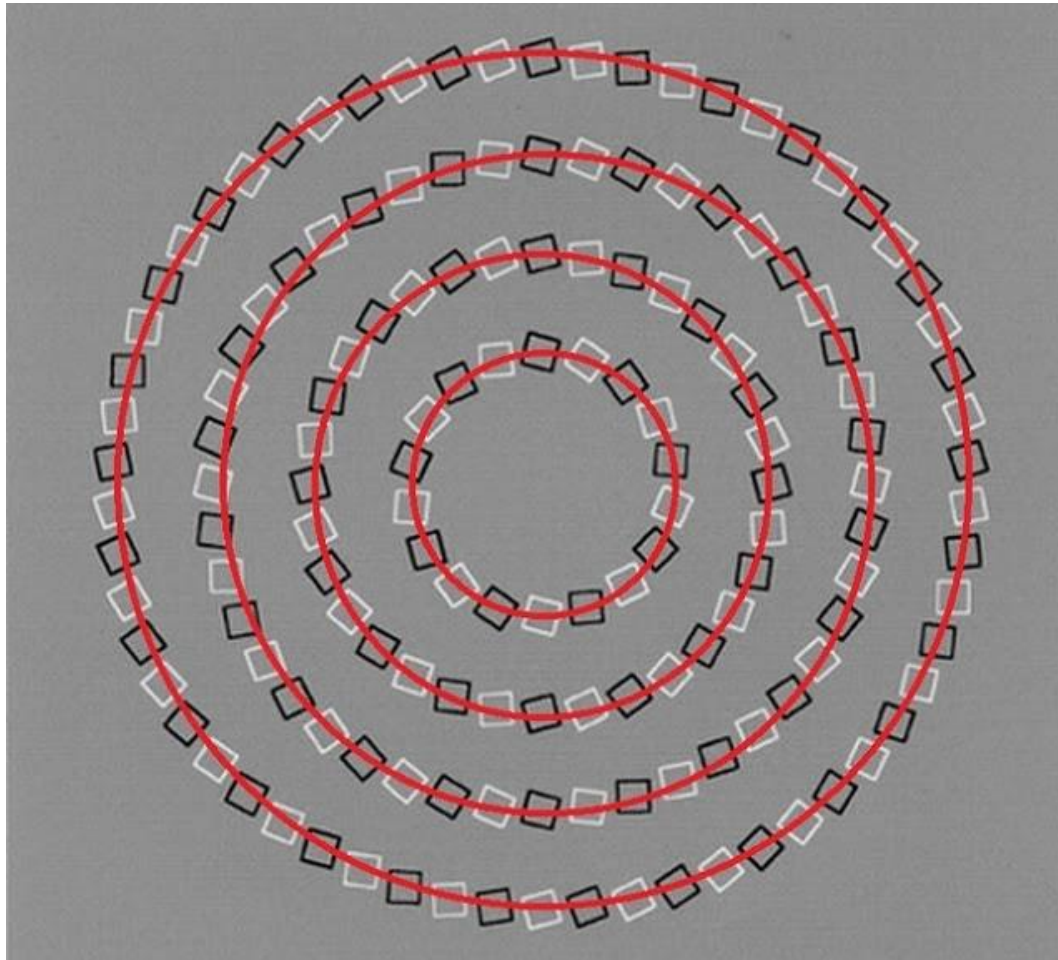


# More Illusions



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# More Illusions



Mapi 17/18 - Computer Vision

# More Illusions



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# More Illusions



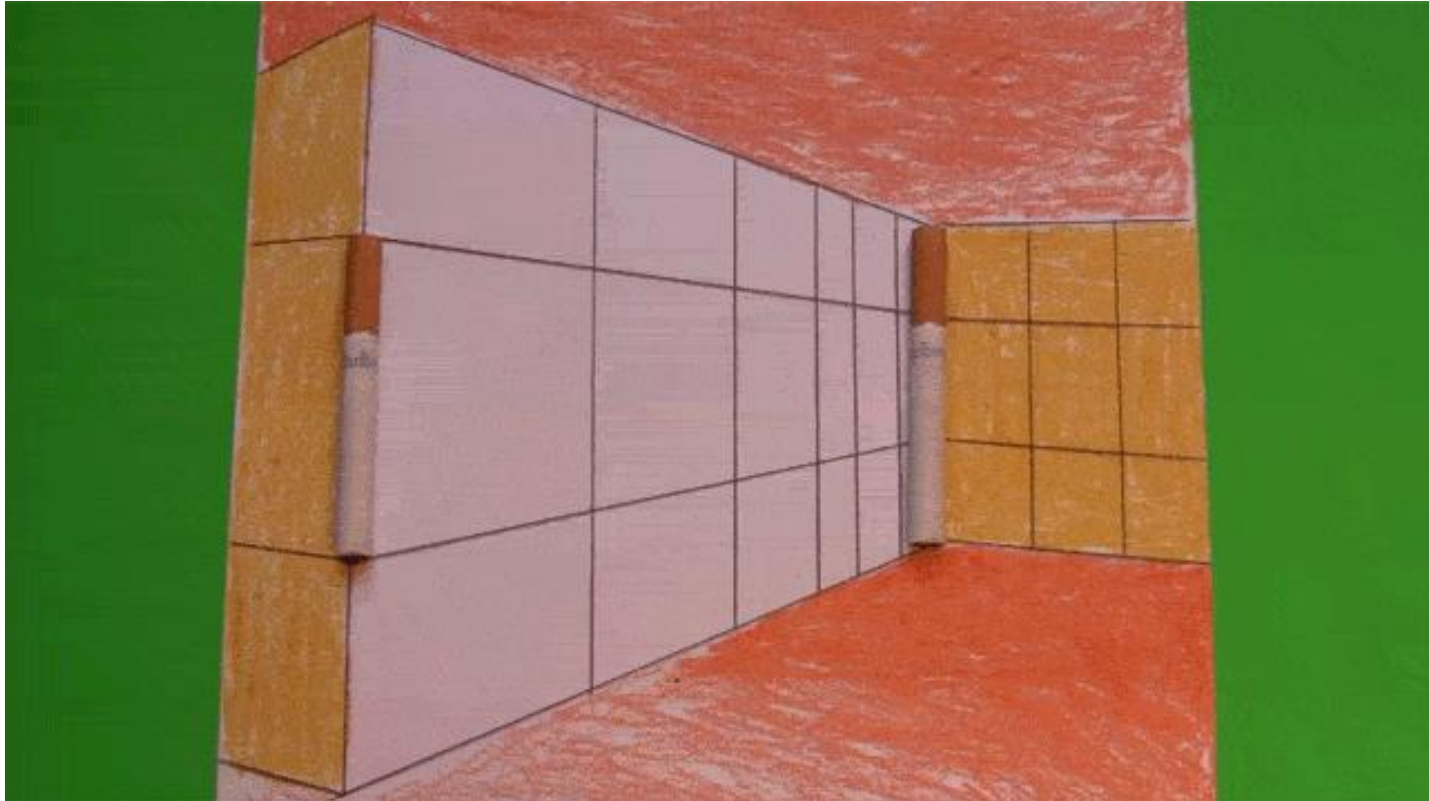
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# More Illusions



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# More Illusions



<http://gizmodo.uol.com.br/20-ilusoes-opticas-para-confundir-a-sua-mente/>

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# More Illusions



<http://gizmodo.uol.com.br/20-ilusoes-opticas-para-confundir-a-sua-mente/>

Mapi 17/18 - Computer Vision

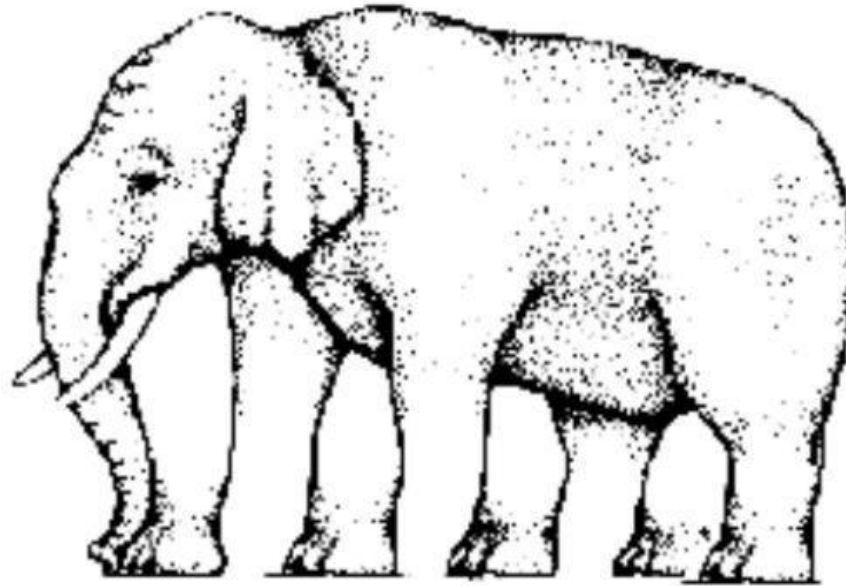
# More Illusions



<http://www.ilusoesopticas.com>

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# More Illusions

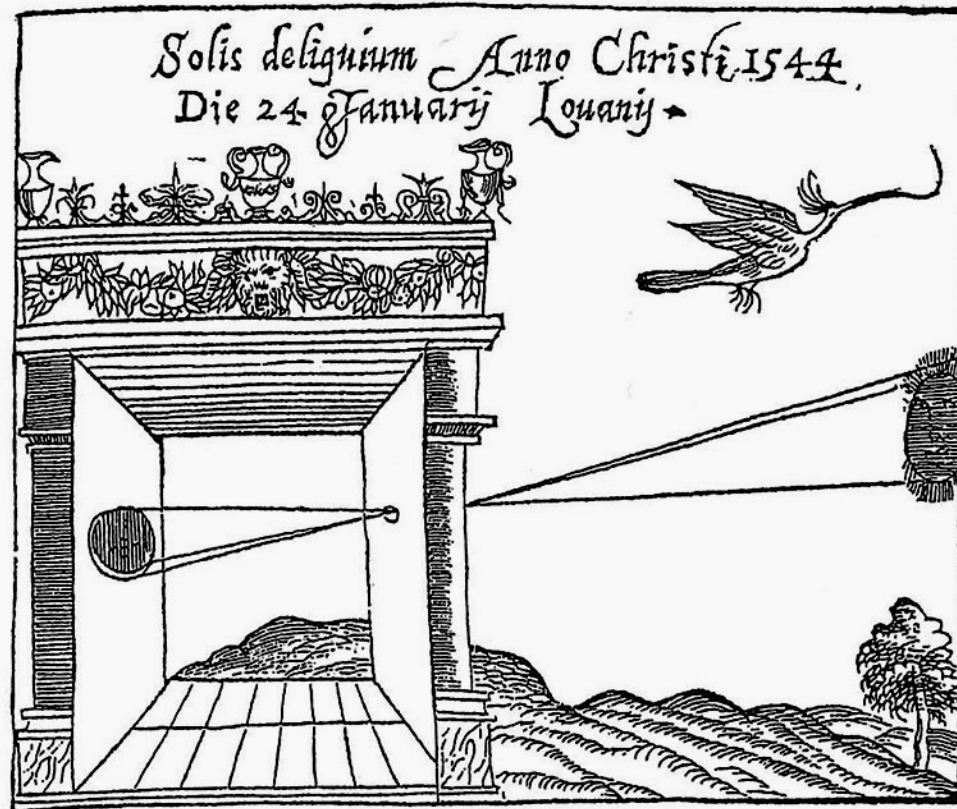


**Quantas pernas tem o elefante?**

# Outline

- **Image Formation**
  - The Human Visual System
  - Image Capturing Systems
- Digital Images
- Colour and Noise

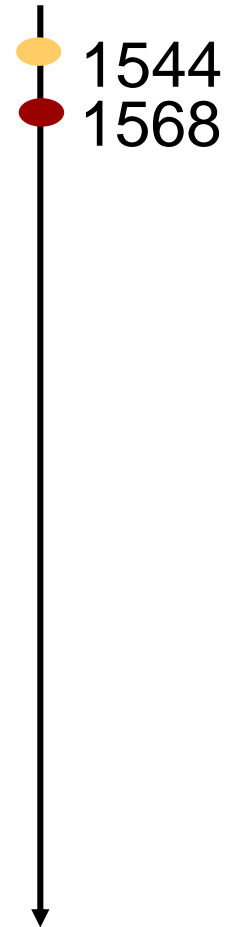
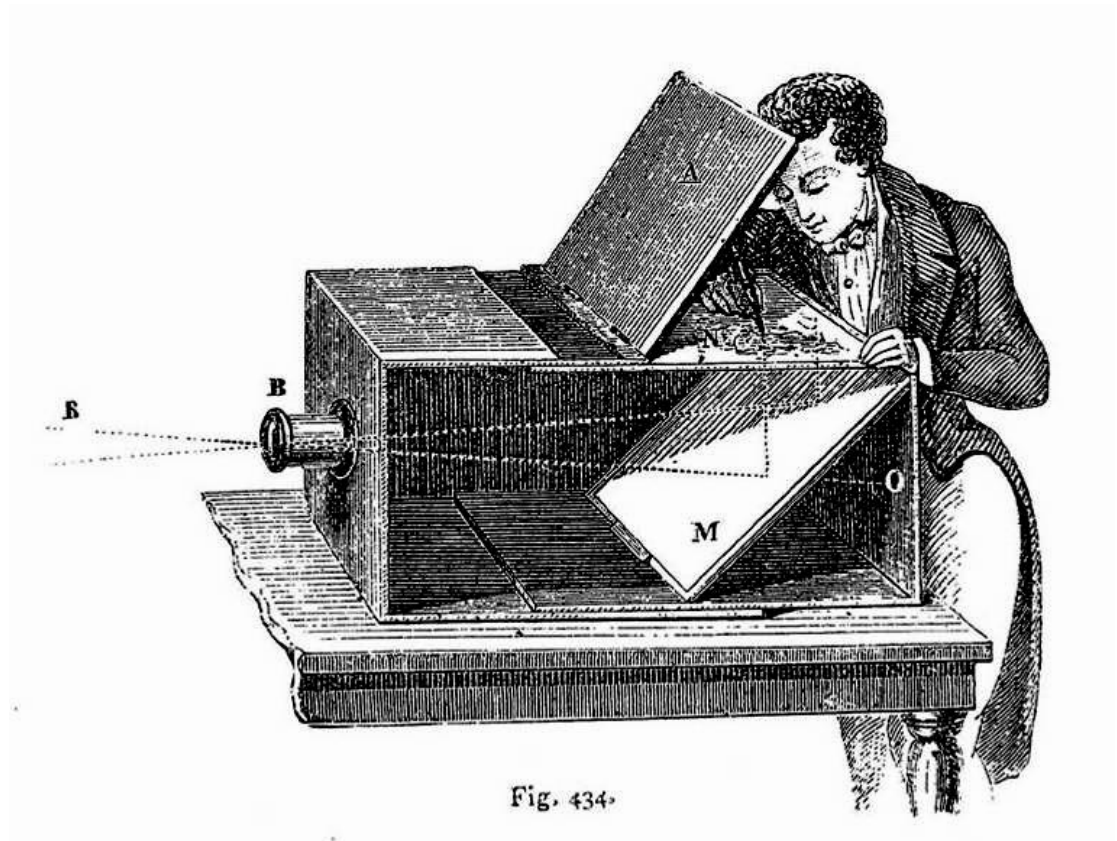
# A Brief History of Images



1544

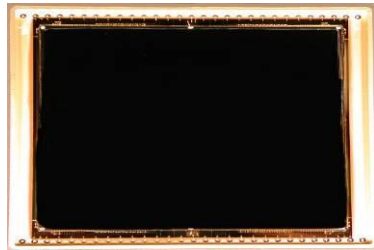
*Camera Obscura*, Gemma Frisius, 1544

# A Brief History of Images

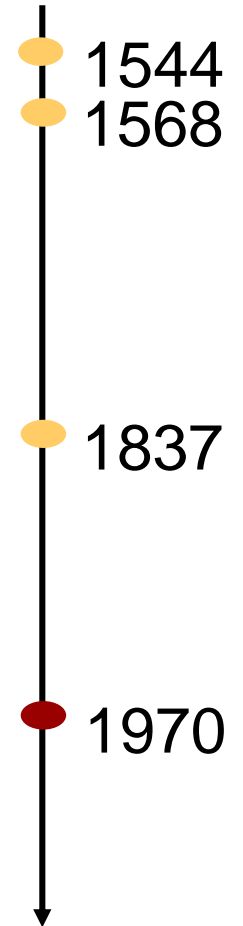


Lens Based Camera Obscura, 1568

# A Brief History of Images



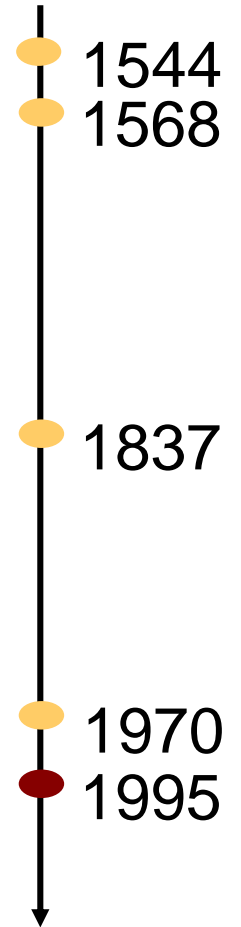
Silicon Image Detector, 1970



# A Brief History of Images

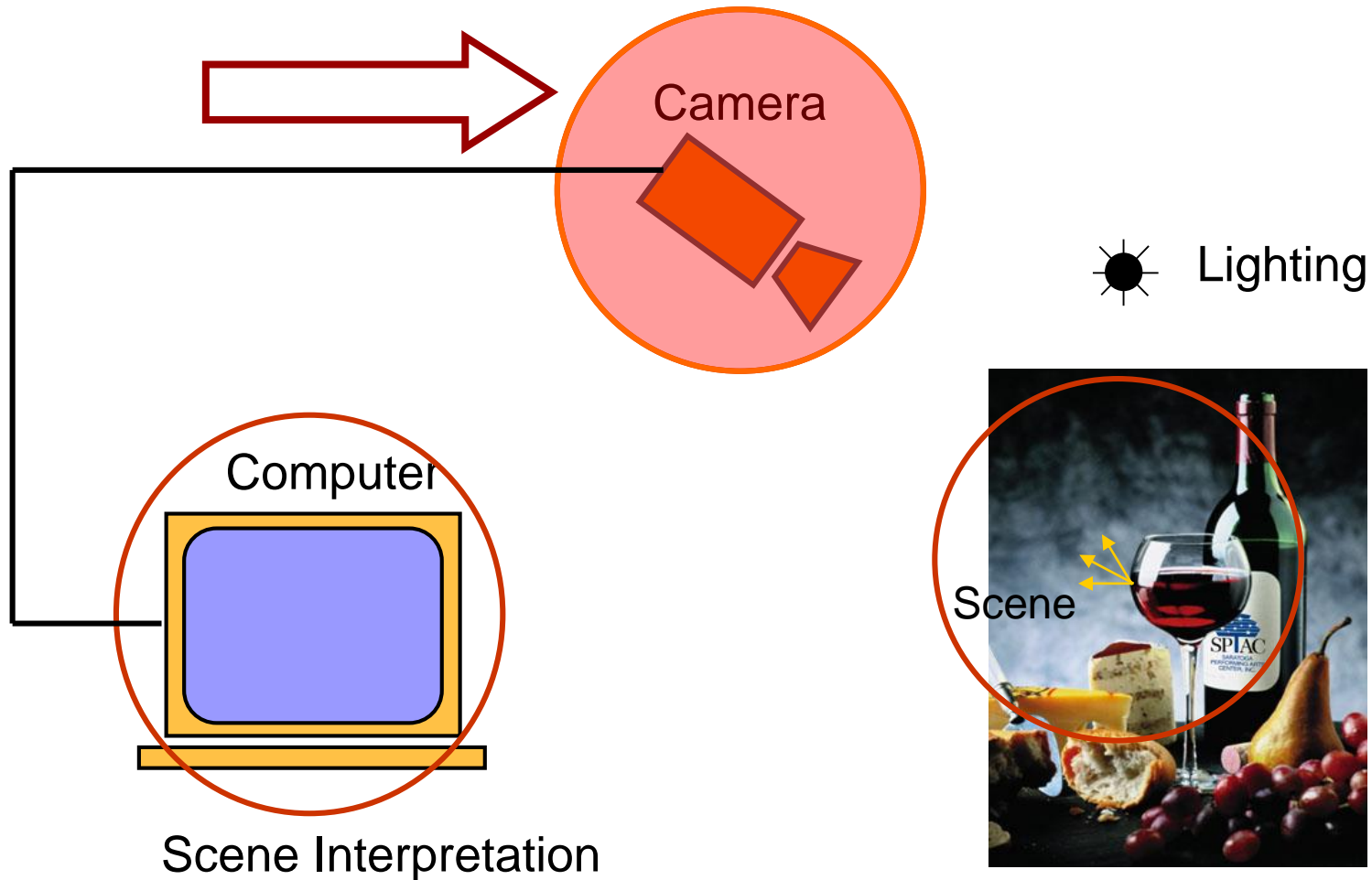


Digital Cameras

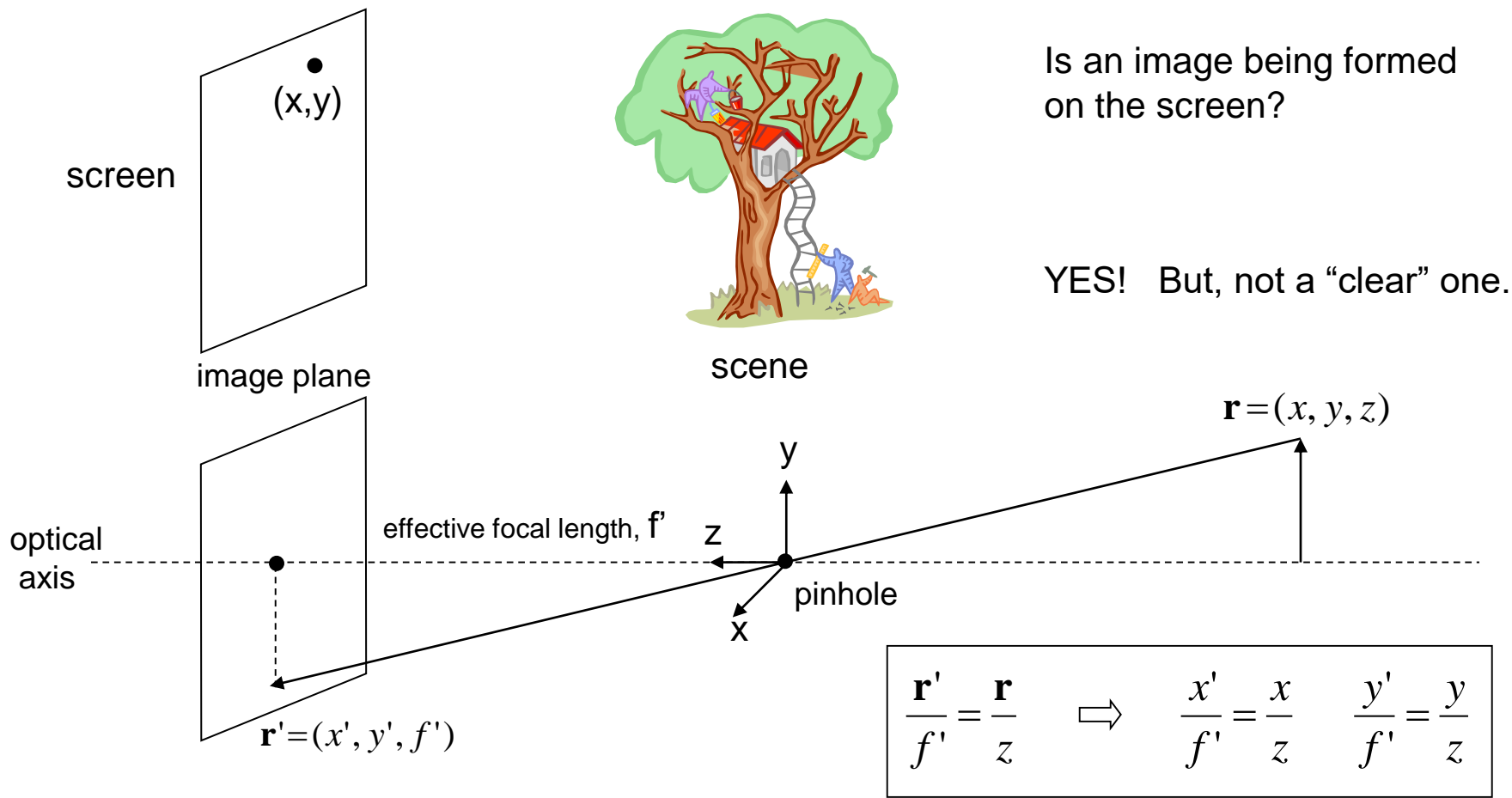




# Components of a Computer Vision System



# Pinhole and the Perspective Projection

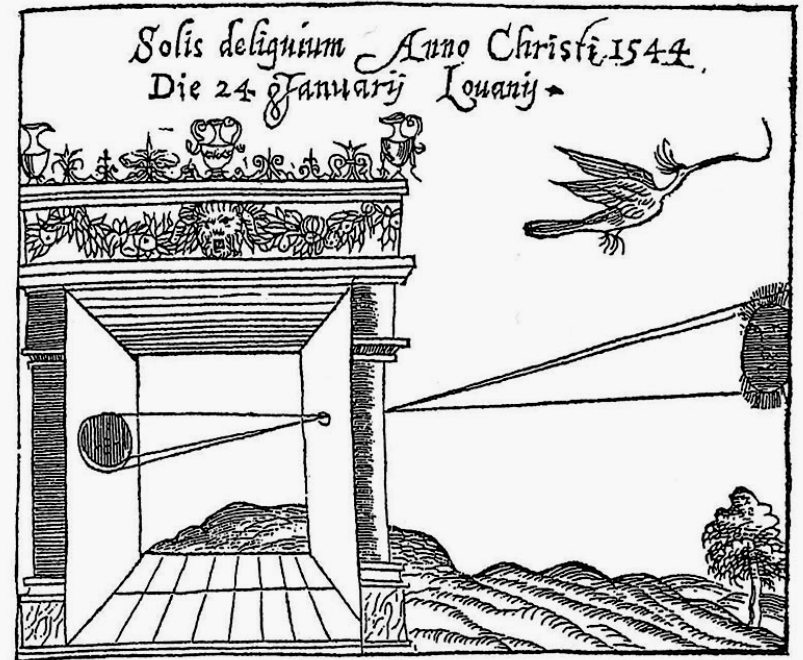


Is an image being formed on the screen?

YES! But, not a “clear” one.

# Pinhole Camera

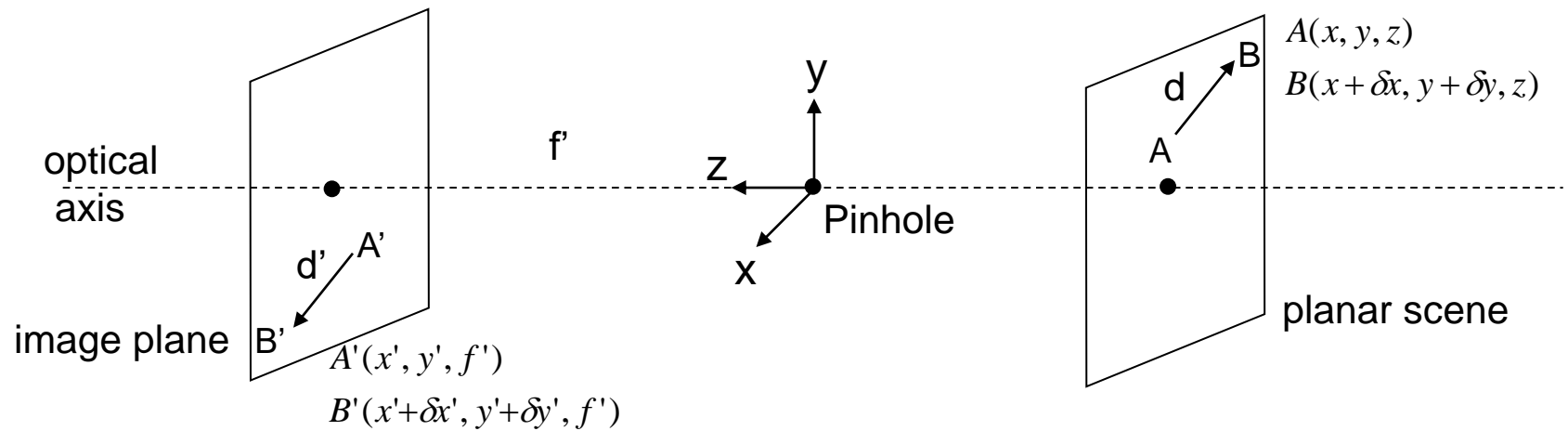
- Basically a pinhole camera is a box, with a tiny hole at one end and film or photographic paper at the other.
- Mathematically: out of all the light rays in the world, choose the set of light rays passing through a point and projecting onto a plane.



Do it by yourself!!!!

<http://www.sbfisica.org.br/fne/Vol8/Num2/v08n02a05.pdf>

# Magnification



From perspective projection:

$$\frac{x'}{f'} = \frac{x}{z} \quad \frac{y'}{f'} = \frac{y}{z}$$



Magnification:

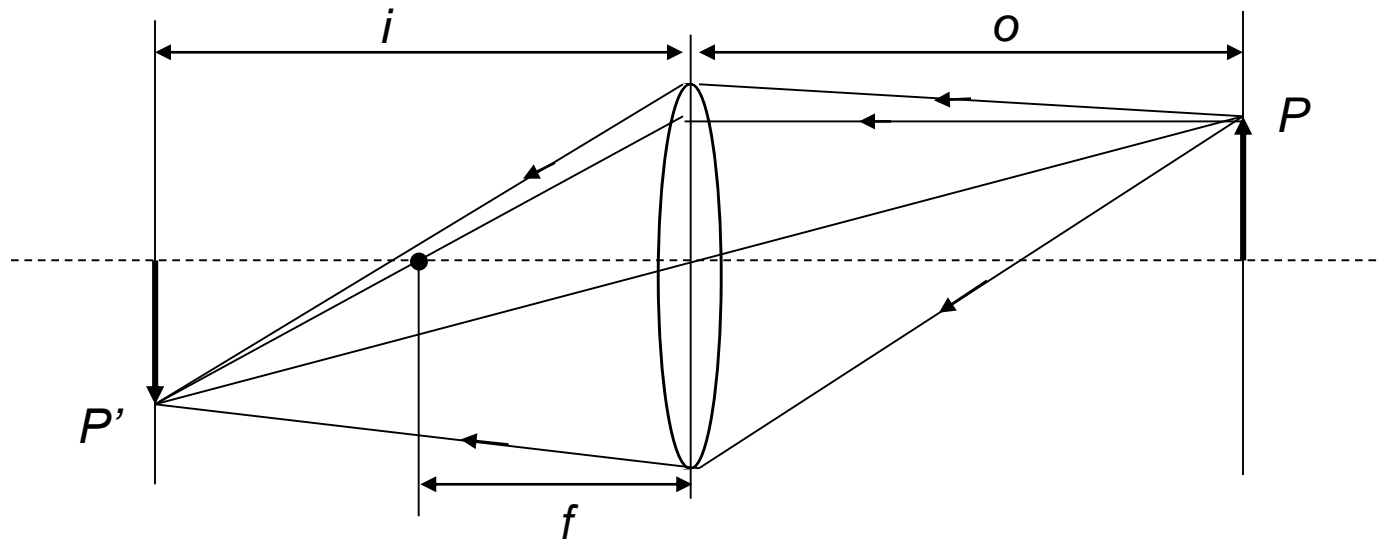
$$m = \frac{d'}{d} = \frac{\sqrt{(\delta x')^2 + (\delta y')^2}}{\sqrt{(\delta x)^2 + (\delta y)^2}} = \frac{f'}{z}$$

$$\frac{x' + \delta x'}{f'} = \frac{x + \delta x}{z} \quad \frac{y' + \delta y'}{f'} = \frac{y + \delta y}{z}$$

$$\frac{Area_{image}}{Area_{scene}} = m^2$$

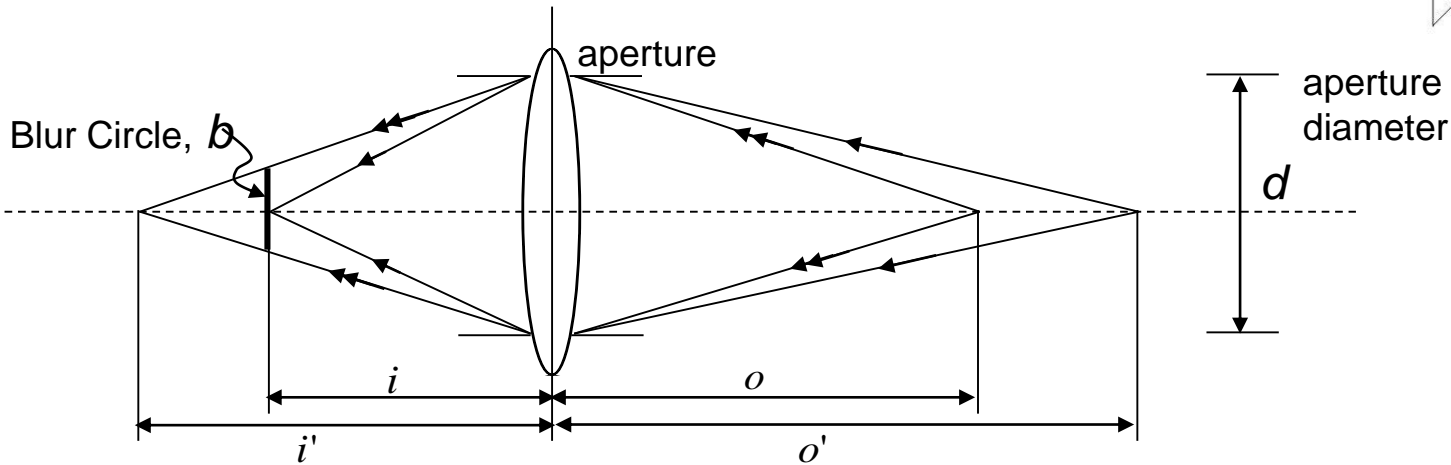
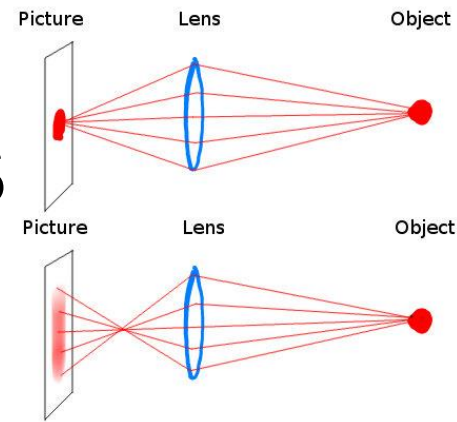
# Image Formation using Lenses

- Lenses are used to avoid problems with pinholes.
- Ideal Lens: Same projection as pinhole but gathers more light!



- Gaussian Thin Lens Formula:  $\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$
- $f$  is the focal length of the lens – determines the lens's ability to refract light

# Focus and Defocus



- Gaussian Law:

$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$$



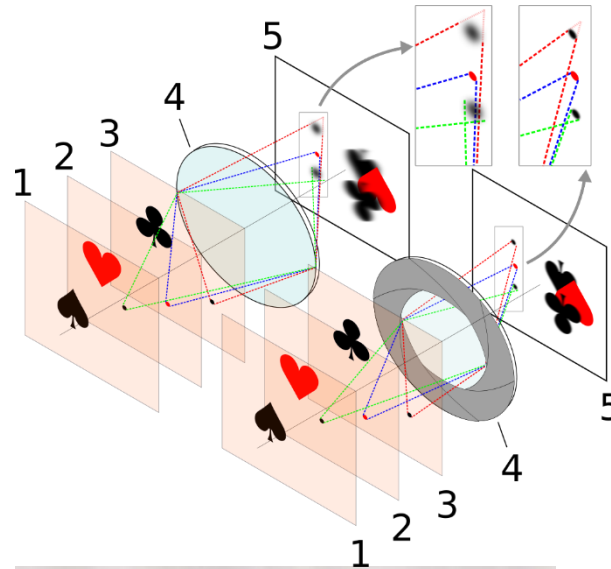
$$(i' - i) = \frac{f}{(o' - f)} \frac{f}{(o - f)} (o - o')$$

$$\frac{1}{i'} + \frac{1}{o'} = \frac{1}{f}$$

- In theory, only one scene plane is in focus.

# Depth of Field

- Range of object distances over which image is sufficiently well focused.
- Range for which *blur circle* is less than the resolution of the sensor.



[http://images.dpchallenge.com/images\\_portfolio/27920/print\\_preview/116336.jpg](http://images.dpchallenge.com/images_portfolio/27920/print_preview/116336.jpg)

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# Image Sensors

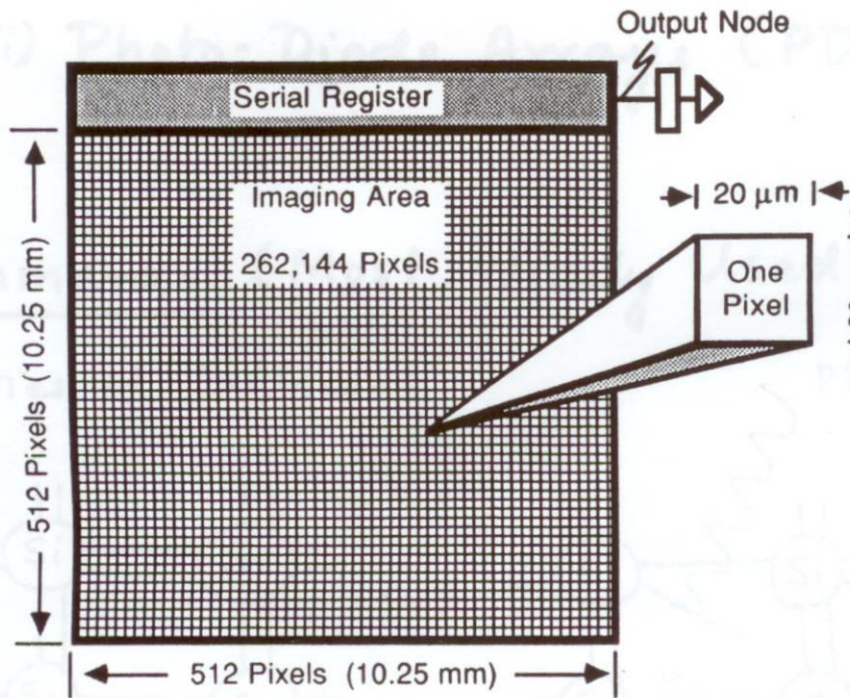


FIG. 4. Typical 512 × 512 CCD.

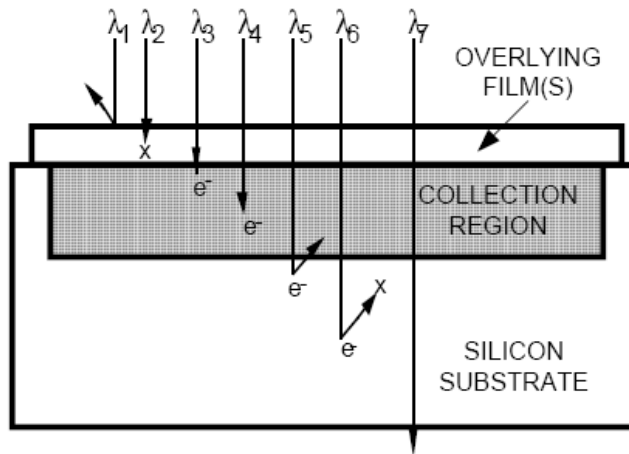
## Considerations

- Speed
- Resolution
- Signal / Noise Ratio
- Cost



# Image Sensors

- Convert light into an electric charge

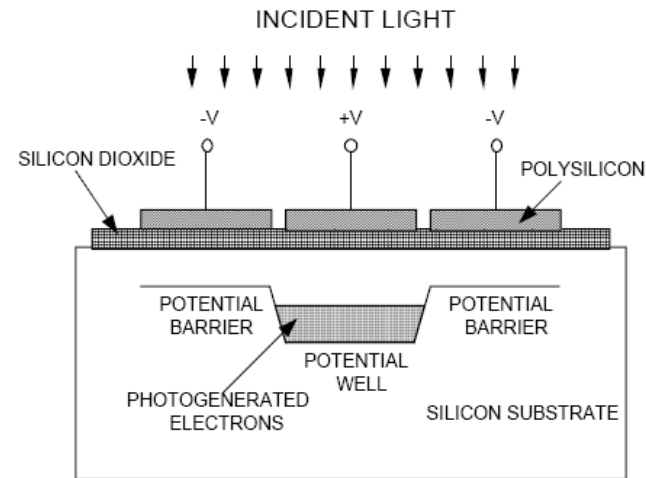
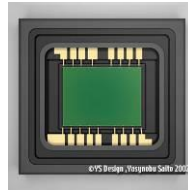


CCD (charge coupled device)

Higher dynamic range

High uniformity

Lower noise

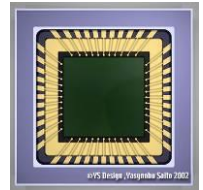


CMOS (complementary metal  
Oxide semiconductor)

Lower voltage

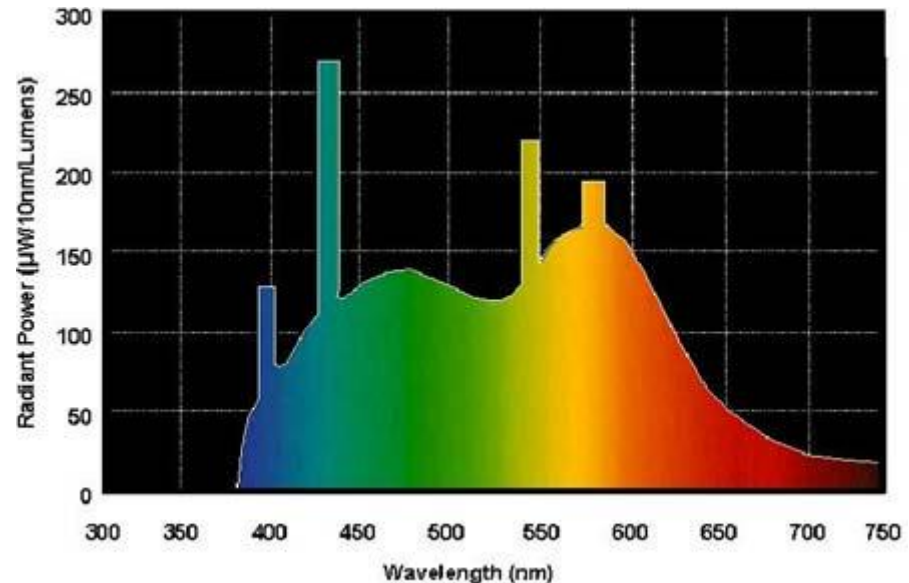
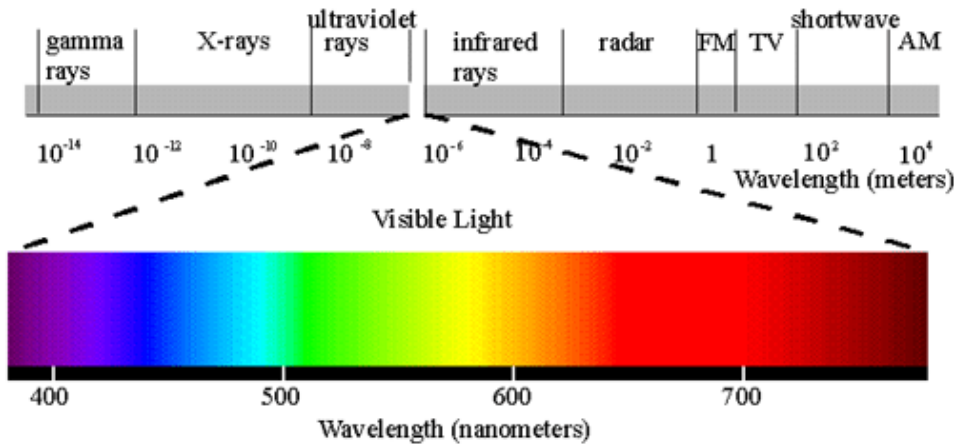
Higher speed

Lower system complexity



# Sensing Brightness

Incoming light has a spectral distribution  $p(\lambda)$

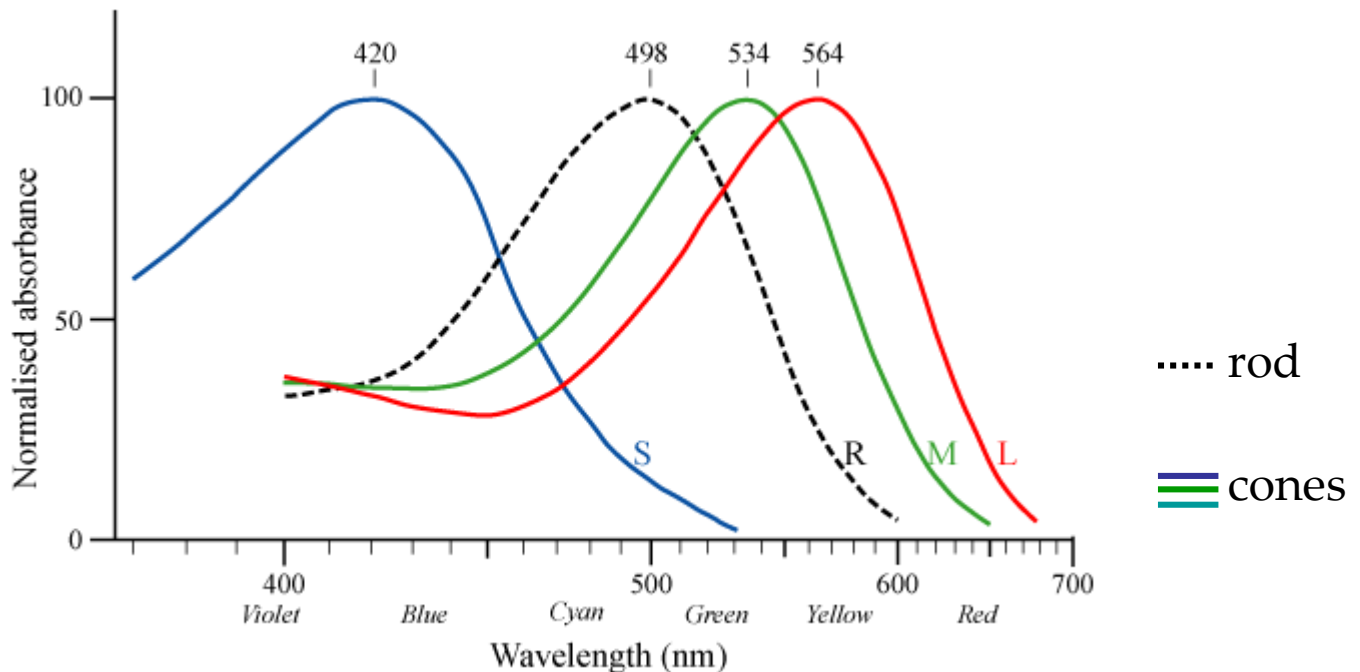


So the pixel intensity becomes

$$I = k \int_{-\infty}^{\infty} q(\lambda)p(\lambda)d\lambda$$

# How do we sense colour?

- Do we have infinite number of filters?

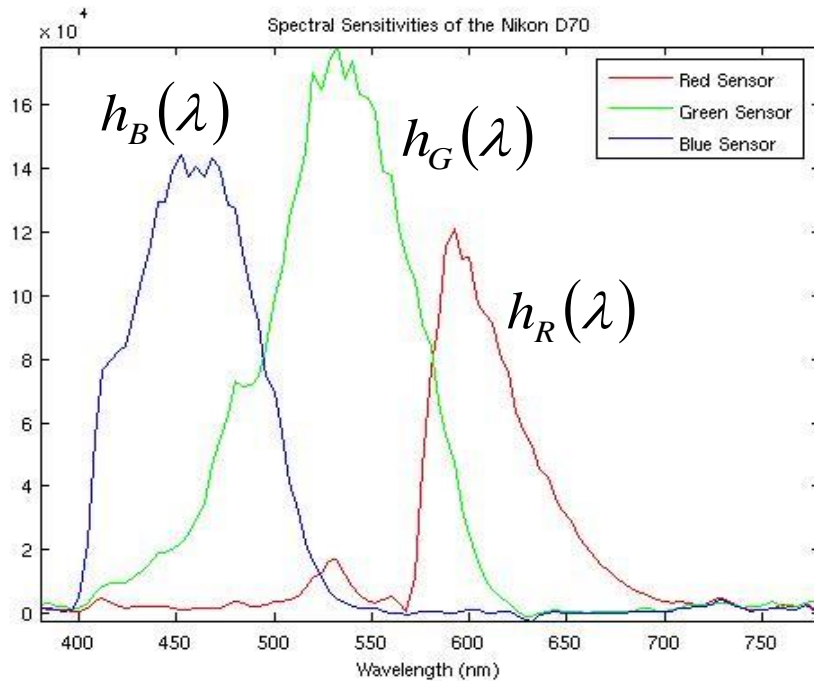


Three filters of different spectral responses

# Sensing Colour

- **Tristimulus (trichromatic) values**  $(I_R, I_G, I_B)$

Camera's spectral response functions:  $h_R(\lambda), h_G(\lambda), h_B(\lambda)$

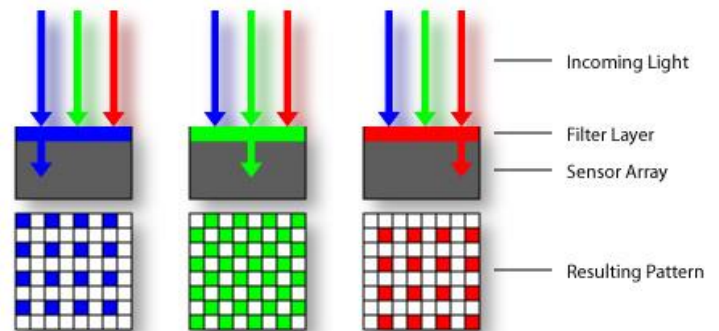
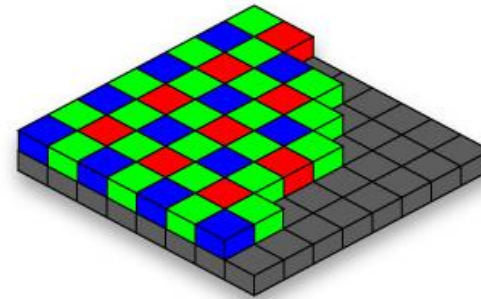
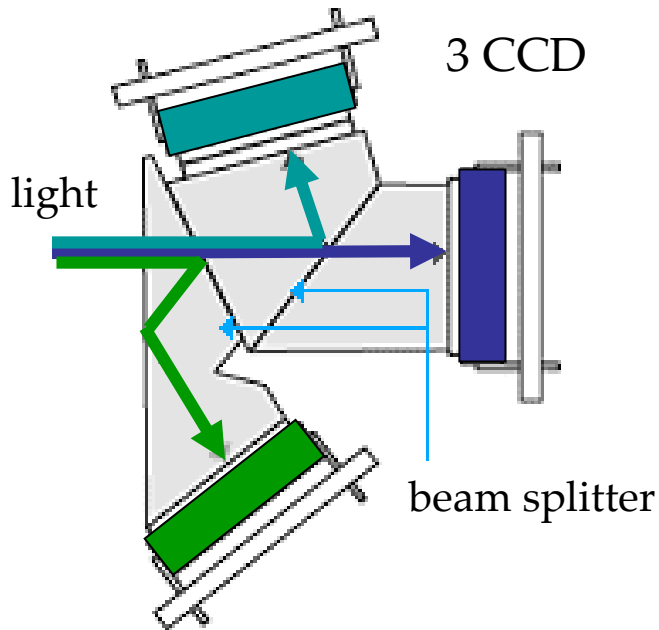


$$I_R = k \int_{-\infty}^{\infty} h_R(\lambda) p(\lambda) d\lambda$$

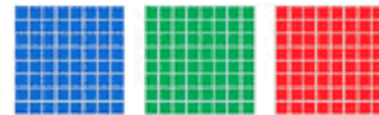
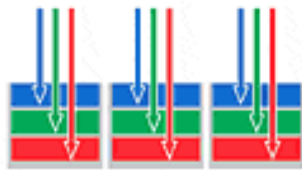
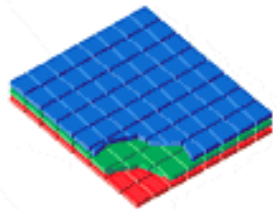
$$I_G = k \int_{-\infty}^{\infty} h_G(\lambda) p(\lambda) d\lambda$$

$$I_B = k \int_{-\infty}^{\infty} h_B(\lambda) p(\lambda) d\lambda$$

# Sensing Colour



Bayer pattern

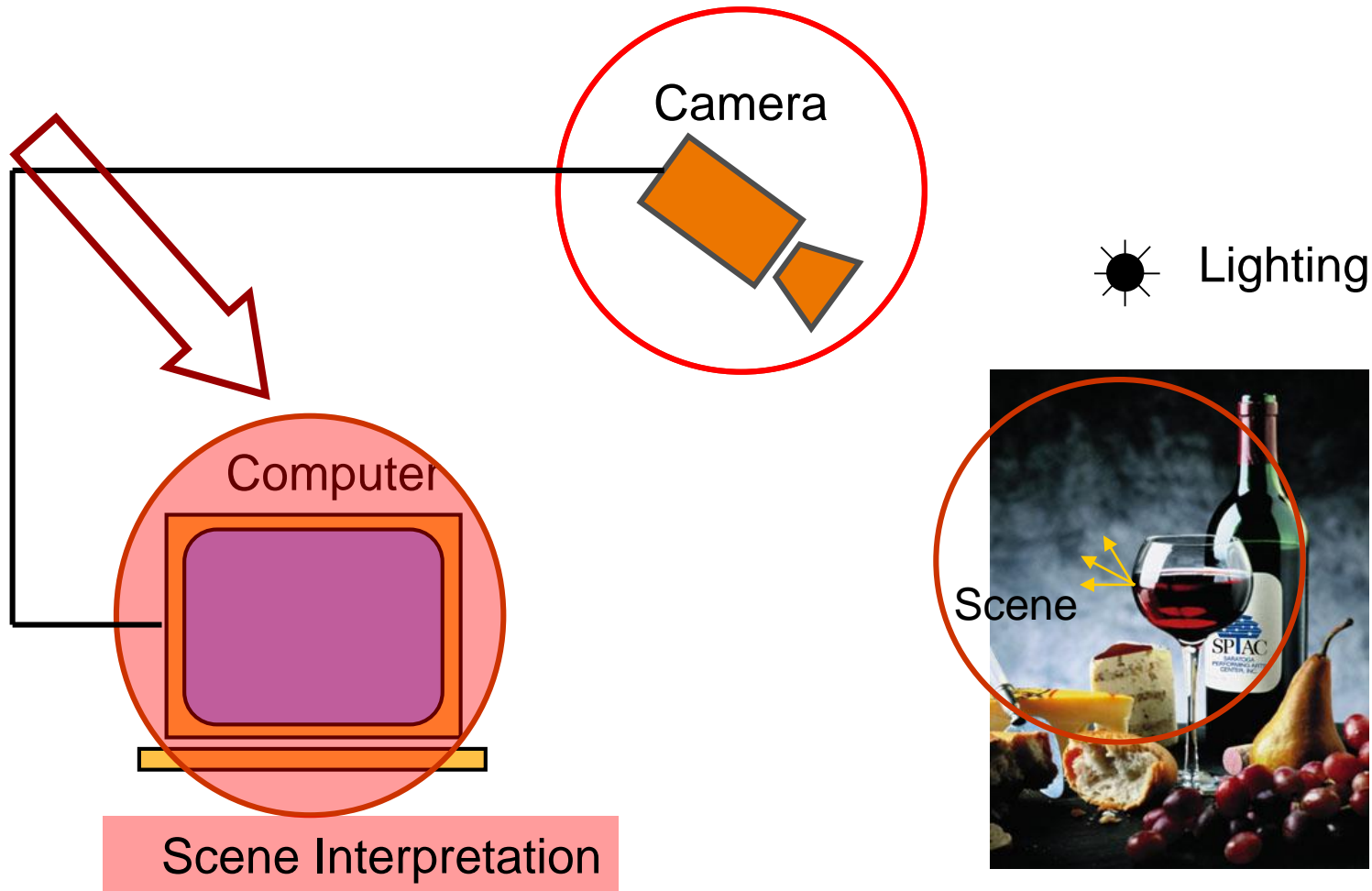


Foveon X3™

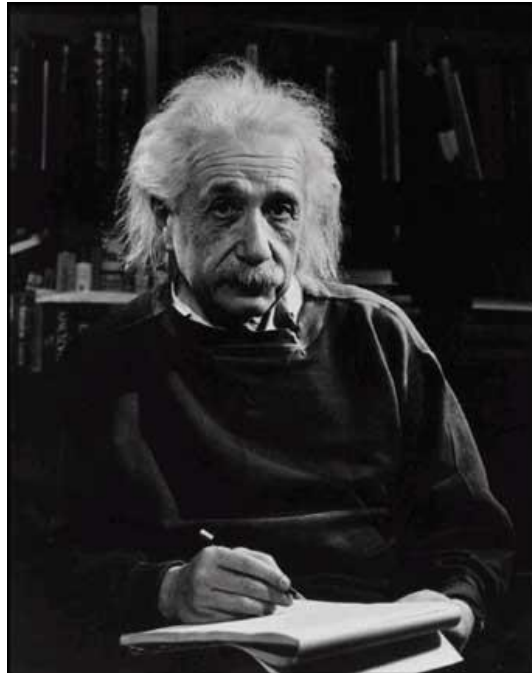
# Outline

- Image Formation
- **Digital Images**
  - Sampling
  - Data Structures
  - Histograms
- Colour and Noise

# Components of a Computer Vision System



# Digital Images



What we see

0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

What a computer sees



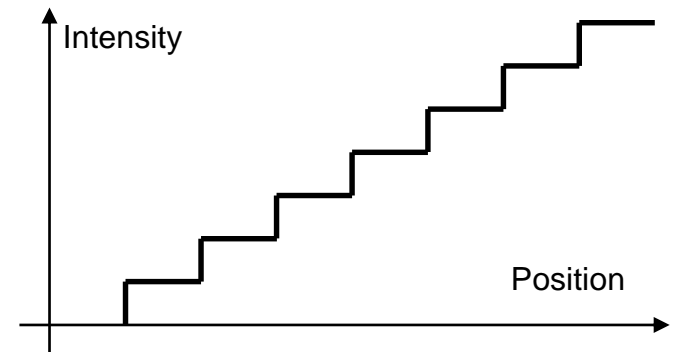
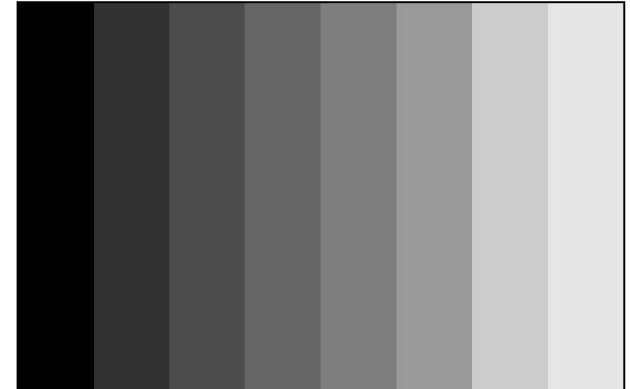
# Simple Image Model

- Image as a 2D light-intensity function

$$f(x, y)$$

- Continuous
- Non-zero, finite value

$$0 < f(x, y) < \infty$$

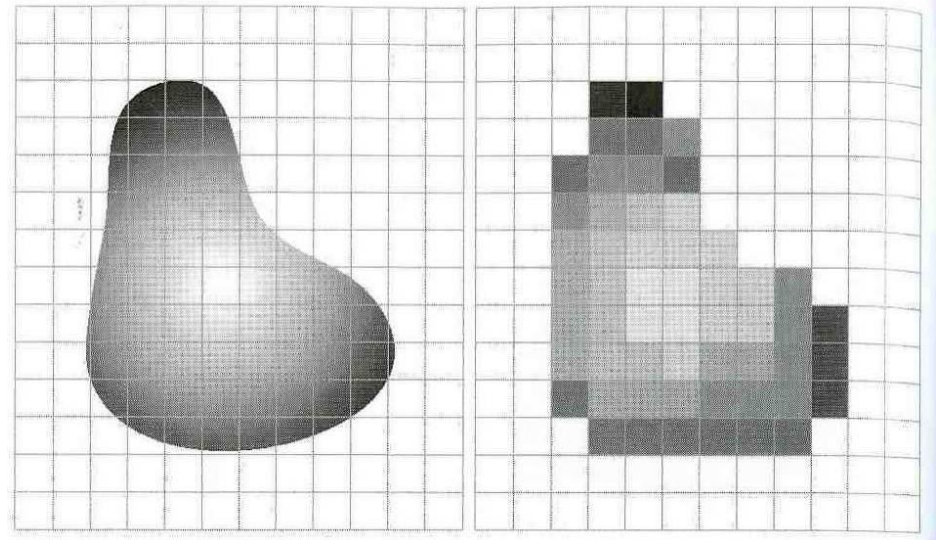


[Gonzalez & Woods]

# Analog to Digital

The scene is:

- **projected** on a 2D plane,
- **sampled** on a regular grid, and each sample is
- **quantized** (rounded to the nearest integer)

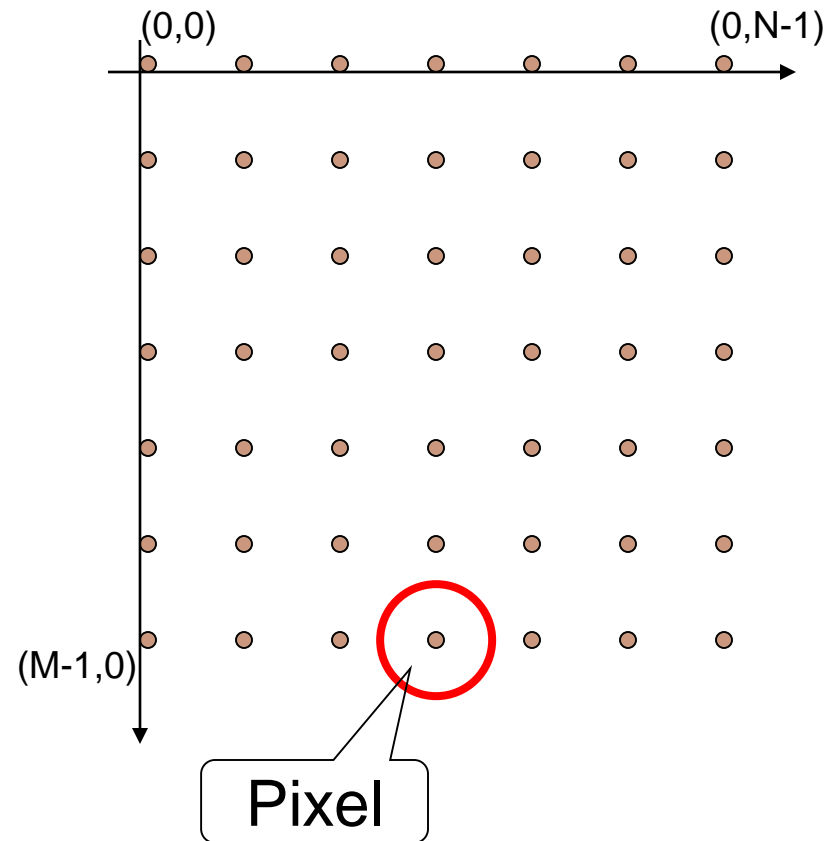


$$f(i, j) = \text{Quantize}\{f(i\Delta, j\Delta)\}$$

# Images as Matrices

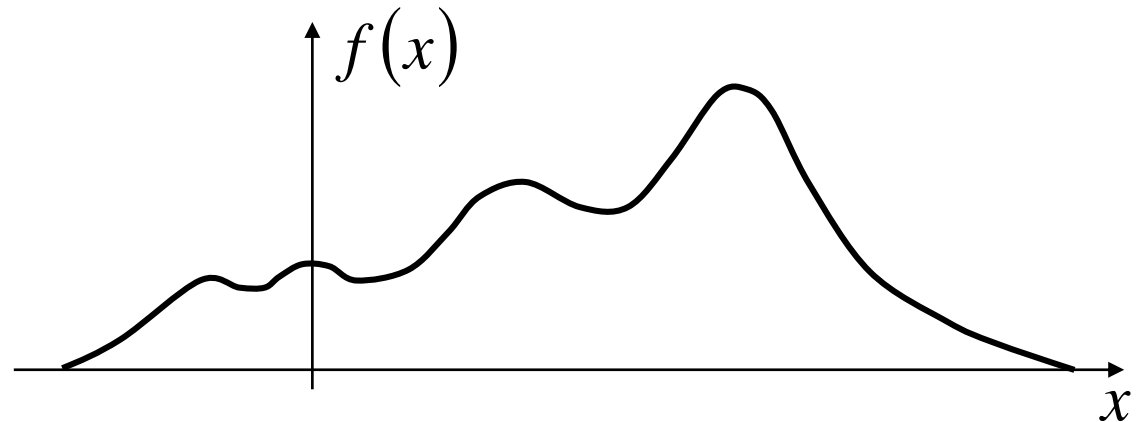
- Each point is a **pixel** with amplitude:
  - $f(x,y)$
- An image is a matrix with size  $N \times M$

$$I = \begin{bmatrix} (0,0) & (0,1) & \dots \\ (1,0) & (1,1) & \dots \\ \dots & \dots & \dots \end{bmatrix}$$



# Sampling Theorem

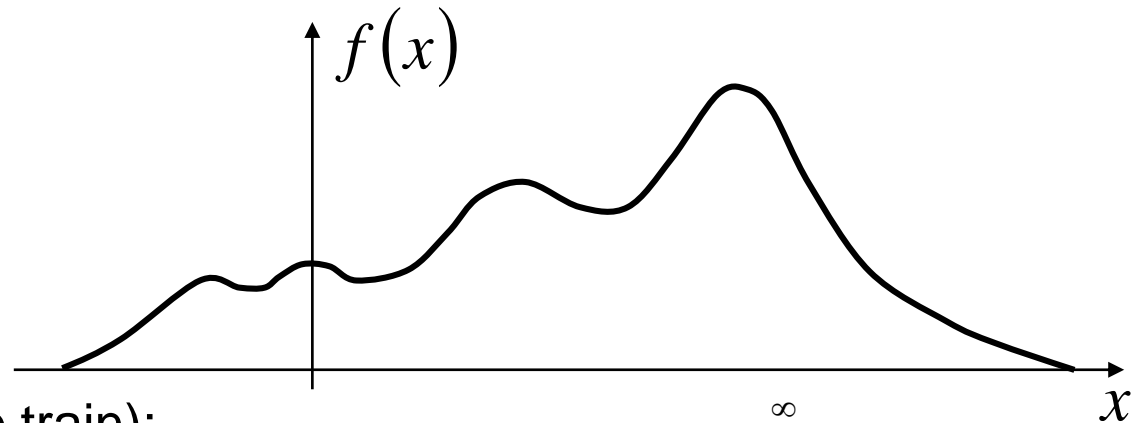
Continuous signal:



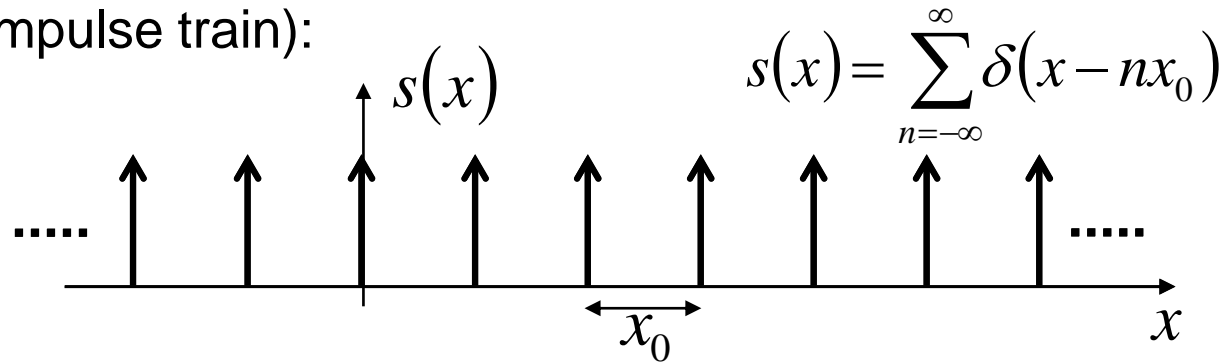
In the field of digital signal processing, the sampling theorem is a fundamental bridge between continuous-time signals (often called "analog signals") and discrete-time signals (often called "digital signals"). It establishes a sufficient condition for a sample rate that permits a discrete sequence of samples to capture all the information from a continuous-time signal of finite bandwidth.

# Sampling Theorem

Continuous signal:



Shah function (Impulse train):



Sampled function:

$$f_s(x) = f(x)s(x) = f(x) \sum_{n=-\infty}^{\infty} \delta(x - nx_0)$$

# Sampling Theorem

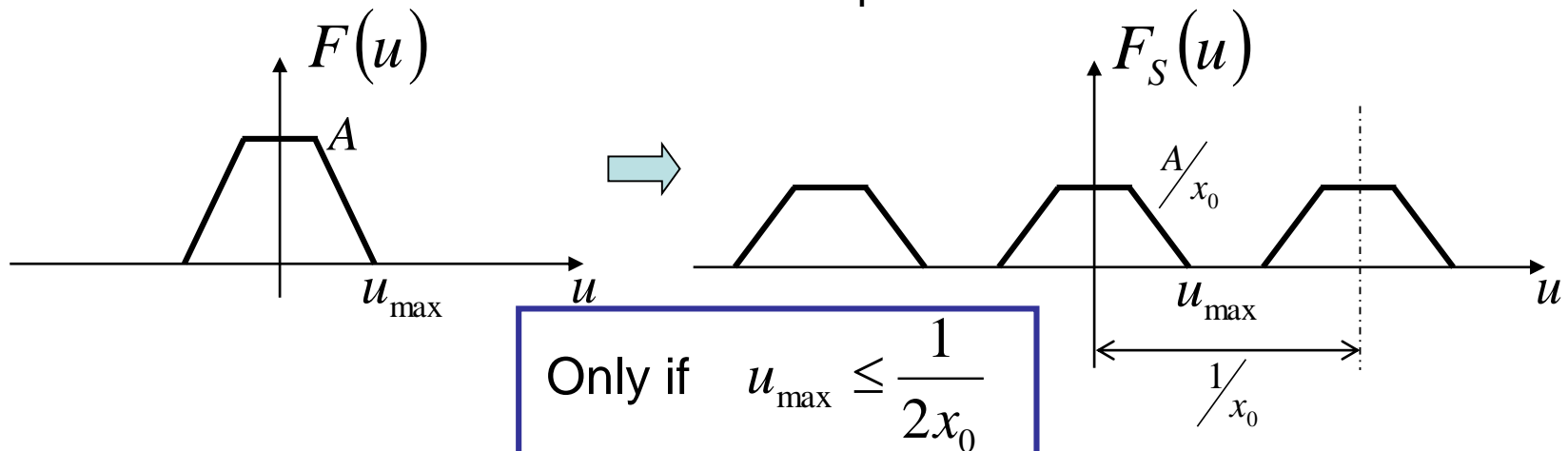
Sampled function:

$$f_s(x) = f(x)s(x) = f(x) \sum_{n=-\infty}^{\infty} \delta(x - nx_0)$$

Sampling frequency  $\frac{1}{x_0}$

$$F_S(u) = F(u) * S(u) = F(u) * \frac{1}{x_0} \sum_{n=-\infty}^{\infty} \delta\left(u - \frac{n}{x_0}\right)$$

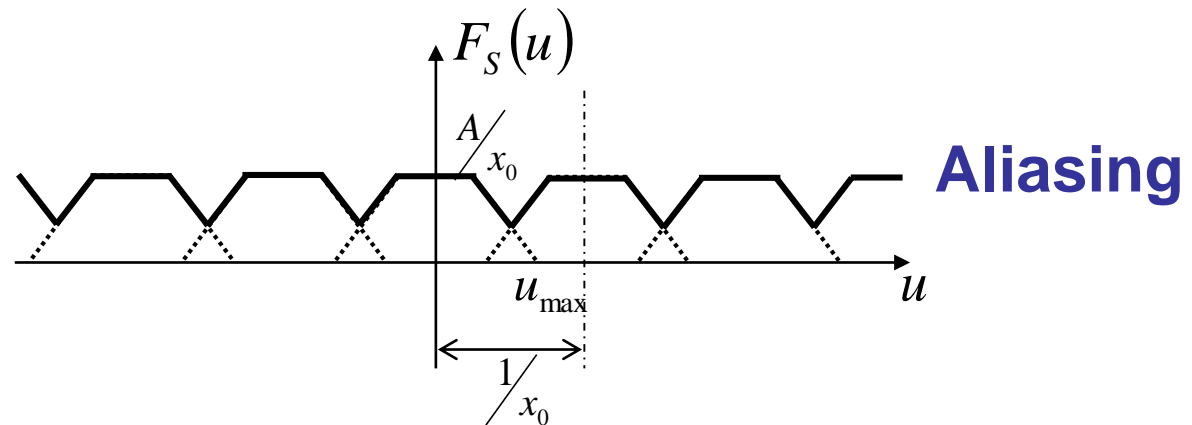
The Fourier transform decomposes a function of time (a signal) into the frequencies that make it up



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# Nyquist Theorem

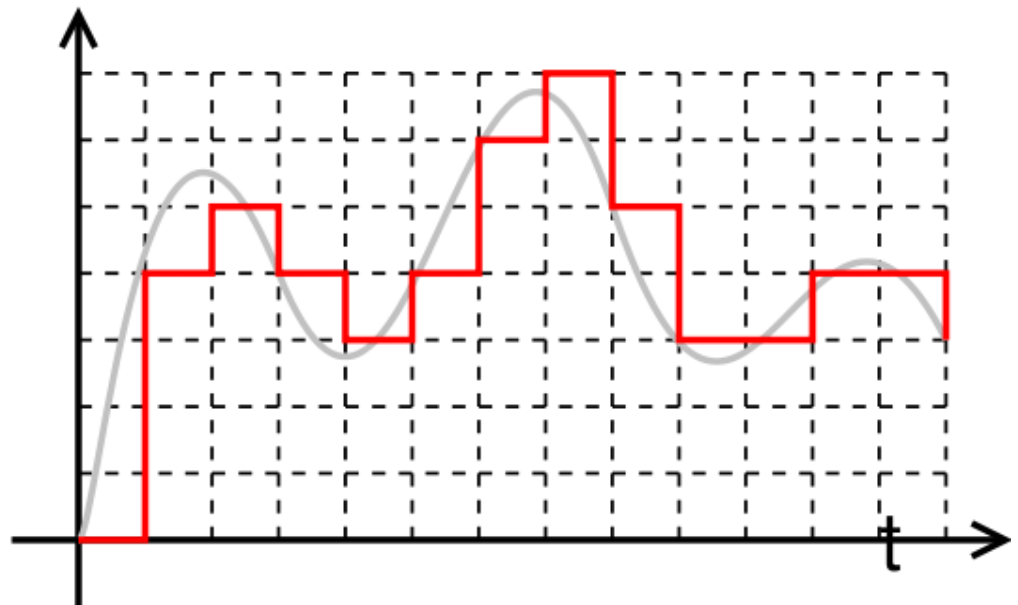
If  $u_{\max} > \frac{1}{2x_0}$



Sampling frequency must be greater than  $2u_{\max}$

# Quantization

- Analog:  $0 < f(x, y) < \infty$
- Digital: Infinite storage space per pixel!
- Quantization

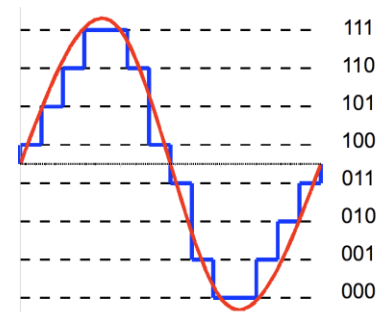
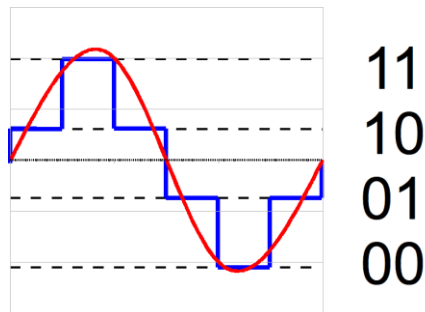
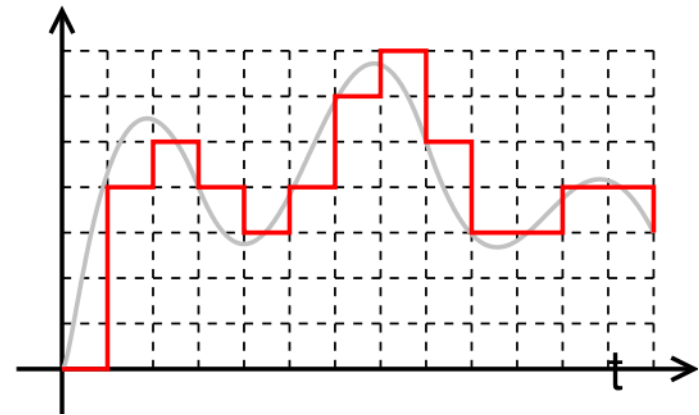




# Quantization Levels

- $G$  - number of levels
- $m$  – storage bits
- Round each value to its nearest level

$$G = 2^m$$



# Effect of quantization



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# Effect of quantization



# Image Size

- Storage space

- Spatial resolution:  $N \times M$
- Quantization:  $m$  bits per pixel
- Required bits  $b$ :

$$b = N \times M \times m$$

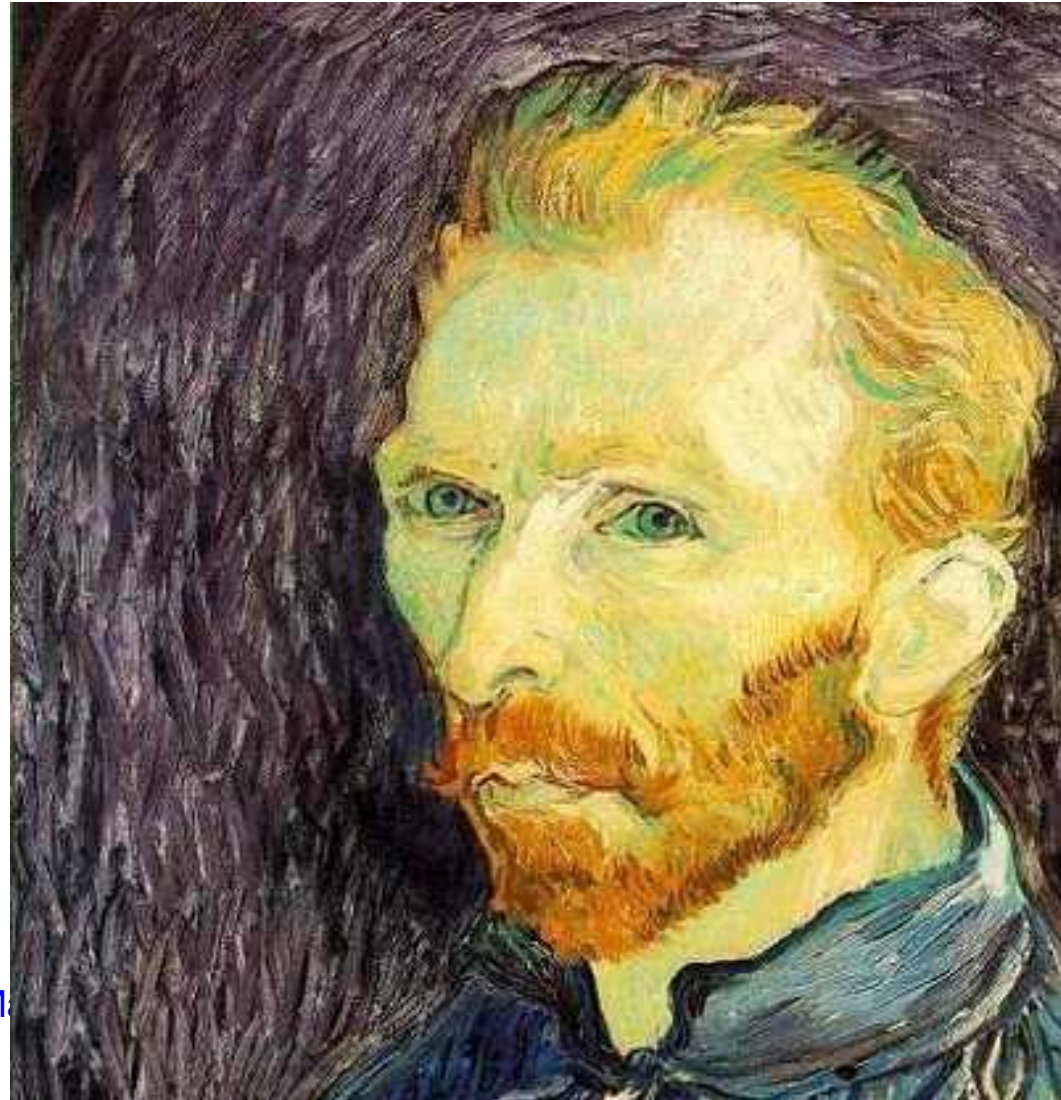
- Rule of thumb:

- More storage space means more image quality

# Image Scaling

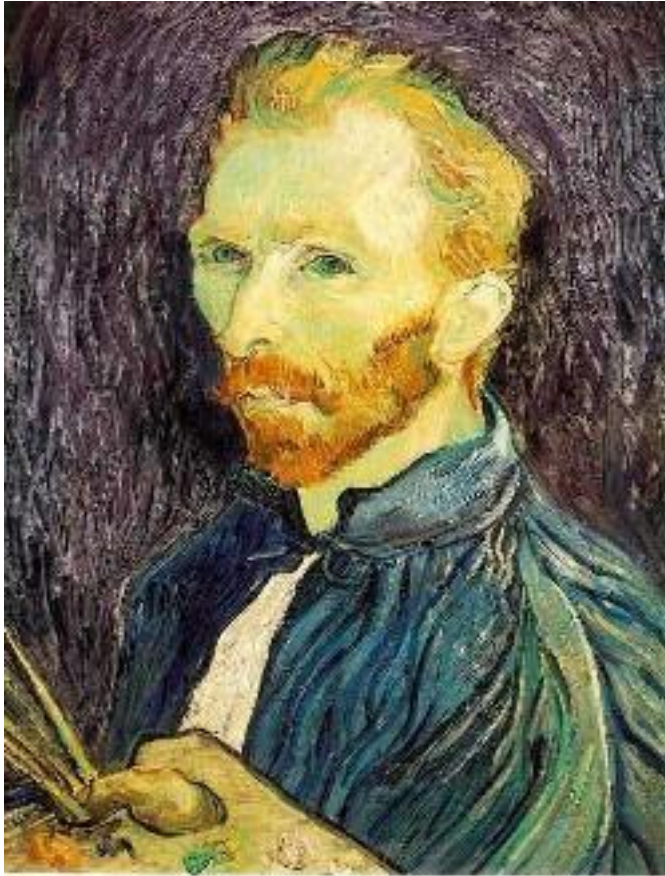
This image is too big to fit on the screen. How can we reduce it?

How to generate a half-sized version?



M

# Sub-sampling



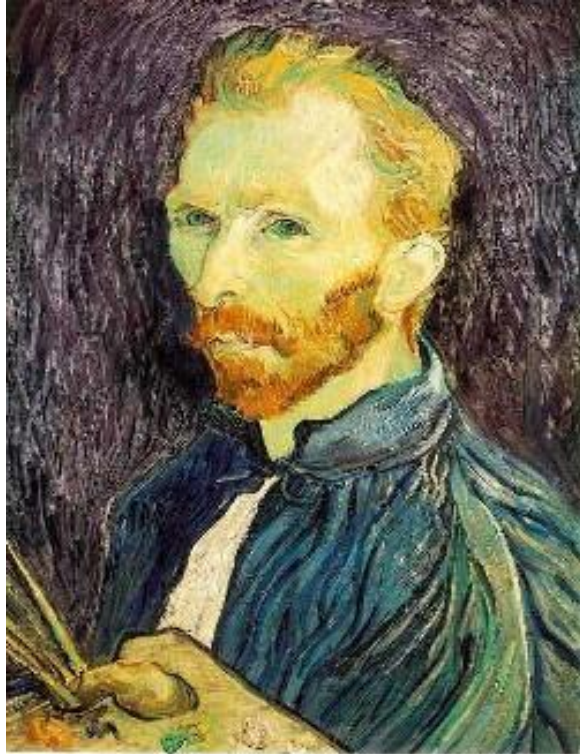
1/4



1/8

Throw away every other row and column to create a 1/2 size image  
- called *image sub-sampling*

# Sub-sampling



1/2



1/4 (2x zoom)



1/8 (4x zoom)

Can we do better?

<https://www.youtube.com/watch?v=6NclJXTlugc>

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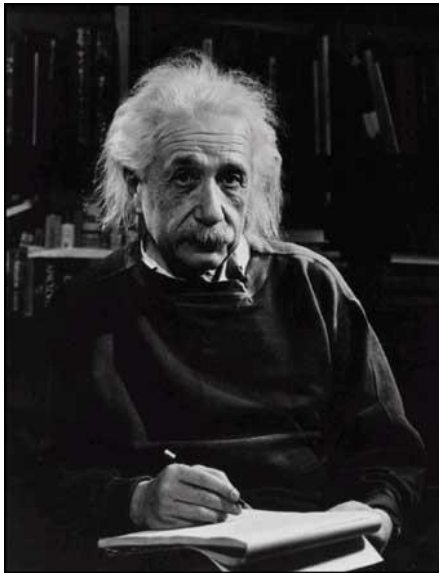
# Outline

- Image Formation
- **Digital Images**
  - Sampling
  - **Data Structures**
  - Histograms
- Colour and Noise



# Data Structures for Digital Images

- Are there other ways to represent digital images?



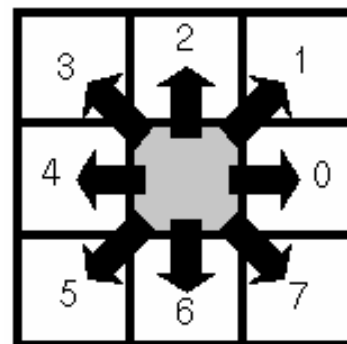
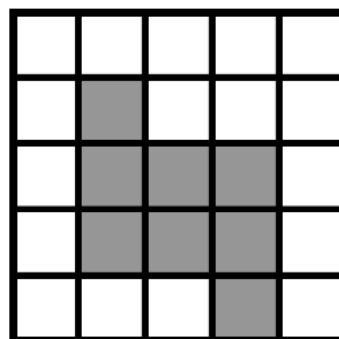
What we see

0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

What a computer sees

# Chain codes

- Chains represent the borders of objects.
- Coding with *chain codes*.
  - Relative.
  - Assume an initial starting point for each object.
- Needs segmentation!

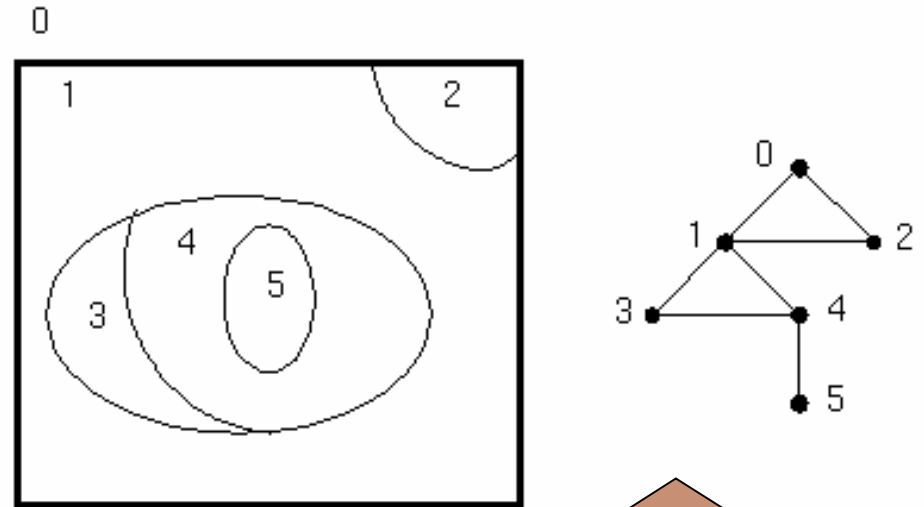


Freeman Chain Code

Using a Freeman Chain Code and considering the top-left pixel as the starting point:  
70663422

# Topological Data Structures

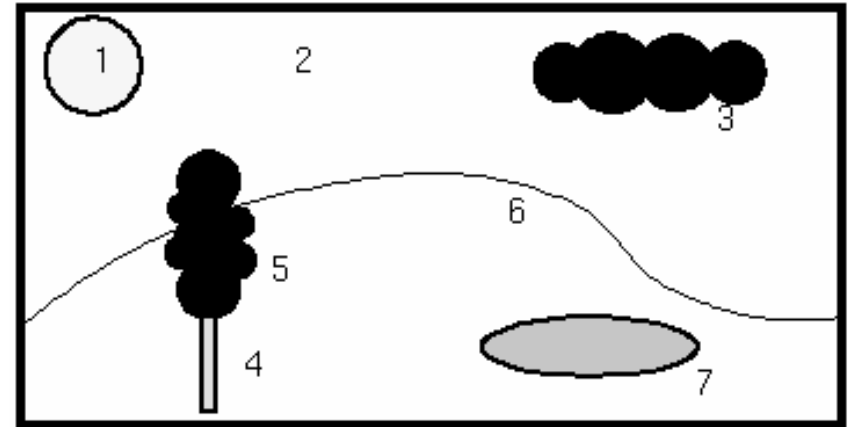
- *Region Adjacency Graph*
  - **Nodes** - Regions
  - **Arcs** – Relationships
- Describes the elements of an image and their spatial relationships.
- Needs segmentation!



*Region Adjacency Graph*

# Relational Structures

- Stores **relations** between **objects**.
- Important **semantic information** of an image.
- Needs **segmentation** and an image description (**features**)!



No.	Object name	Colour	Min. row	Min. col.	Inside
1	sun	white	5	40	2
2	sky	blue	0	0	-
3	cloud	grey	20	180	2
4	tree trunk	brown	95	75	6
5	tree crown	green	53	63	-
6	hill	light green	97	0	-
7	pond	blue	100	160	6

*Relational Table*

# Outline

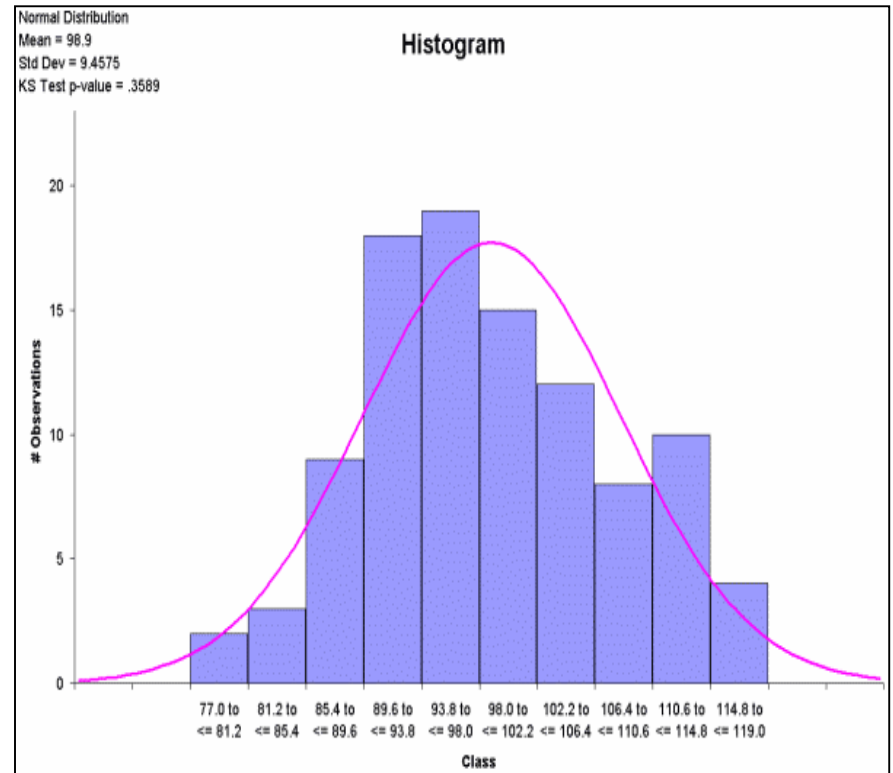
- Image Formation
- **Digital Images**
  - Sampling
  - Data Structures
  - Histograms
- Colour and Noise

# Histograms

- “In statistics, a histogram is a graphical display of tabulated frequencies.”

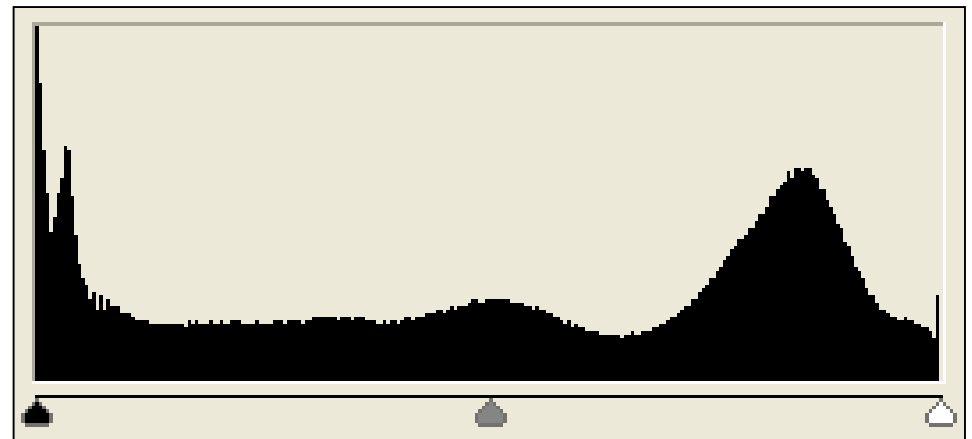
[Wikipedia]

- Typically represented as a bar chart:



# Image Histograms

- Colour or Intensity distribution.
- Typically:
  - Reduced number of *bins*.
  - Normalization.
- Compressed representation of an image.
  - No spatial information whatsoever!



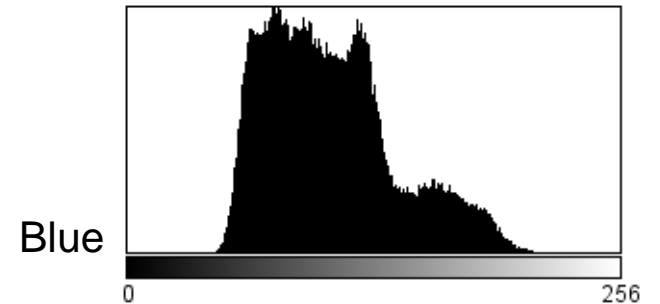
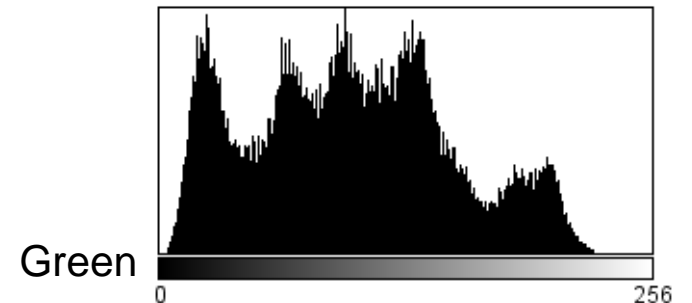
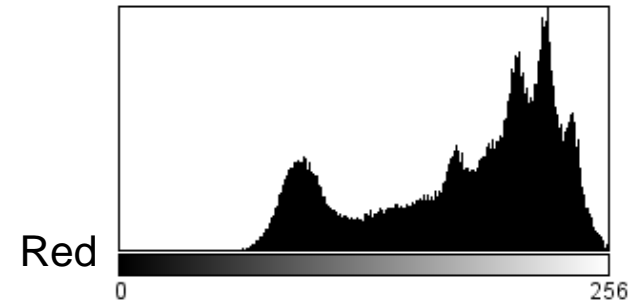
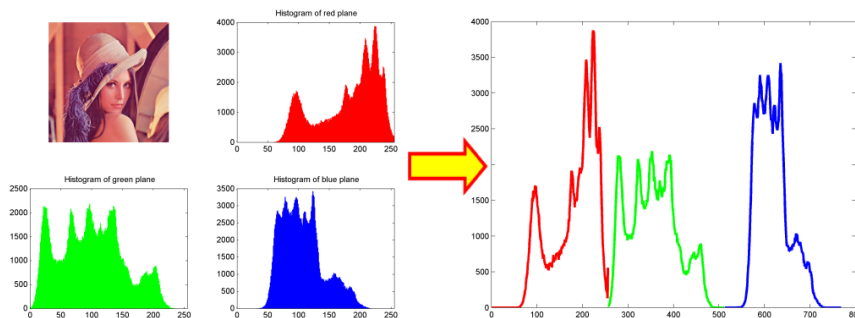
# Colour Histogram

- As many histograms as axis of the colour space.

Ex: RGB Colour space

- Red Histogram
- Green Histogram
- Blue Histogram

- Combined histogram.

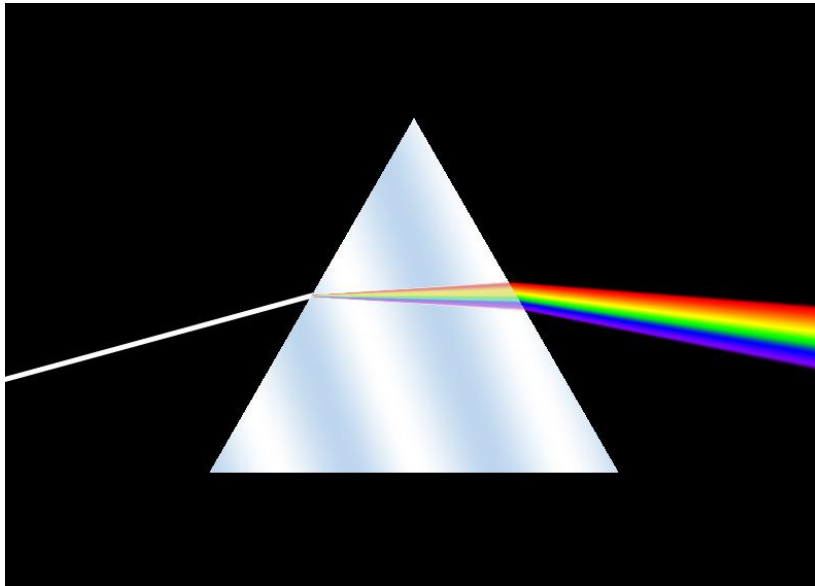




# Outline

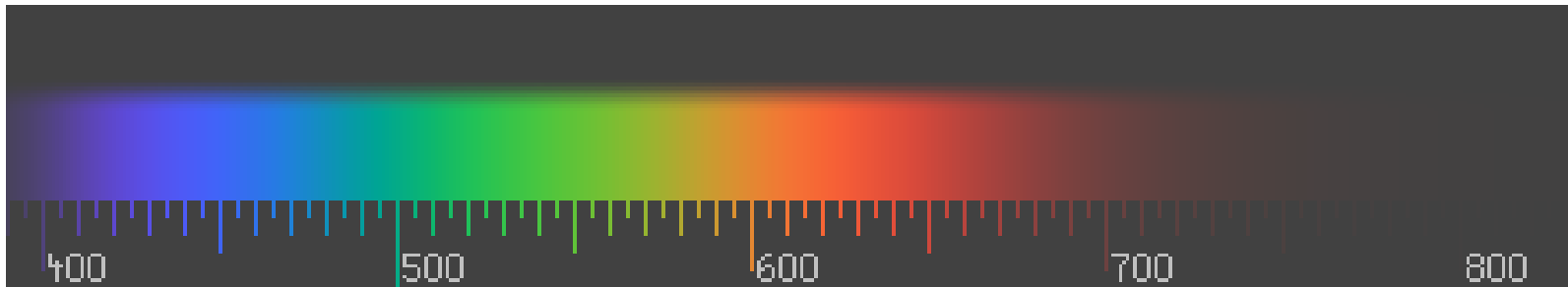
- Image Formation
- Digital Images
- **Colour and Noise**
  - Colour spaces
  - Colour processing
  - Noise

# What is colour?

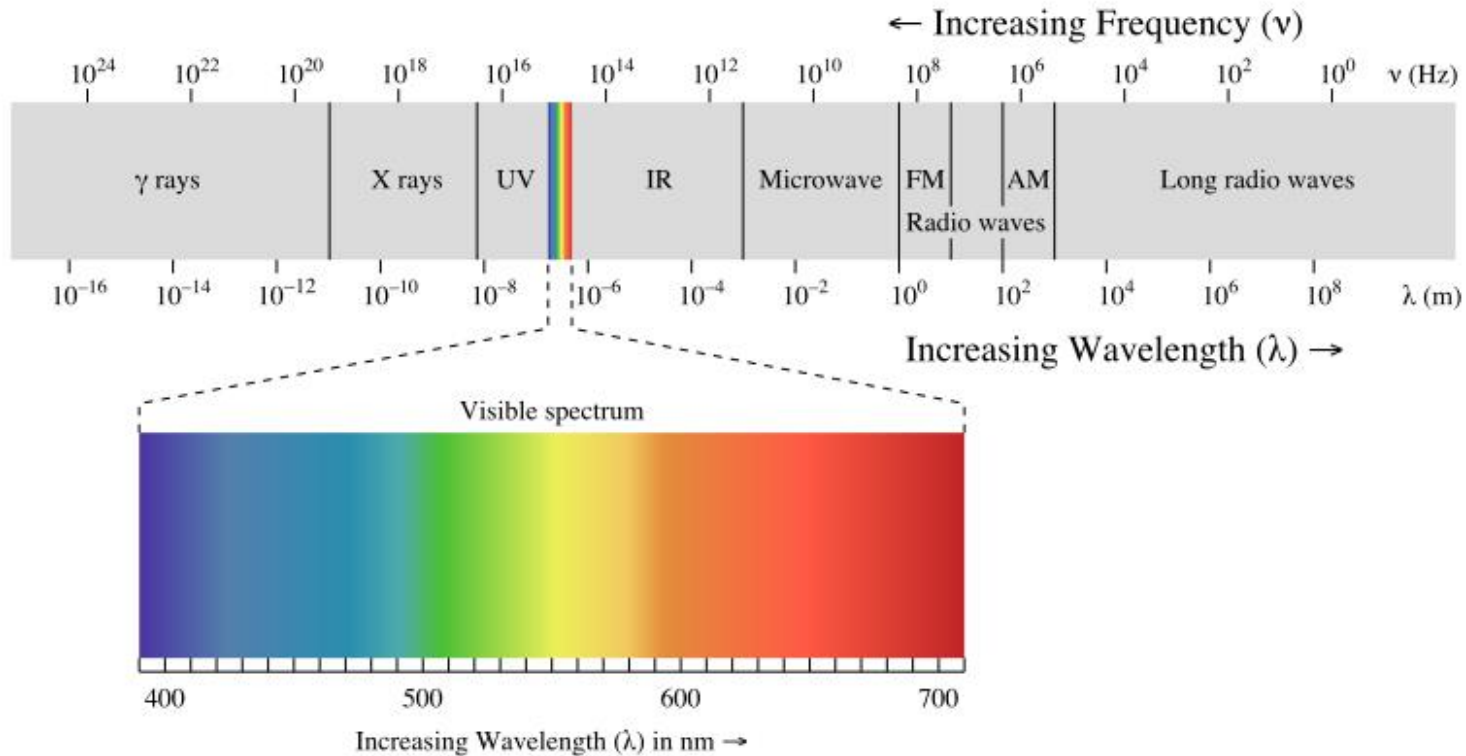


Optical Prism  
dispersing light

Visible colour  
spectrum



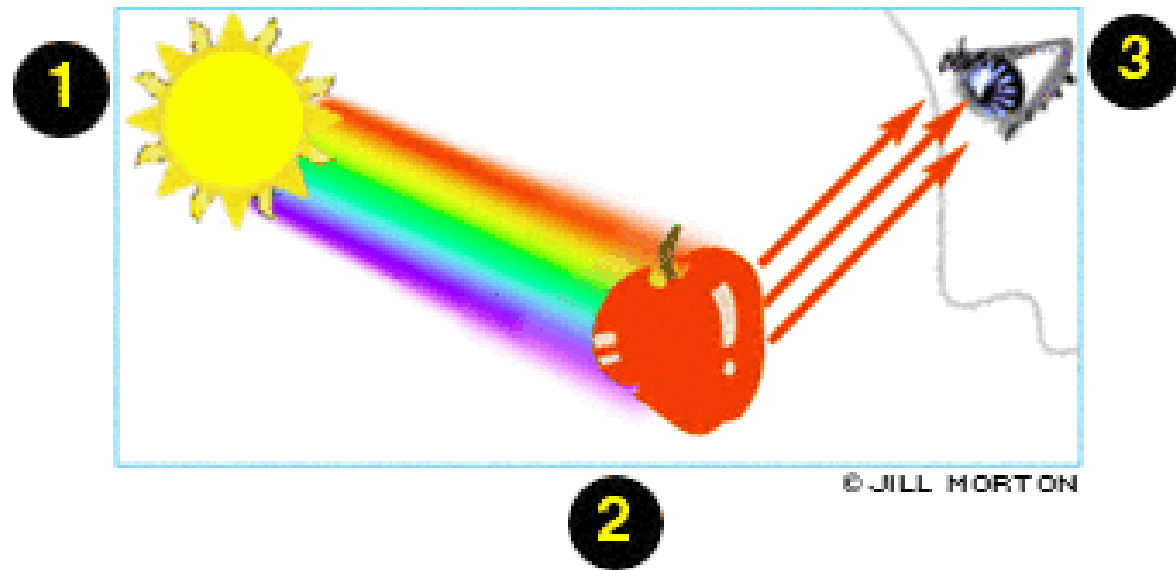
# Visible Spectrum



<http://science.howstuffworks.com/light.htm>

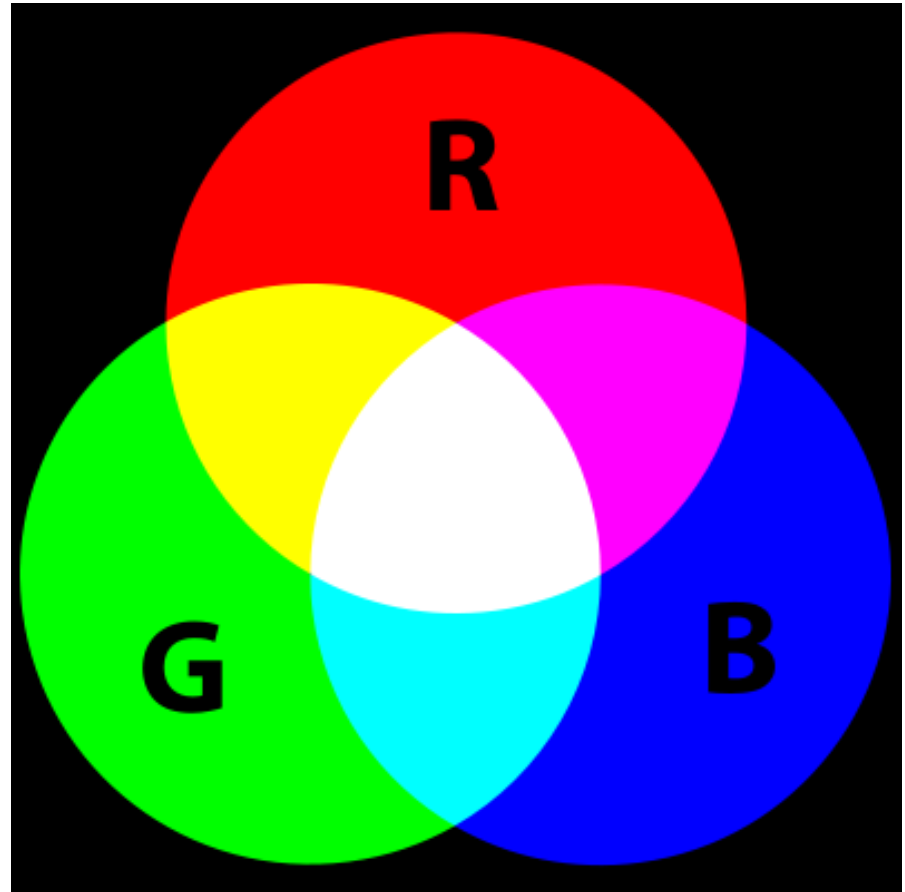
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# How do we see colour?



# Primary Colours

- Not a fundamental property of light.
- Based on the physiological response of the human eye.
- Form an additive colour system.



# Colour Space

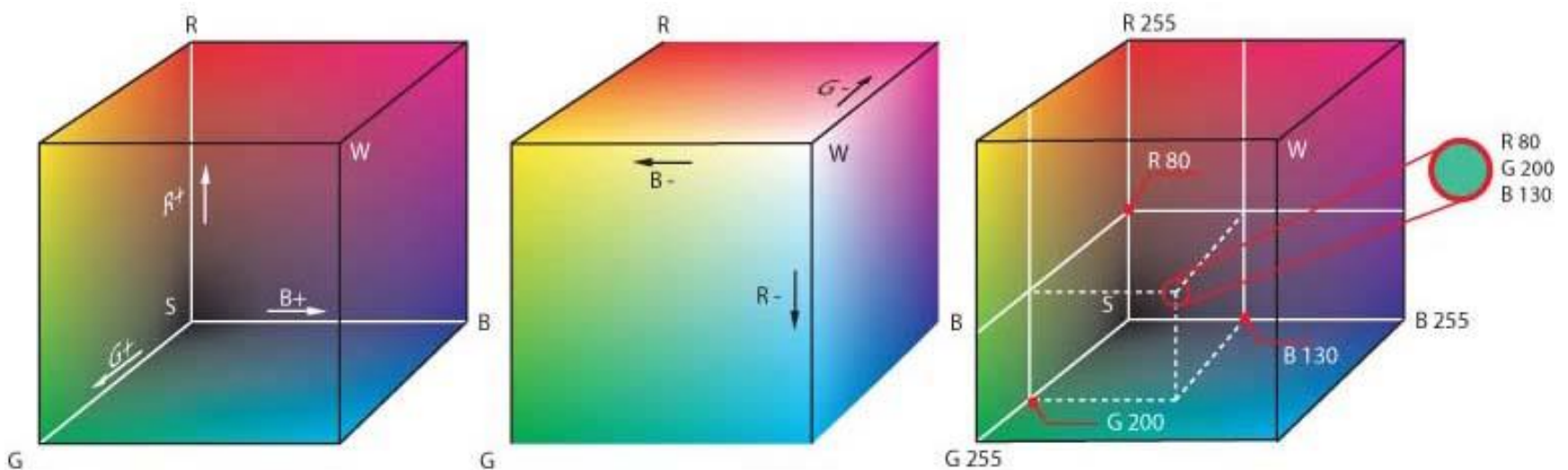
- “The purpose of a color model is to facilitate the specification of colours in some standard, generally accepted way”

Gonzalez & Woods

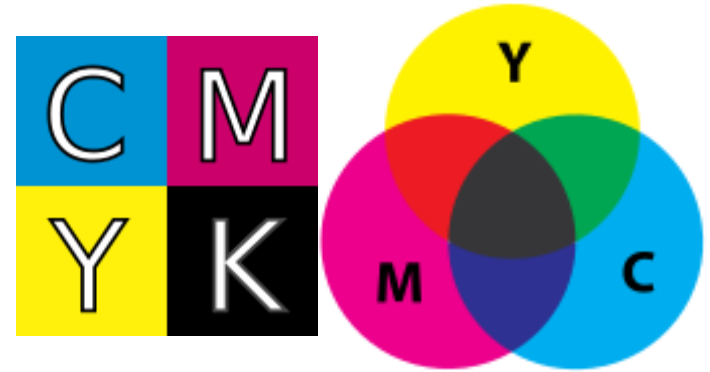
- Colour space
  - Coordinate system
  - Subspace: One colour -> One point

# RGB

- Red Green Blue
- Defines a colour cube.
- Additive components.
- Great for image capture.
- Great for image projection.
- Poor colour description.



# CMYK

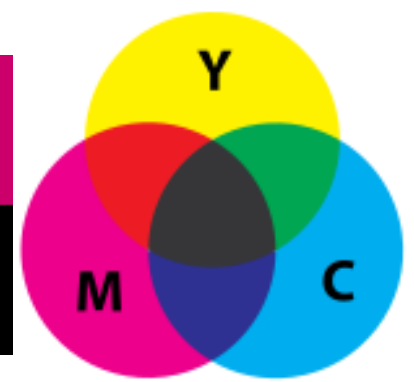
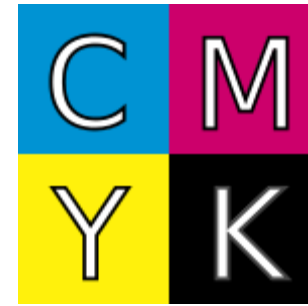


- Cyan Magenta Yellow Key.
- Variation of RGB.
- Technological reasons: great for printers.
- Subtractive model





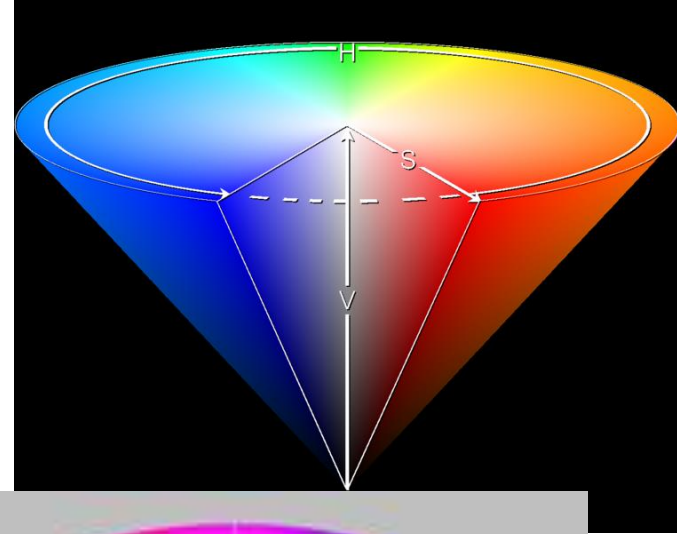
# CMYK



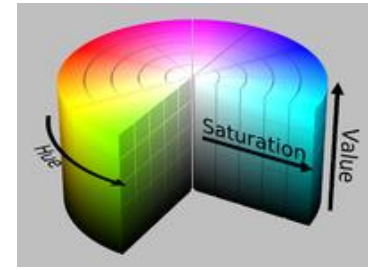
- In additive color models such as RGB, white is the "additive" combination of all primary colored lights, while black is the absence of light.
- In the CMYK model, it is the opposite: white is the natural color of the paper or other background, while black results from a full combination of colored inks.
- To save cost on ink, and to produce deeper black tones, unsaturated and dark colors are produced by using black ink instead of the combination of cyan, magenta and yellow.

# HSI (HSV)

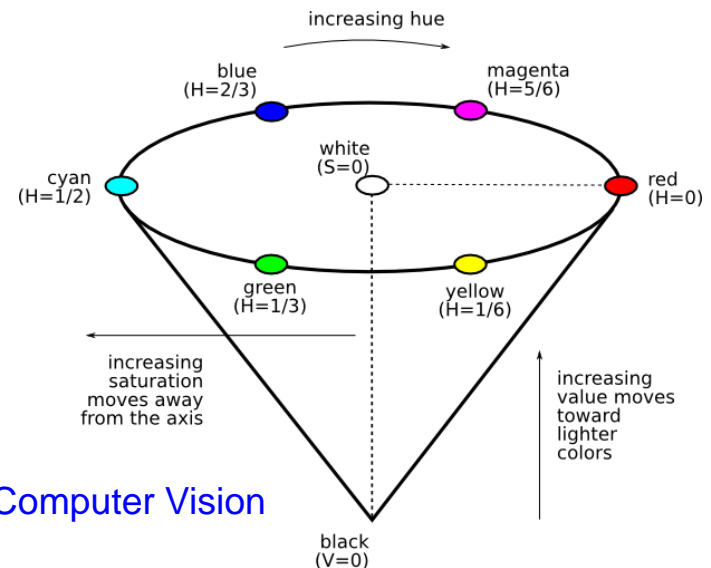
- Hue Saturation Intensity (Value)
- Defines a colour cone
- Great for colour description.
- cylindrical-coordinate representation of RGB
- Attempt to be more intuitive and perceptually relevant than cube



# HSI (HSV)

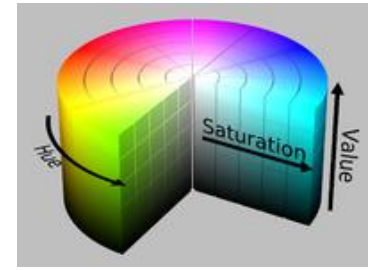


- The *hue* (H) of a color refers to which pure color it resembles. All tints, tones and shades of red have the same hue.
- Hues are described by a number that specifies the position of the corresponding pure color on the color wheel, as a fraction between 0 and 1. Value 0 refers to red; 1/6 is yellow; 1/3 is green; and so forth around the color wheel.

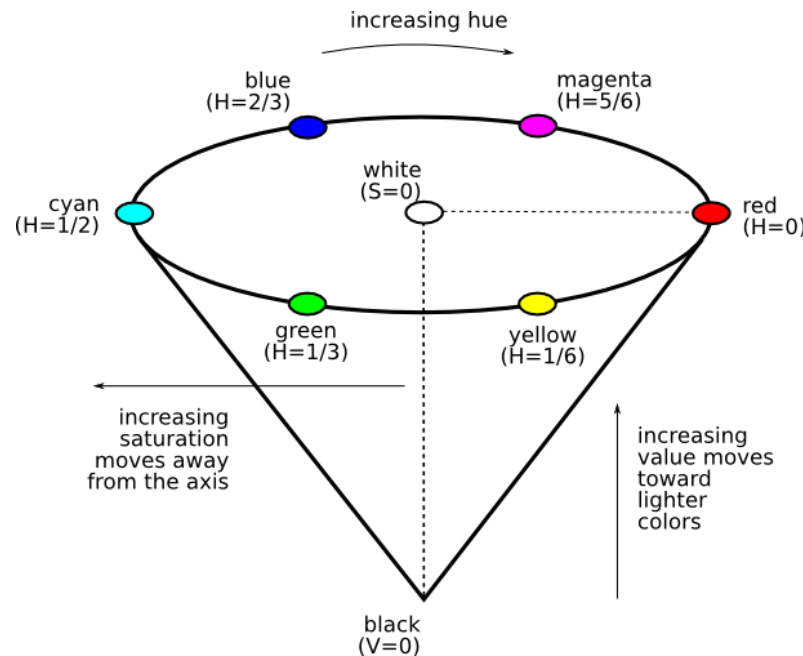


Mapi 17/18 - Computer Vision

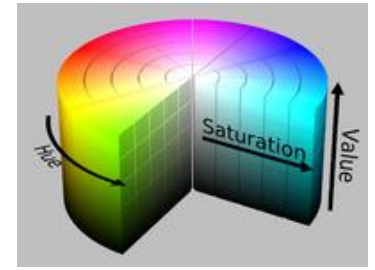
# HSI (HSV)



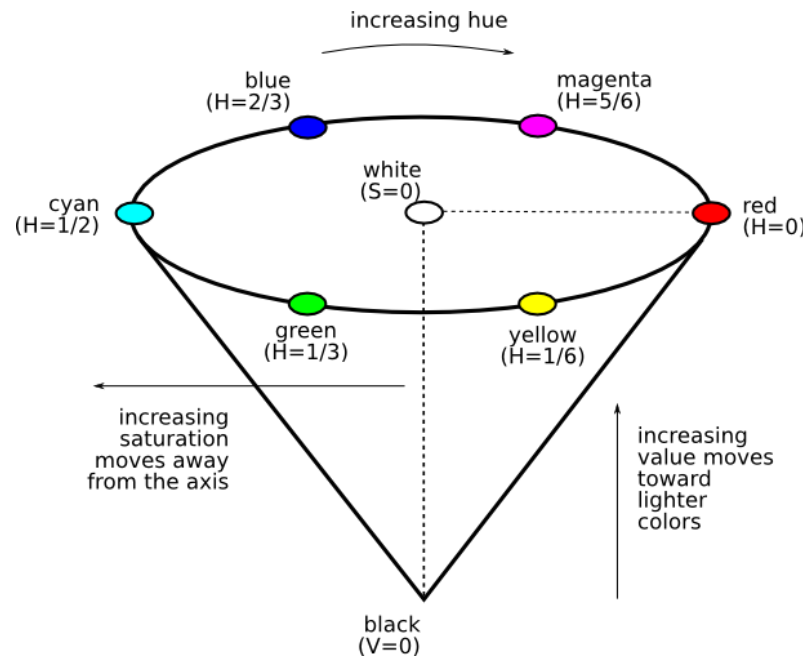
- The *saturation* ( $S$ ) of a color describes how white the color is. A pure red is fully saturated, with a saturation of 1; tints of red have saturations less than 1; and white has a saturation of 0.



# HSI (HSV)

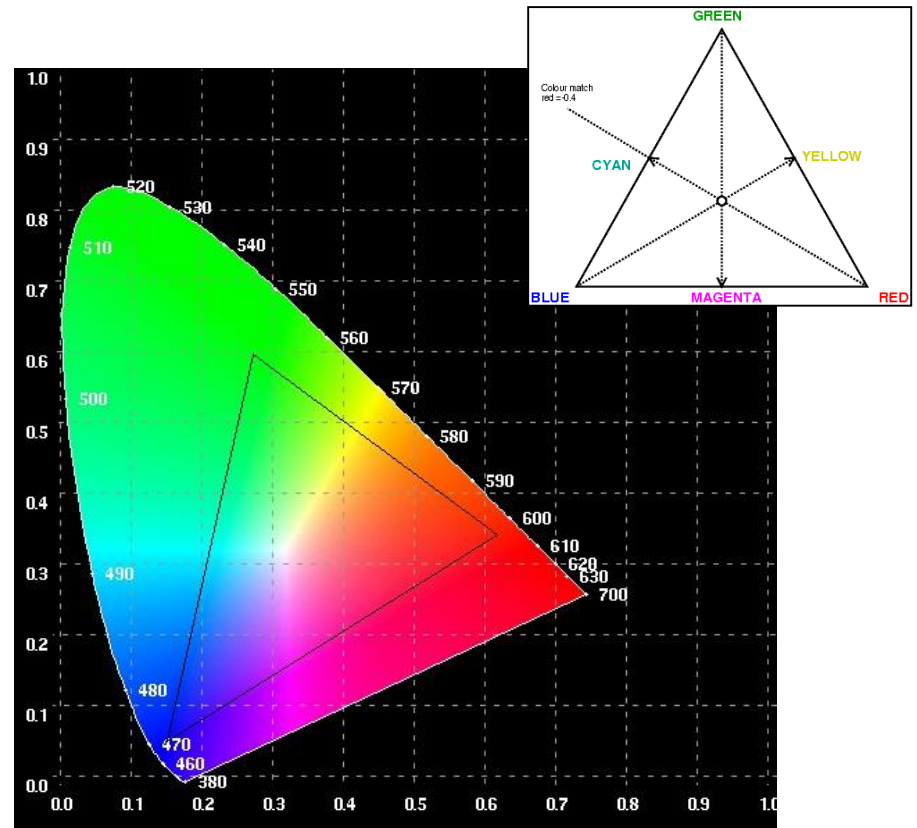


- The *value* ( $V$ ) of a color, also called its *lightness*, describes how dark the color is. A value of 0 is black, with increasing lightness moving away from black.



# Chromaticity Diagram

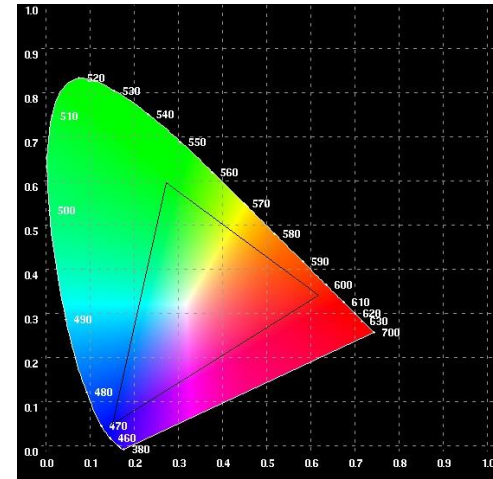
- **Axis:**
  - Hue
  - Saturation
- **Outer line represents our visible spectrum.**



[http://www.cs.rit.edu/~ncs/color/a\\_chroma.html](http://www.cs.rit.edu/~ncs/color/a_chroma.html)

# Chromaticity Diagram

- The **CIE 1931 XYZ color spaces** were the first defined quantitative links between physical pure colors (i.e. wavelengths) in the electromagnetic visible spectrum, and physiological perceived colors in human color vision. The mathematical relationships that define these color spaces are essential tools for color management, important when dealing with color inks, illuminated displays, and recording devices such as digital cameras.

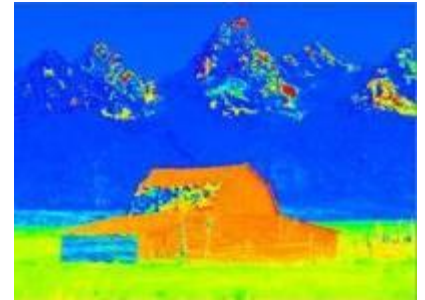


[http://www.cs.rit.edu/~ncs/color/a\\_chroma.html](http://www.cs.rit.edu/~ncs/color/a_chroma.html)

# RGB to HSI

Hue:

$$H = \begin{cases} \theta & \Leftarrow B \leq G \\ 360 - \theta & \Leftarrow B > G \end{cases}$$



$$\theta = \cos^{-1} \left\{ \frac{\frac{1}{2} [(R - G) + (R - B)]}{\left[ (R - G)^2 + (R - B)(G - B) \right]^{1/2}} \right\}$$



Saturation

$$S = 1 - \frac{3}{(R + G + B)} [\min(R, G, B)]$$



Intensity

$$I = \frac{1}{3} (R + G + B)$$



# HSI to RGB

- Depends on the 'sector' of H

$$120 \leq H < 240$$

$$0 \leq H < 120$$

$$B = I(1 - S)$$

$$R = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right]$$

$$G = 3I - (R + B)$$

$$240 \leq H < 360$$

$$H = H - 120^\circ$$

$$R = I(1 - S)$$

$$G = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right]$$

$$B = 3I - (R + G)$$

$$H = H - 240^\circ$$

$$G = I(1 - S)$$

$$B = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right]$$

$$R = 3I - (G + B)$$

# Outline

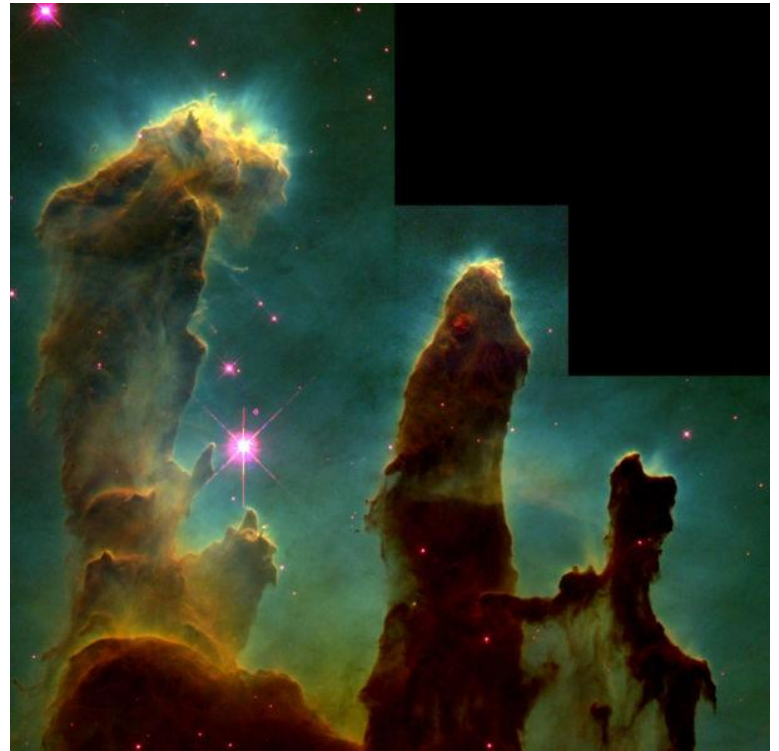
- Image Formation
- Digital Images
- **Colour and Noise**
  - Colour spaces
  - **Colour processing**
  - Noise



A WFPC2 image of a small region of the [Tarantula Nebula](#) in the [Large Magellanic Cloud](#) [NASA/ESA]

# Pseudocolour

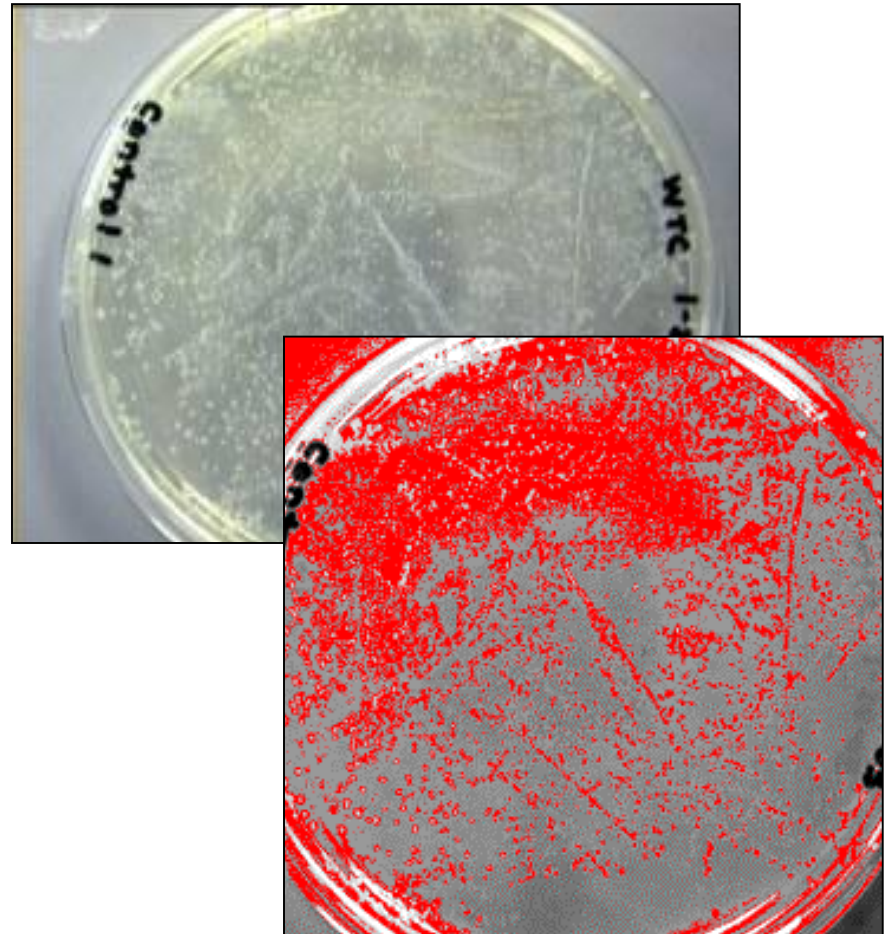
- Also called *False Colour*.
- Opposed to *True Colour* images.
- The colours of a pseudocolour image do not attempt to approximate the real colours of the subject.

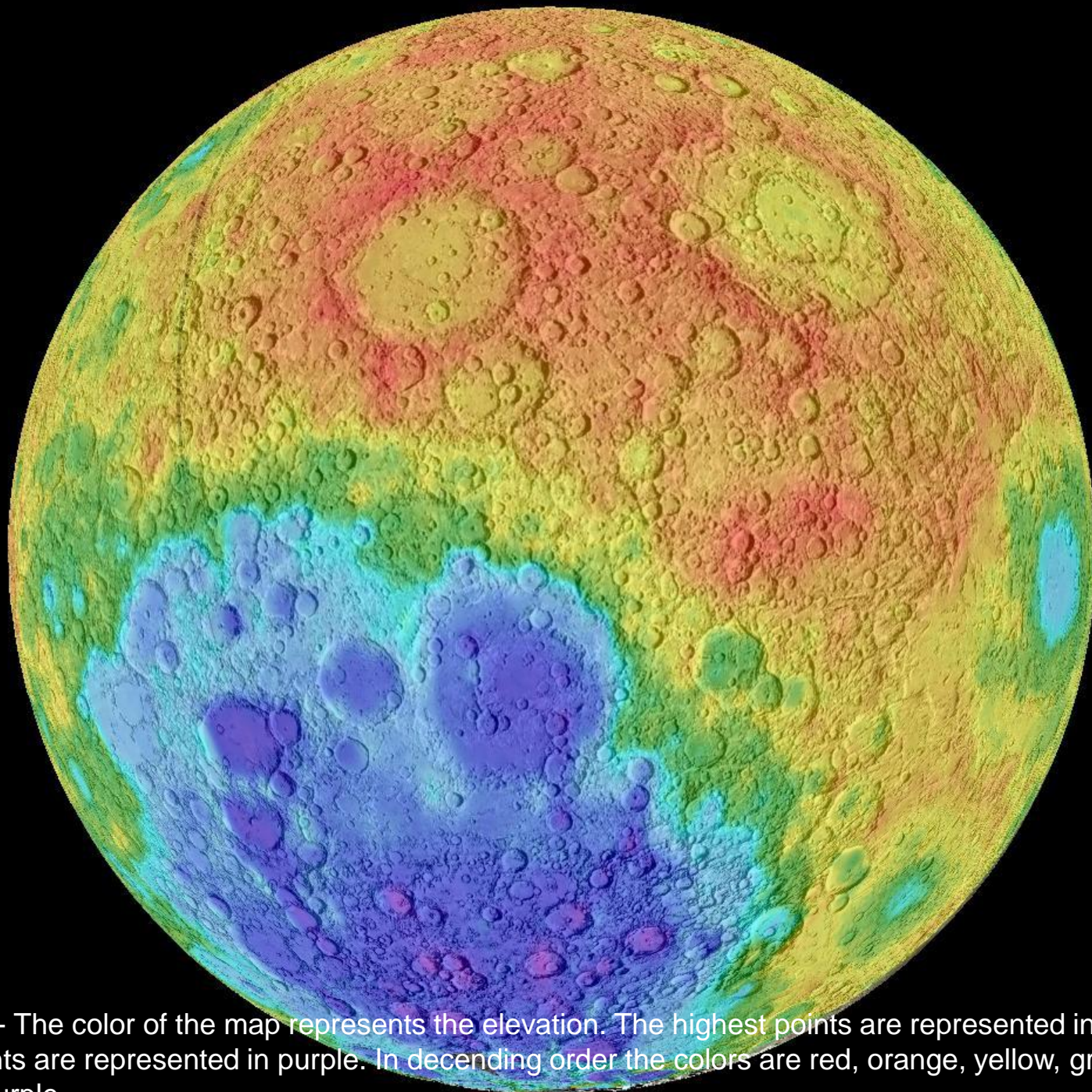


One of Hubble's most famous images: "pillars of creation" where stars are forming in the Eagle Nebula. [NASA/ESA]

# Intensity Slicing

- Quantize pixel intensity to a specific number of values (*slices*).
- Map one colour to each *slice*.
- Loss of information.
- Enhanced human visibility.



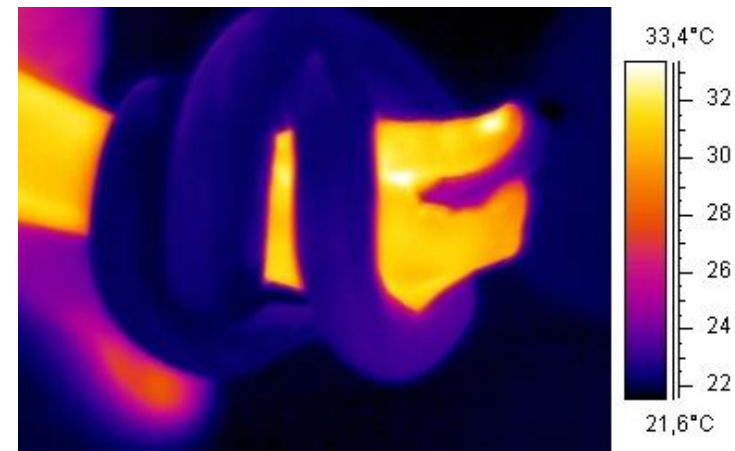
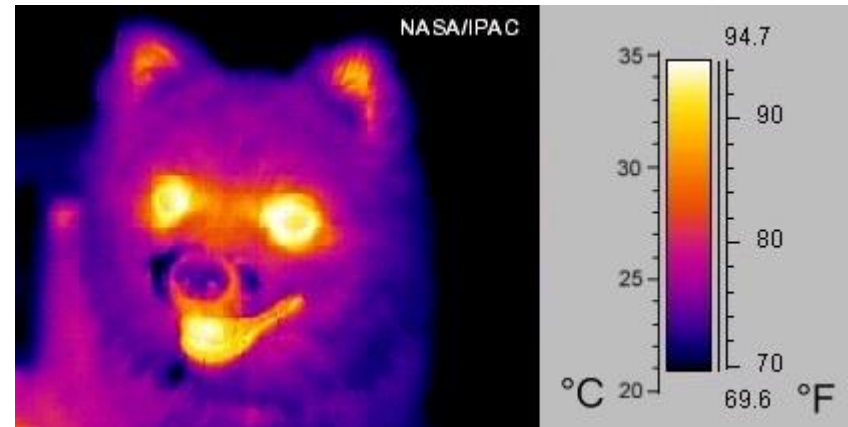


The [Moon](#) - The color of the map represents the elevation. The highest points are represented in red. The lowest points are represented in purple. In descending order the colors are red, orange, yellow, green, cyan, blue and purple.

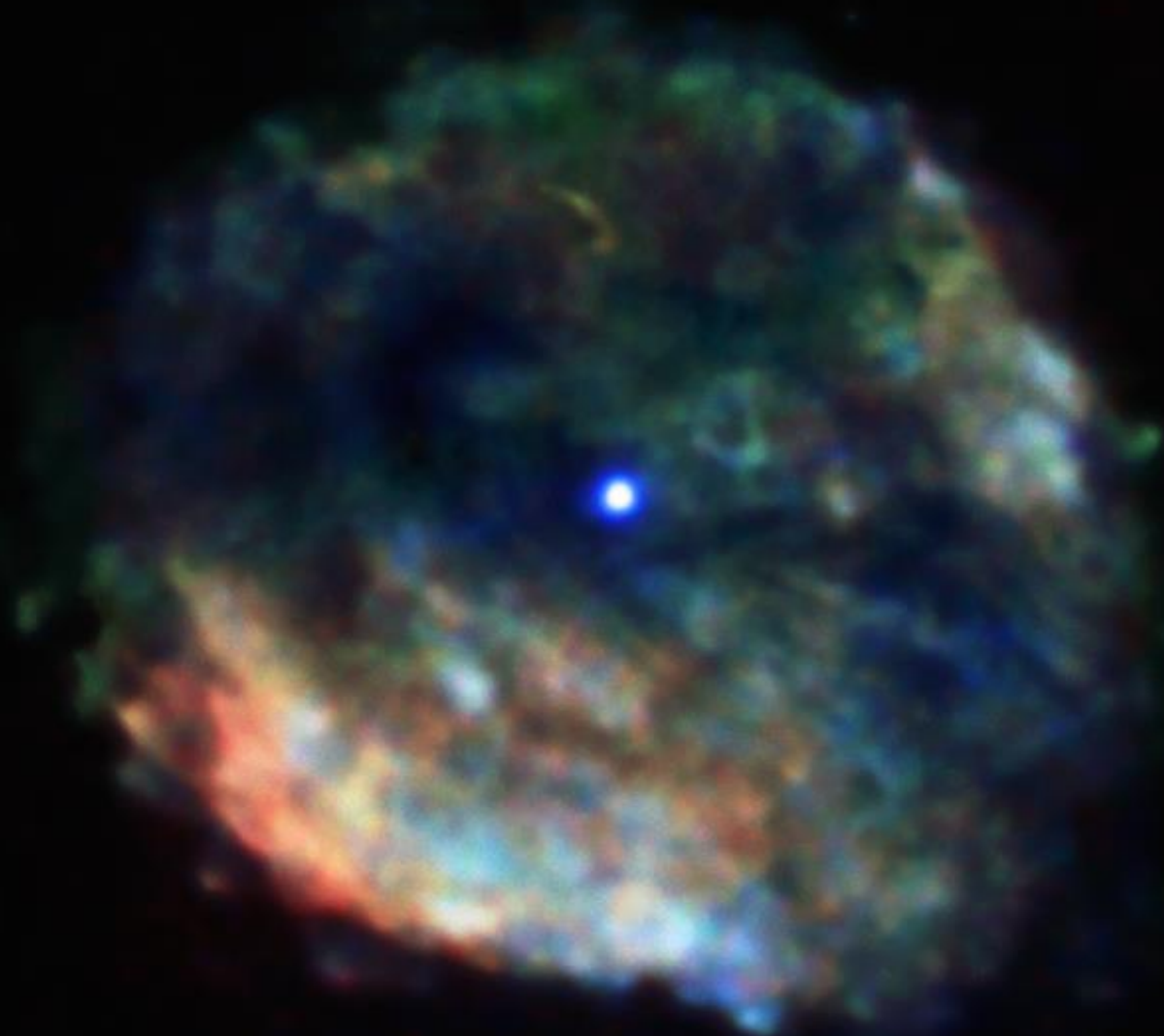
# Intensity to Colour Transformation

- Each colour component is calculated using a transformation function.
- Viewed as an Intensity to Colour map.
- Does not need to use RGB space!

$$f(x, y) \Rightarrow \begin{cases} f_R(x, y) = T_R[f(x, y)] \\ f_G(x, y) = T_G[f(x, y)] \\ f_B(x, y) = T_B[f(x, y)] \end{cases}$$



A supernova  
remnant created  
from the death of  
a massive star  
about 2,000 years  
ago.



[http://chandra.harvard.edu/photo/false\\_color.html](http://chandra.harvard.edu/photo/false_color.html)

<http://landsat.gsfc.nasa.gov/education/compositor/>

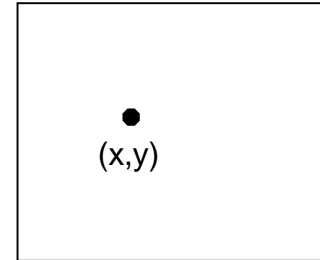


# Colour Image Processing

- **Grey-scale image**

- One value per position.

$$f(x,y) = I$$

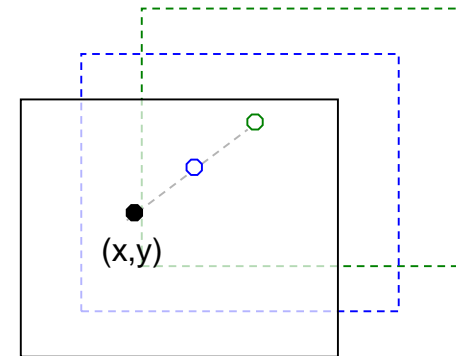


Grey-scale image

- **Colour image**

- One vector per position.

$$f(x,y) = [R \ G \ B]^T$$



RGB Colour image

# Colour Transformations

- Consider single-point operations:

$T_i$ : Transformation function for colour component  $i$

$s_i, r_i$ : Components of  $g$  and  $f$

$$g(x, y) = T[f(x, y)]$$

$$s_i = T_i(r_1, r_2, \dots, r_n)$$

$$i = 1, 2, \dots, n$$

- Simple example:

- Increase Brightness of an RGB image

$$s_R = r_R + 20$$

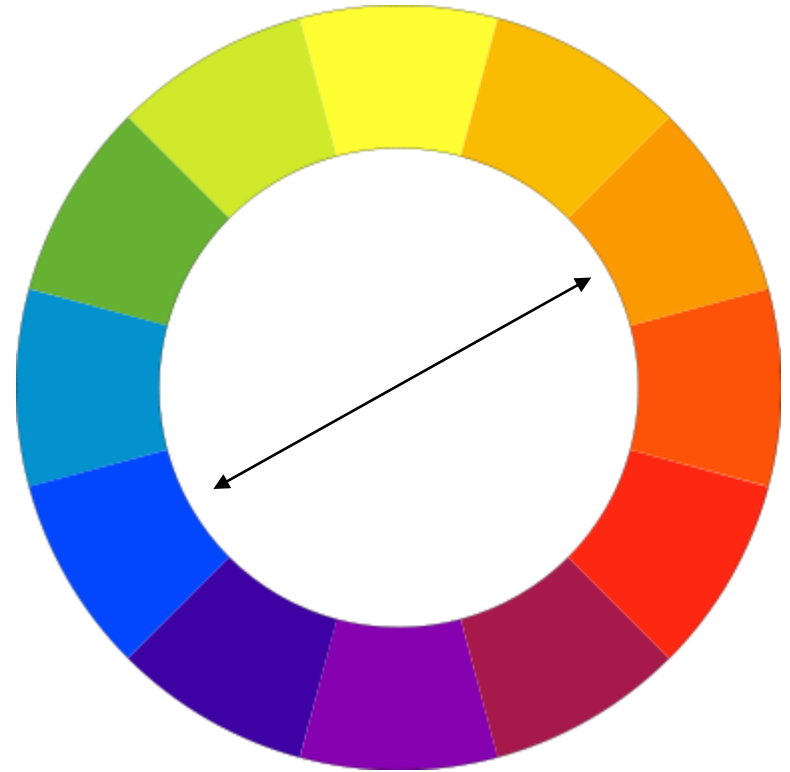
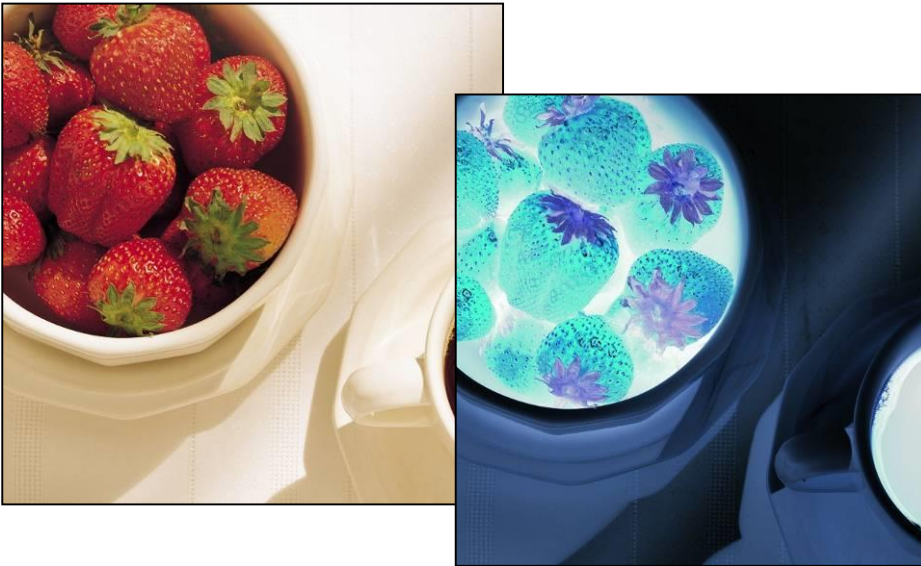
$$s_G = r_G + 20$$

$$s_B = r_B + 20$$

What about an image negative?

# Colour Complements

- Colour equivalent of an image negative.



Complementary Colours

# Colour Slicing

- Define a hyper-volume of interest inside my colour space.
- Keep colours if inside the hyper-volume.
- Change the others to a neutral colour.

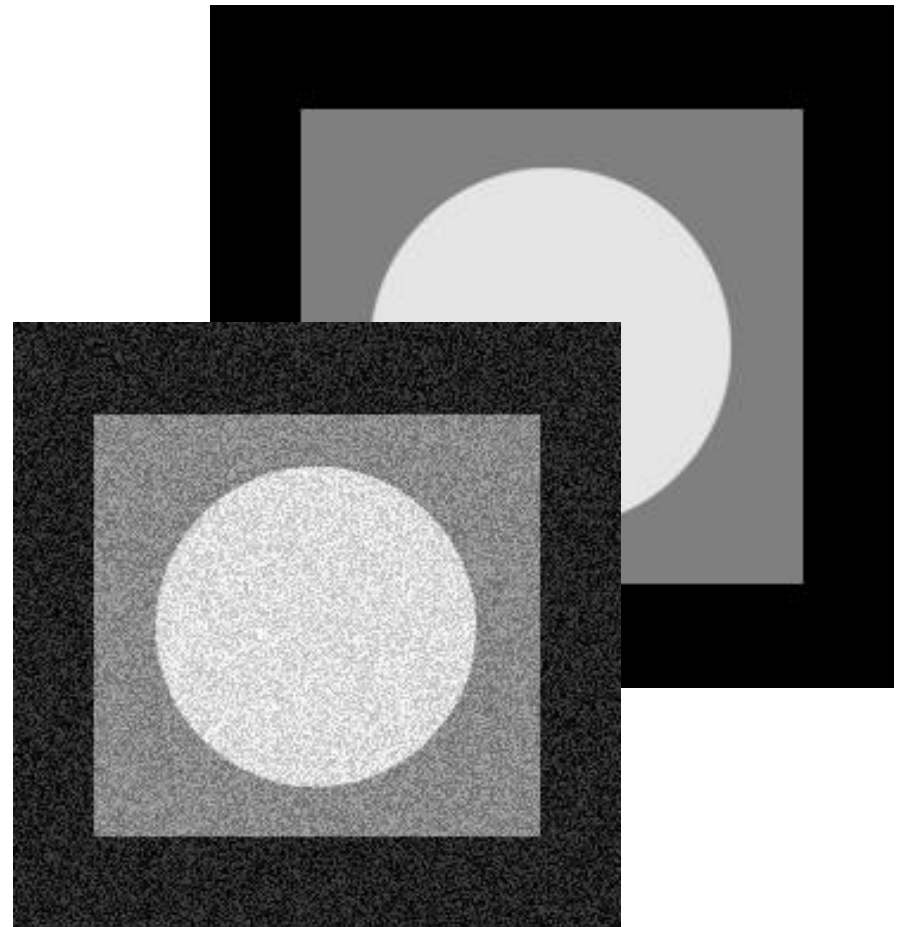


# Outline

- Image Formation
- Digital Images
- **Colour and Noise**
  - Colour spaces
  - Colour processing
  - **Noise**

# Bring the Noise

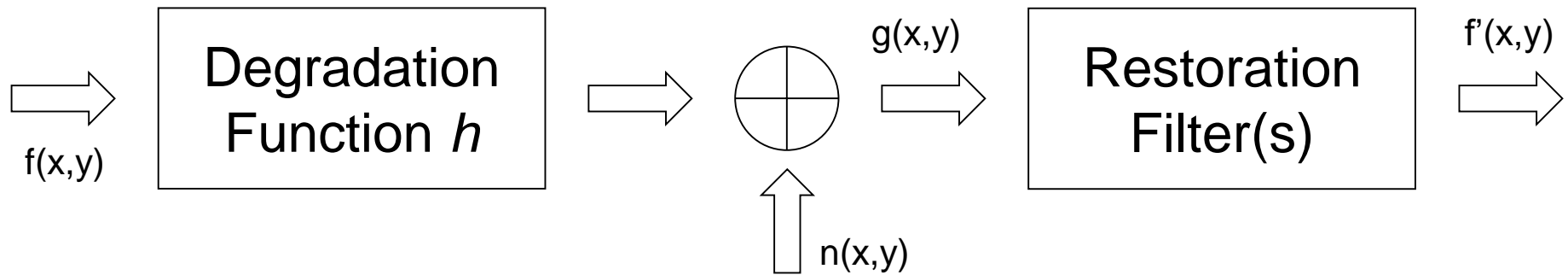
- Noise is a distortion of the measured signal.
- Every physical system has noise.
- Images:
  - The importance of noise is affected by our human visual perception
  - Ex: Digital TV ‘block effect’ due to noise.



# Where does it come from?

- **‘Universal’ noise sources:**
  - Thermal, sampling, quantization, measurement.
- **Specific for digital images:**
  - The number of photons hitting each image sensor is governed by quantum physics:  
*Photon Noise.*
  - Noise generated by electronic components of image sensors:
    - *On-Chip Noise, KTC Noise, Amplifier Noise, etc.*

# Degradation / Restoration



$$g(x, y) = h(x, y) * f(x, y) + n(x, y)$$
$$G(u, v) = H(u, v)F(u, v) + N(u, v)$$

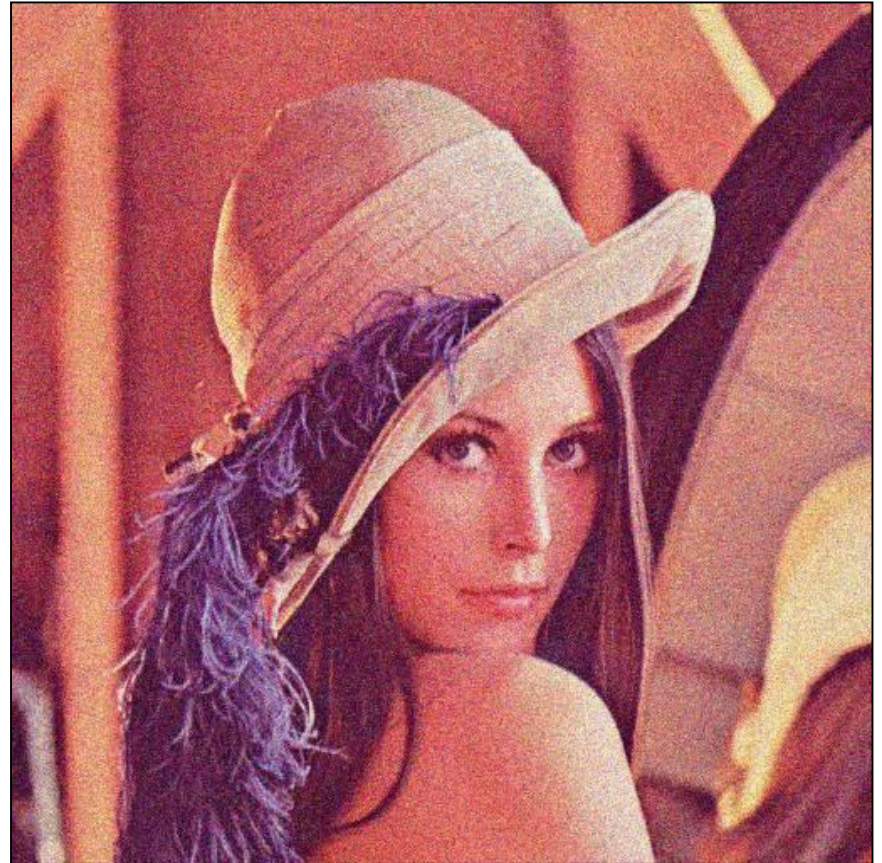


# Noise Models

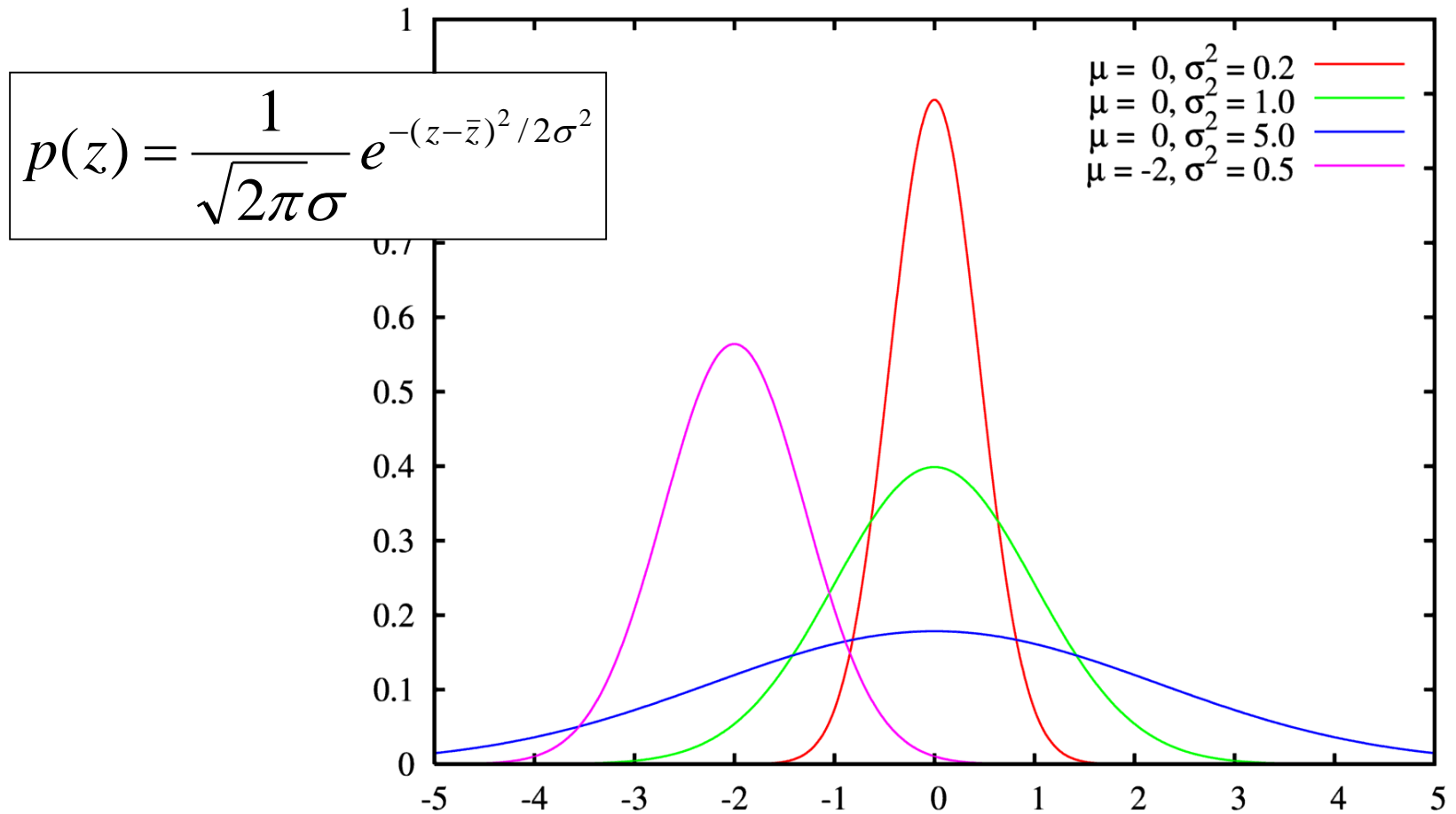
- **Noise models**
  - We need to mathematically handle noise.
  - Spatial and frequency properties.
  - Probability theory helps!
- **Advantages:**
  - Easier to filter noise.
  - Easier to measure its importance.
  - More robust systems!

# Model: Gaussian Noise

- Gaussian PDF (Probability Density Function).
- Great approximation of reality.
  - Models noise as a sum of various small noise sources, which is indeed what happens in reality.



# Model: Gaussian Noise



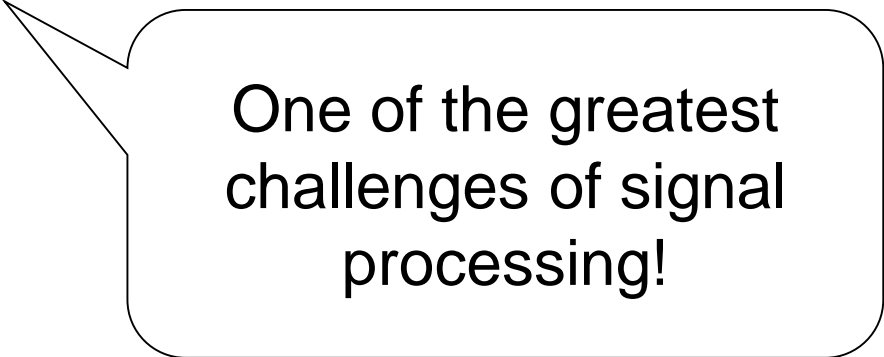
# Model: Salt and Pepper Noise

- Considers that a value can randomly assume the MAX or MIN value for that sensor.
  - Happens in reality due to the malfunction of isolated image sensors.



# How do we handle it?

- **Not always trivial!**
  - Frequency filters.
  - Estimate the degradation function.
  - Inverse filtering.
  - ...



One of the greatest challenges of signal processing!

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