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# VC 12/13 – T9

## Region-Based Segmentation

Mestrado em Ciência de Computadores  
Mestrado Integrado em Engenharia de Redes e  
Sistemas Informáticos

*Miguel Tavares Coimbra*

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# Outline

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- Region-based Segmentation
- Morphological Filters

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# Topic: Region-based Segmentation

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- Region-based Segmentation
- Morphological Filters

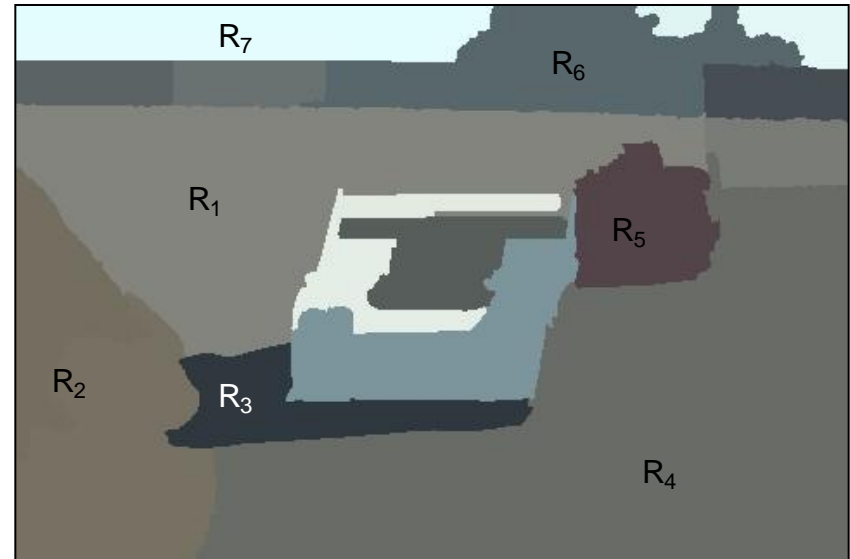
# Why Region-Based Segmentation?

- **Segmentation**
  - Edge detection and Thresholding not always effective.
- **Homogenous regions**
  - *Region-based segmentation.*
  - Effective in noisy images.

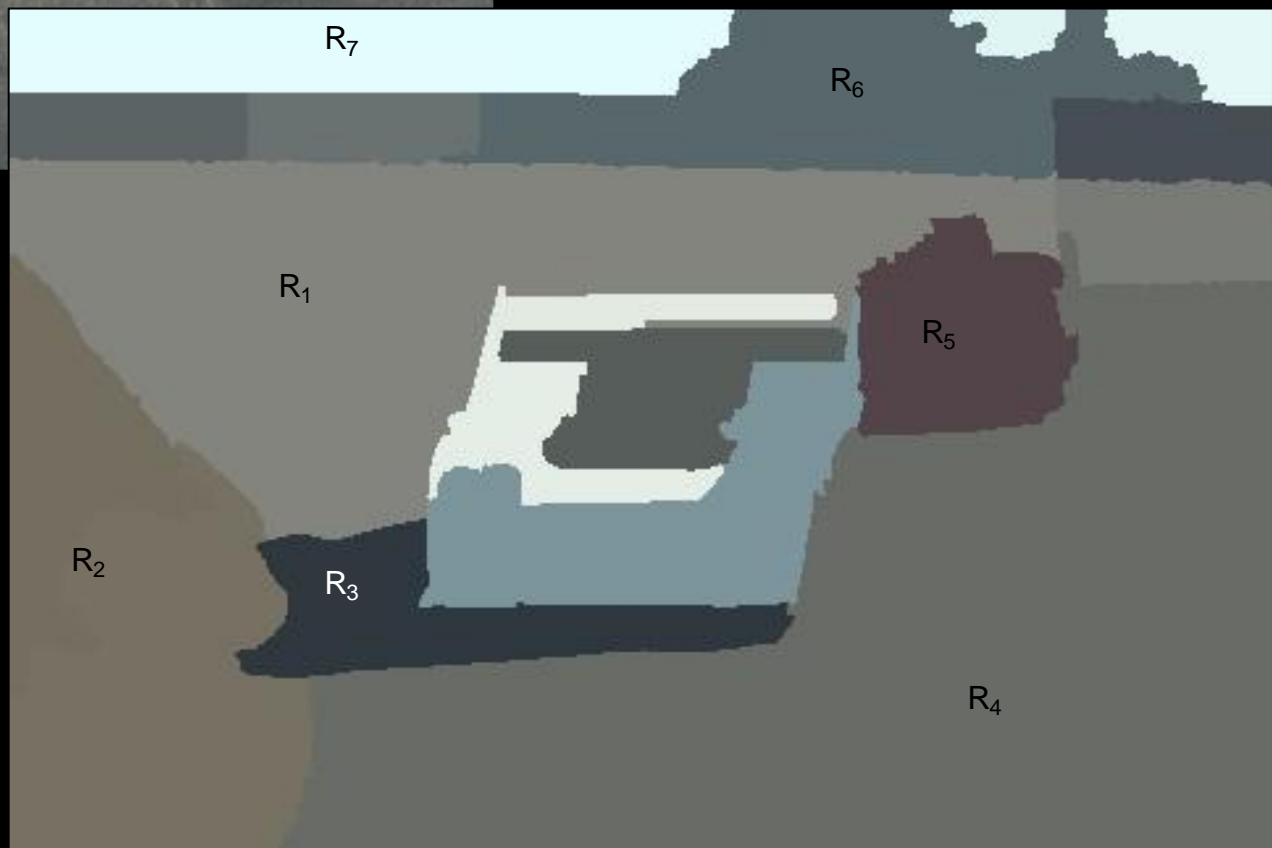


# Definitions

- Based on *sets*.
- Each image  $R$  is a set of regions  $R_i$ .
  - Every pixel belongs to one region.
  - One pixel can only belong to a single region.



$$R = \bigcup_{i=1}^S R_i \quad R_i \cap R_j = \emptyset$$



# Basic Formulation

Let  $R$  represent the entire image region. Segmentation partitions  $R$  into  $n$  subregions,  $R_1, R_2, \dots, R_n$ , such that:

a)  $\bigcup_{i=1}^n R_i = R$

b)  $R_i$  is a connected region,  $i = 1, 2, \dots, n$ .

c)  $R_i \cap R_j = \emptyset$  for all  $i$  and  $j, i \neq j$

d)  $P(R_i) = TRUE$  for  $i = 1, 2, \dots, n$ .

e)  $P(R_i \cup R_j) = FALSE$  for  $i \neq j$ .

a) Every pixel must be in a region

b) Points in a region must be connected.

c) Regions must be disjoint.

d) All pixels in a region satisfy specific properties.

e) Different regions have different properties.

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# How do we form regions?

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- Region Growing
- Region Merging
- Region Splitting
- Split and Merge
- Watershed
- ...

0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

What a computer sees

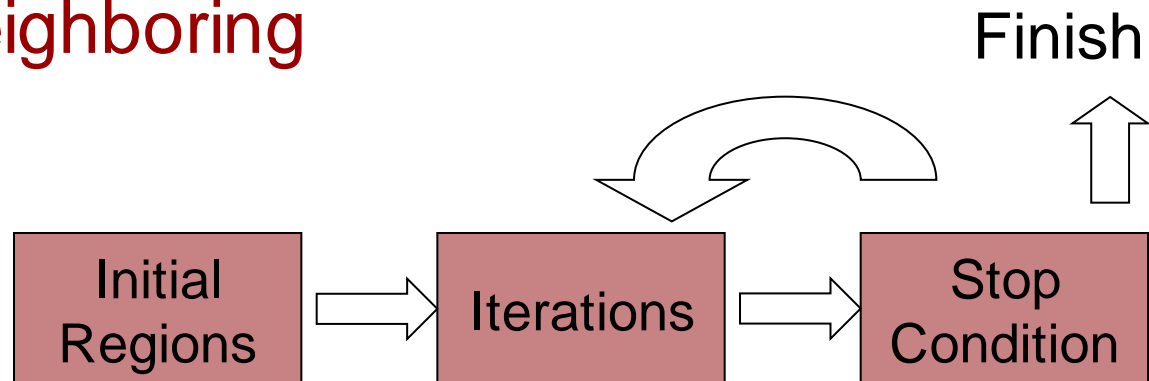


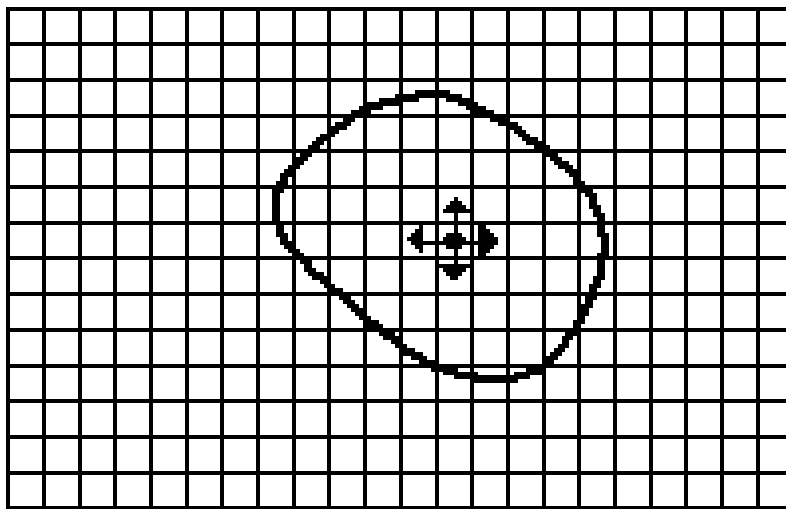
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# Region growing

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- Groups pixels into larger regions.
- Starts with a **seed** region.
- **Grows** region by **merging** neighboring pixels.
- Iterative process
  - How to start?
  - How to iterate?
  - When to stop?

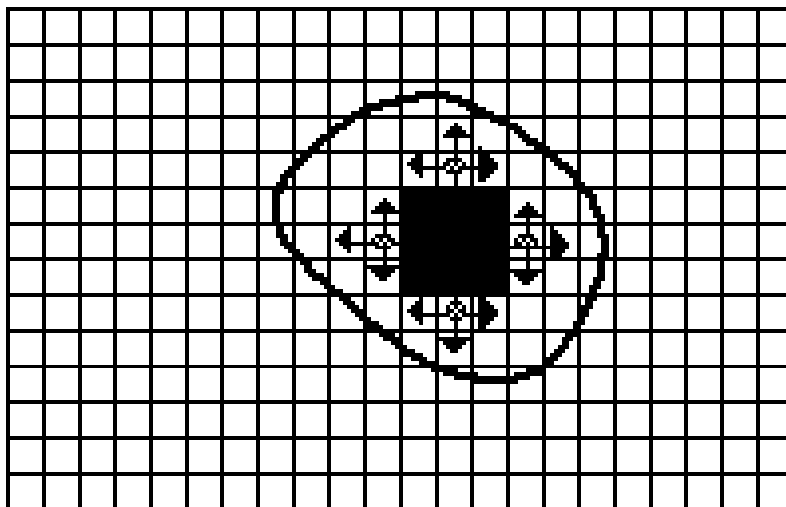




• Seed Pixel

↑ Direction of Growth

(a) Start of Growing a Region



■ Grown Pixels

⊙ Pixels Being Considered

(b) Growing Process After a Few Iterations

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# *Region merging*

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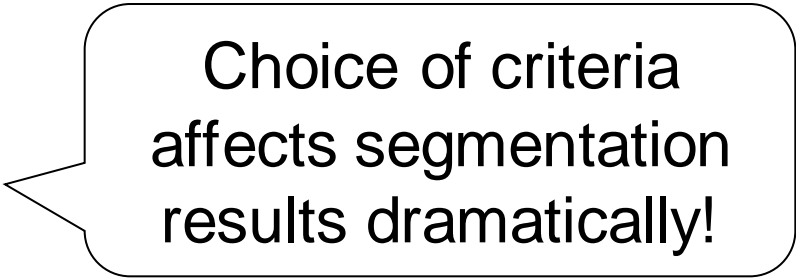
- **Algorithm**
  - Divide image into an initial set of regions.
    - One region per pixel.
  - Define a **similarity criteria** for merging regions.
  - **Merge** similar regions.
  - Repeat previous step until no more merge operations are possible.

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# Similarity Criteria

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- Homogeneity of regions is used as the main segmentation criterion in region growing.
  - gray level
  - color, texture
  - shape
  - model
  - etc.



Choice of criteria affects segmentation results dramatically!

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# Gray-Level Criteria

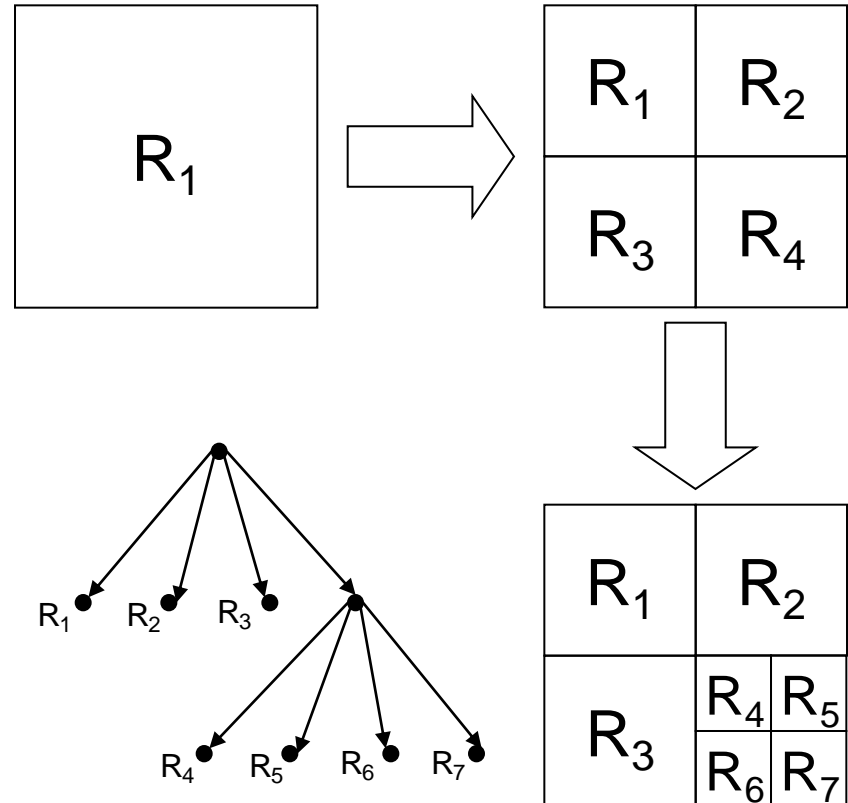
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- Comparing to Original Seed Pixel
  - Very sensitive to choice of **seed point**.
- Comparing to Neighbor in Region
  - Allows gradual changes in the region.
  - Can cause significant drift.
- Comparing to Region Statistics
  - Acts as a **drift dampener**.
- Other possibilities!

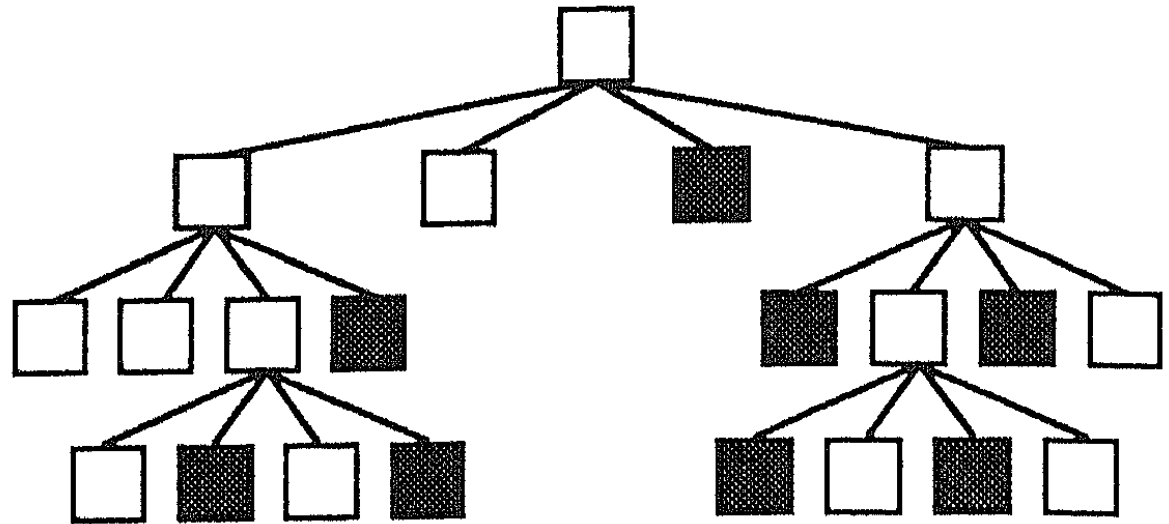
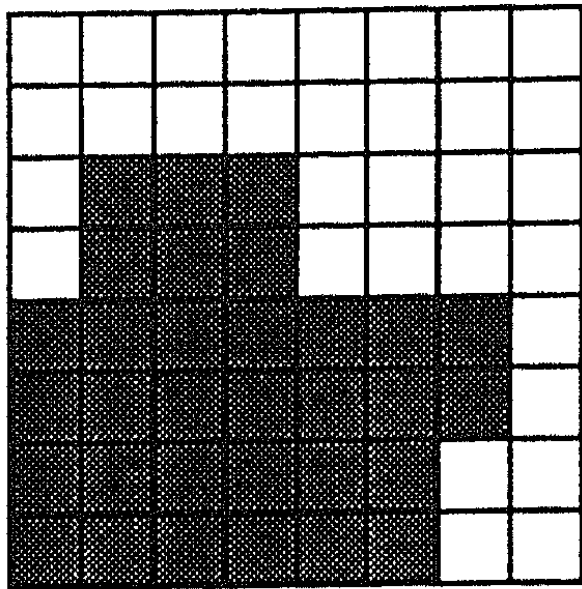
# Region splitting

- Algorithm

- One initial set that includes the **whole image**.
- **Similarity criteria.**
- Iteratively **split** regions into sub-regions.
- Stop when no more splittings are possible.



*The segmentation problem*



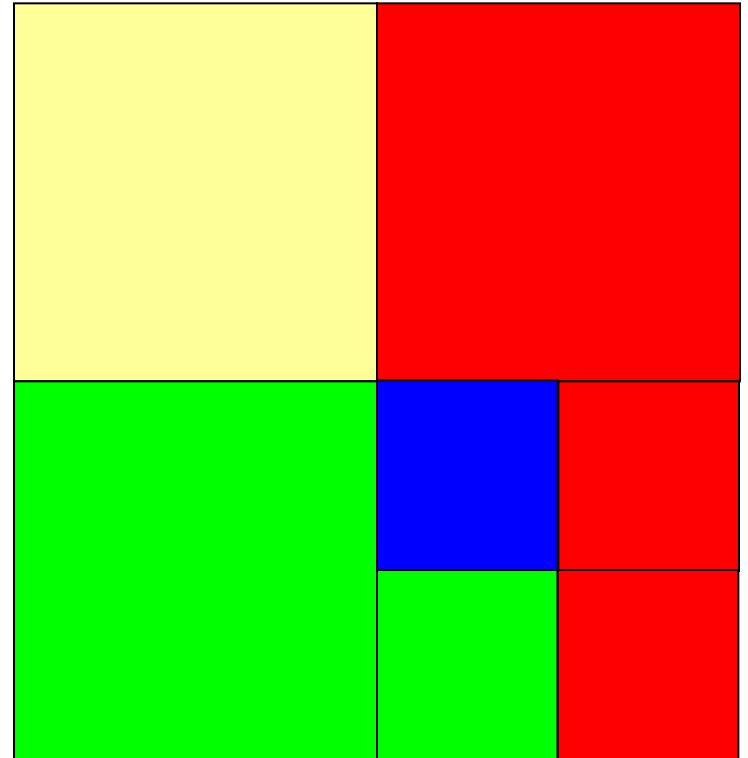
**Figure 5.23** A quad-tree representation of an  $8 \times 8$  binary image.

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# *Split and Merge*

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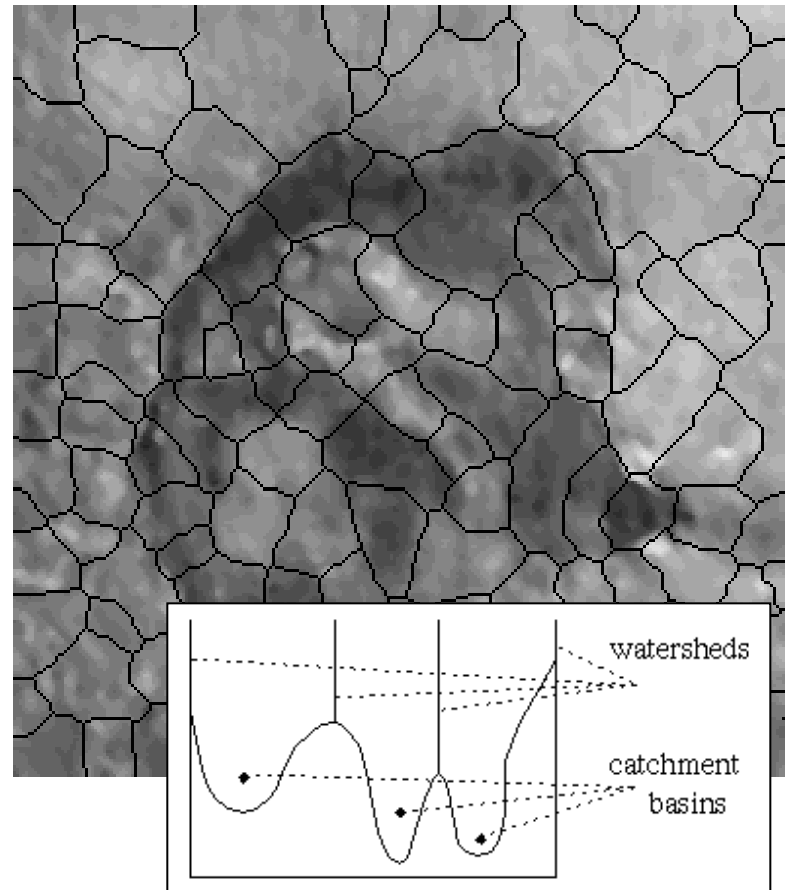
- Combination of both algorithms.
- Can handle a larger variety of shapes.
  - Simply apply previous algorithms consecutively.





# The *Watershed* Transform

- **Geographical inspiration.**
  - Shed water over rugged terrain.
  - Each lake corresponds to a region.
- **Characteristics**
  - Computationally complex.
  - Great flexibility in segmentation.
  - Risk of over-segmentation.

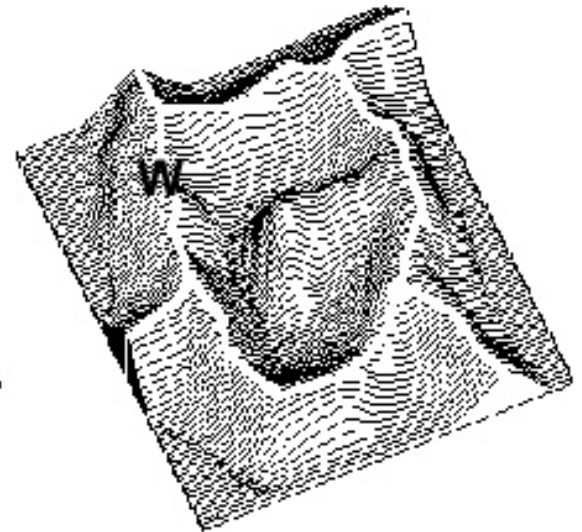
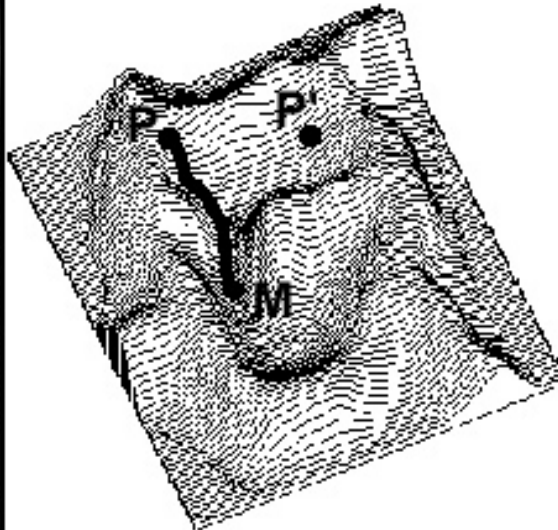
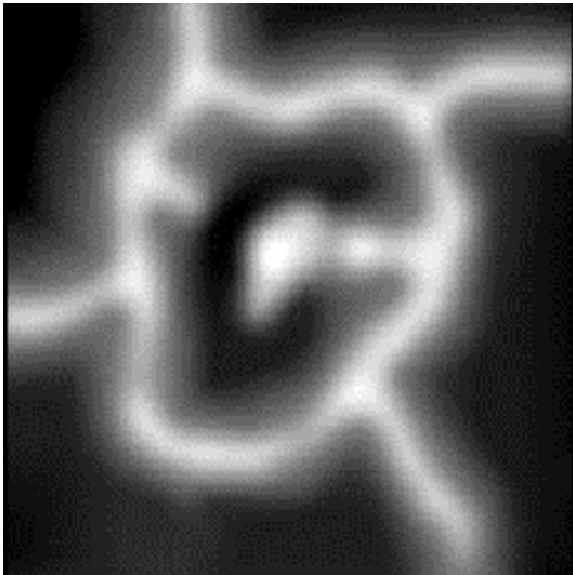


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# The Drainage Analogy

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- Two points are in the same region if they drain to the same point.

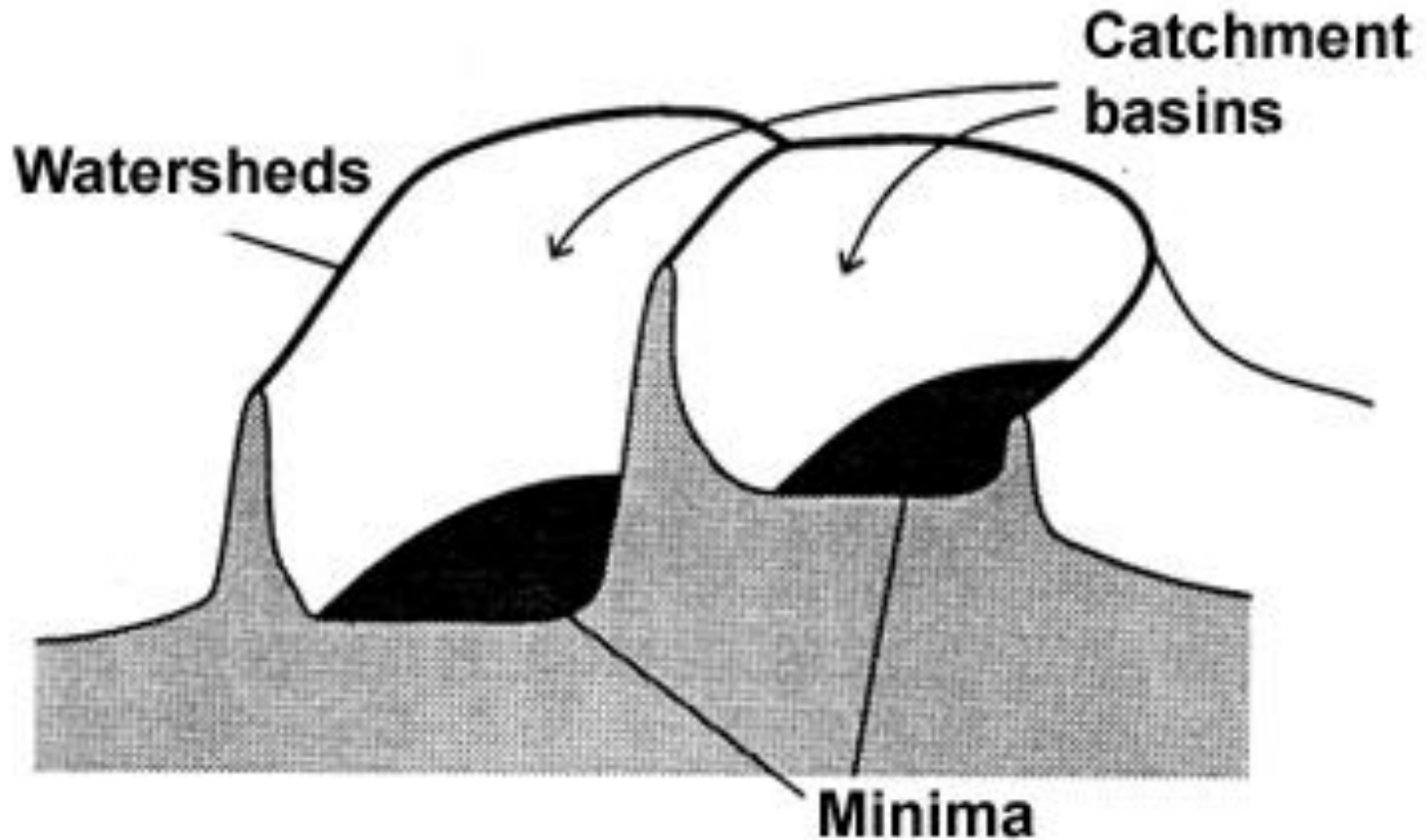


Courtesy of Dr. Peter Yim at National Institutes of Health, Bethesda, MD

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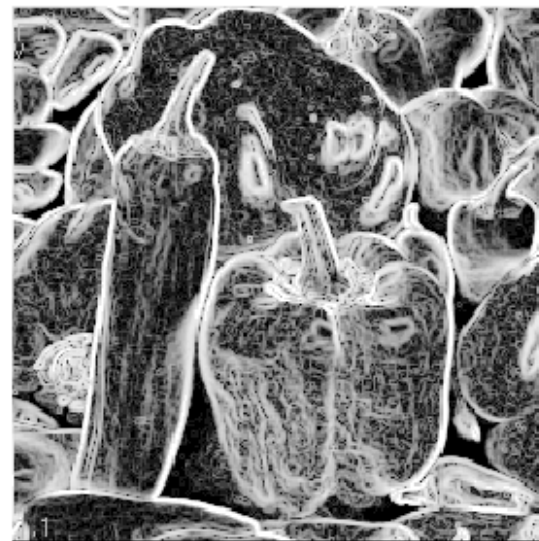
# The Immersion Analogy

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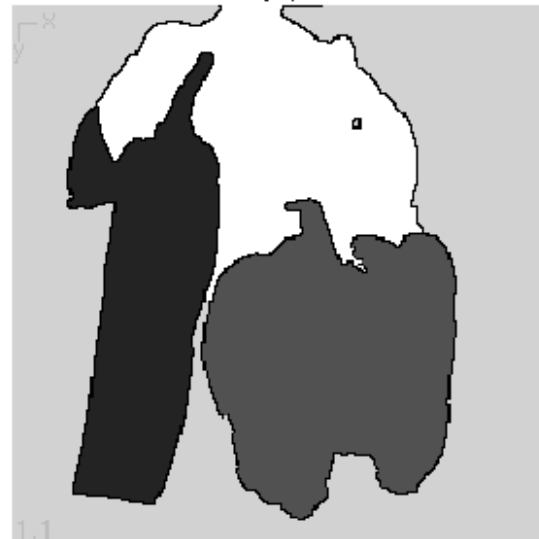
(a)



(b)



(c)



(d)

[Milan Sonka,  
Vaclav Hlavac,  
and Roger Boyle]

Figure 5.51: *Watershed segmentation: (a) original; (b) gradient image,  $3 \times 3$  Sobel edge detection, histogram equalized; (c) raw watershed segmentation; (d) watershed segmentation using region markers to control oversegmentation. Courtesy W. Higgins, Penn State University.*

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# Over-Segmentation

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- **Over-segmentation.**
  - Raw watershed segmentation produces a severely oversegmented image with hundreds or thousands of catchment basins.
- **Post-Processing.**
  - Region merging.
  - Edge information.
  - Etc.

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# Topic: Morphological Filters

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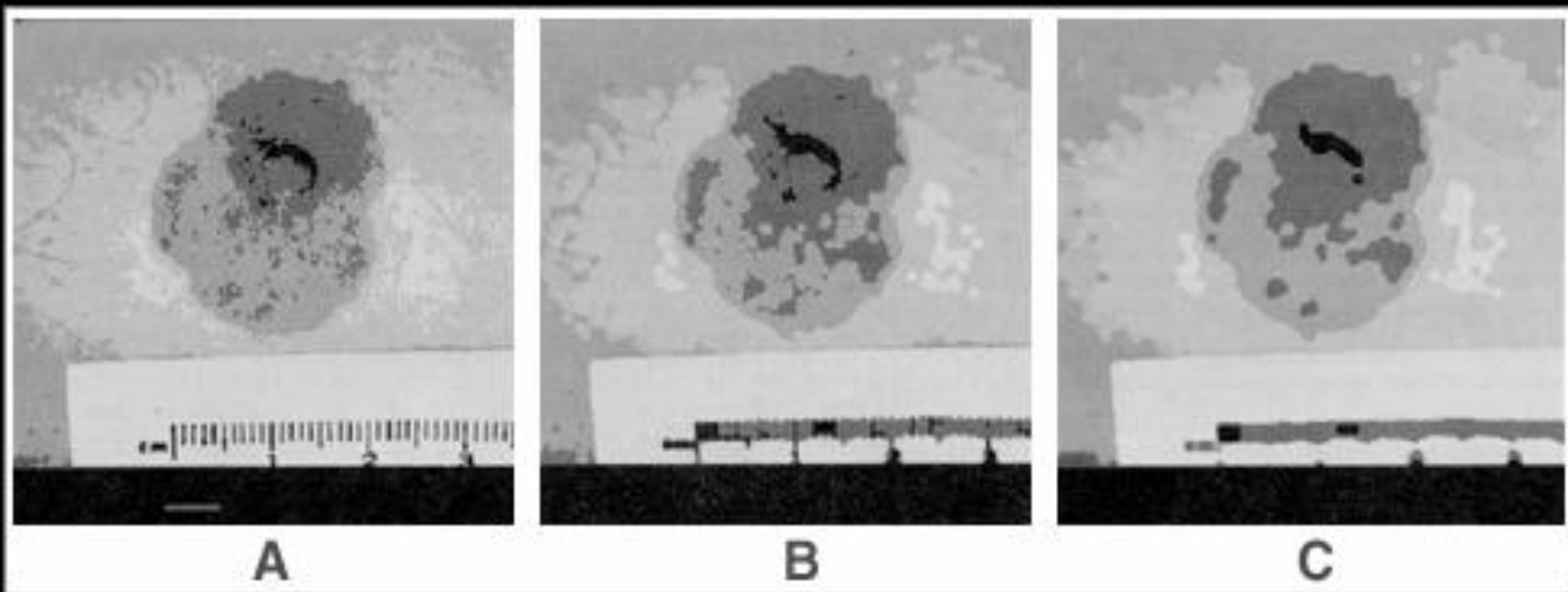
- Region-based Segmentation
- **Morphological Filters**

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# Mathematical Morphology

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- Provides a mathematical description of geometric structures.
- Based on *sets*.
  - Groups of pixels which define an image region.
- What is this used for?
  - Binary images.
  - Can be used for **post-processing** segmentation results!
- Core techniques
  - Erosion, Dilation.
  - Open, Close.

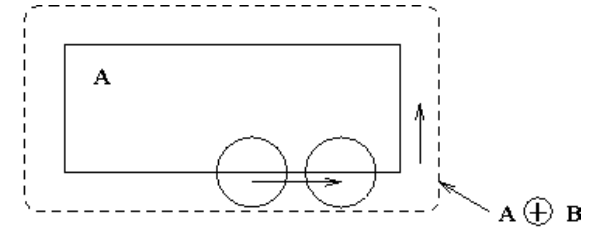
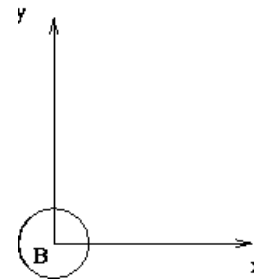


Tumor Segmentation using Morphologic Filtering



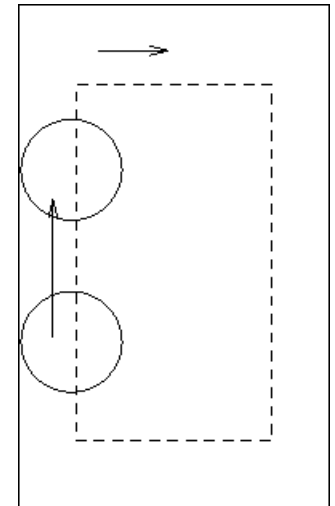
# Dilation, Erosion

- Two sets:
  - Image
  - Morphological *kernel*.
- Dilation (D)
  - Union of the **kernel** with the **image** set.
  - Increases resulting area.
- Erosion (E)
  - Intersection.
  - Decreases resulting area.



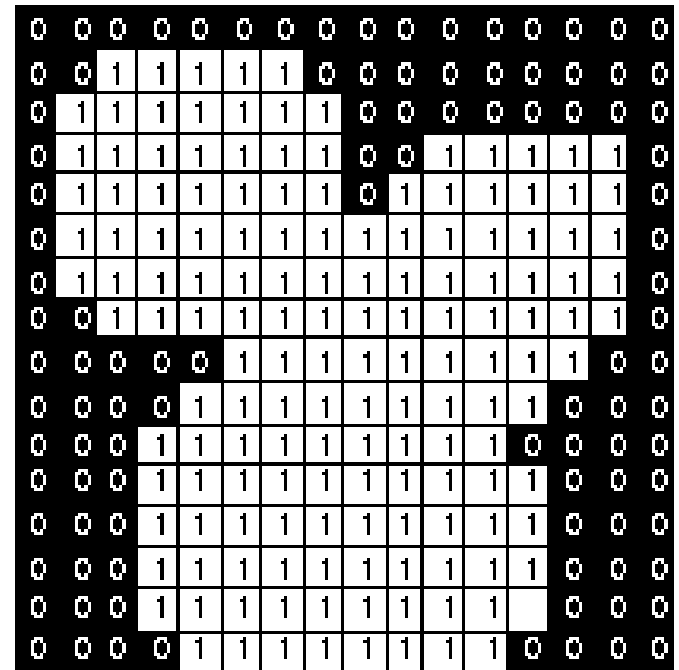
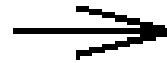
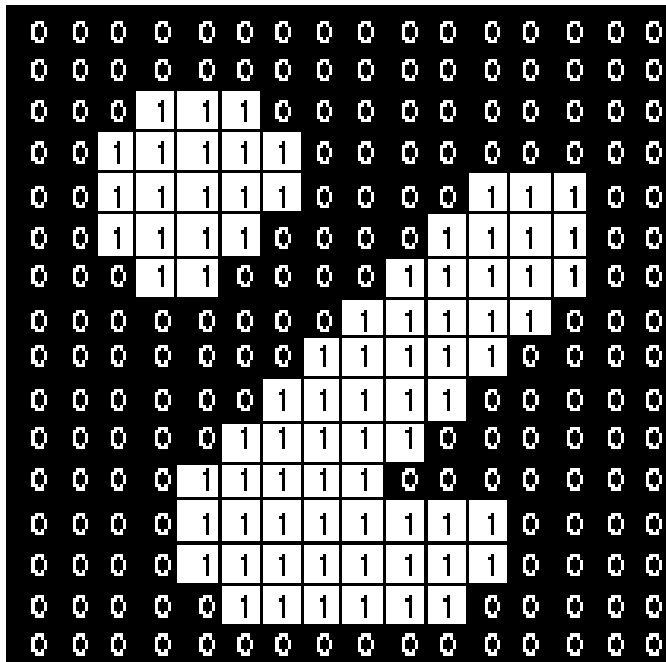
$$D(A, B) = A \oplus B = \bigcup_{\beta \in B} (A + \beta)$$

$$E(A, B) = A \ominus B = \bigcap_{\beta \in B} (A - \beta)$$



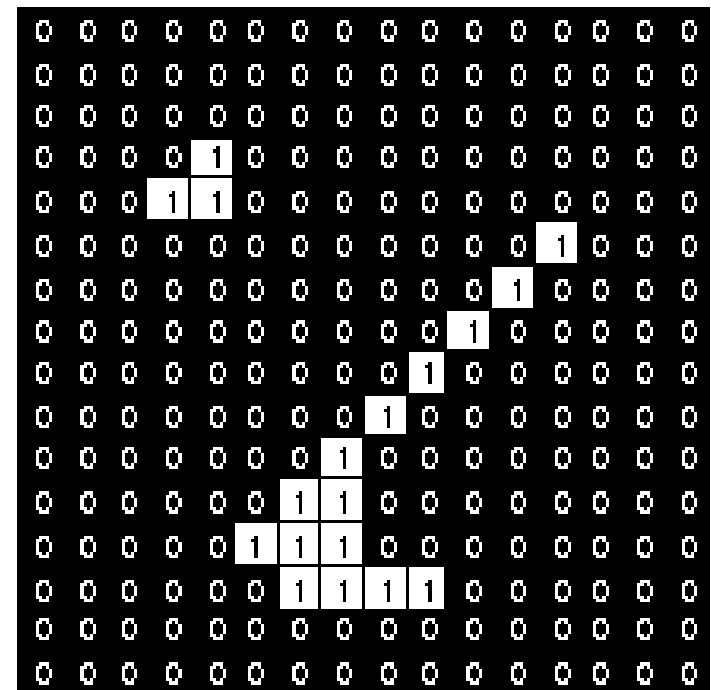
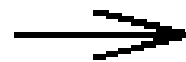
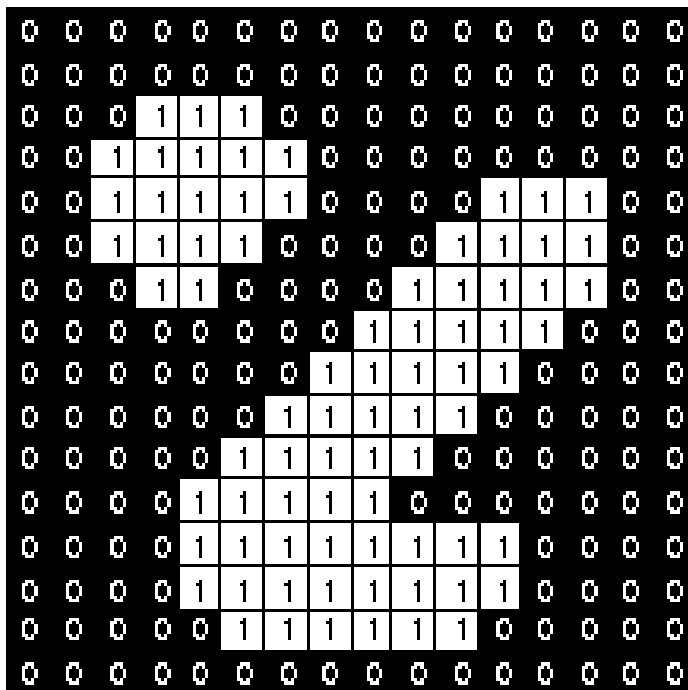
# Dilation

- Example using a 3x3 morphological kernel



# Erosion

- Example using a 3x3 morphological kernel



# Opening, Closing

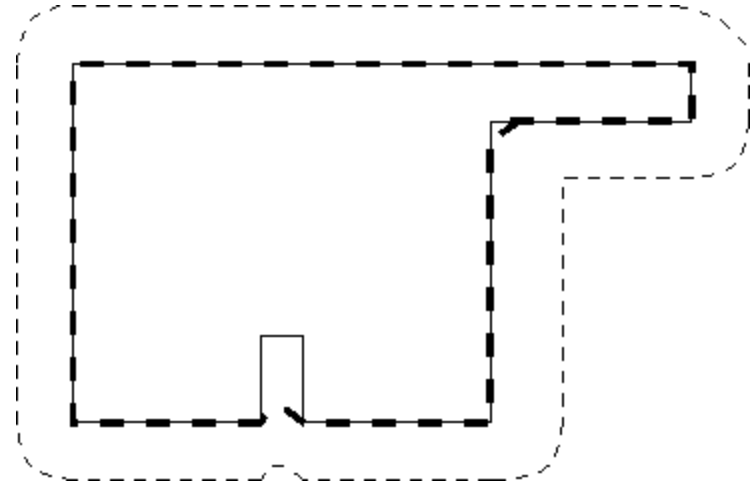
- **Opening**

- **Erosion**, followed by **dilation**.
- Less destructive than an erosion.
- **Adapts** image shape to kernel shape.



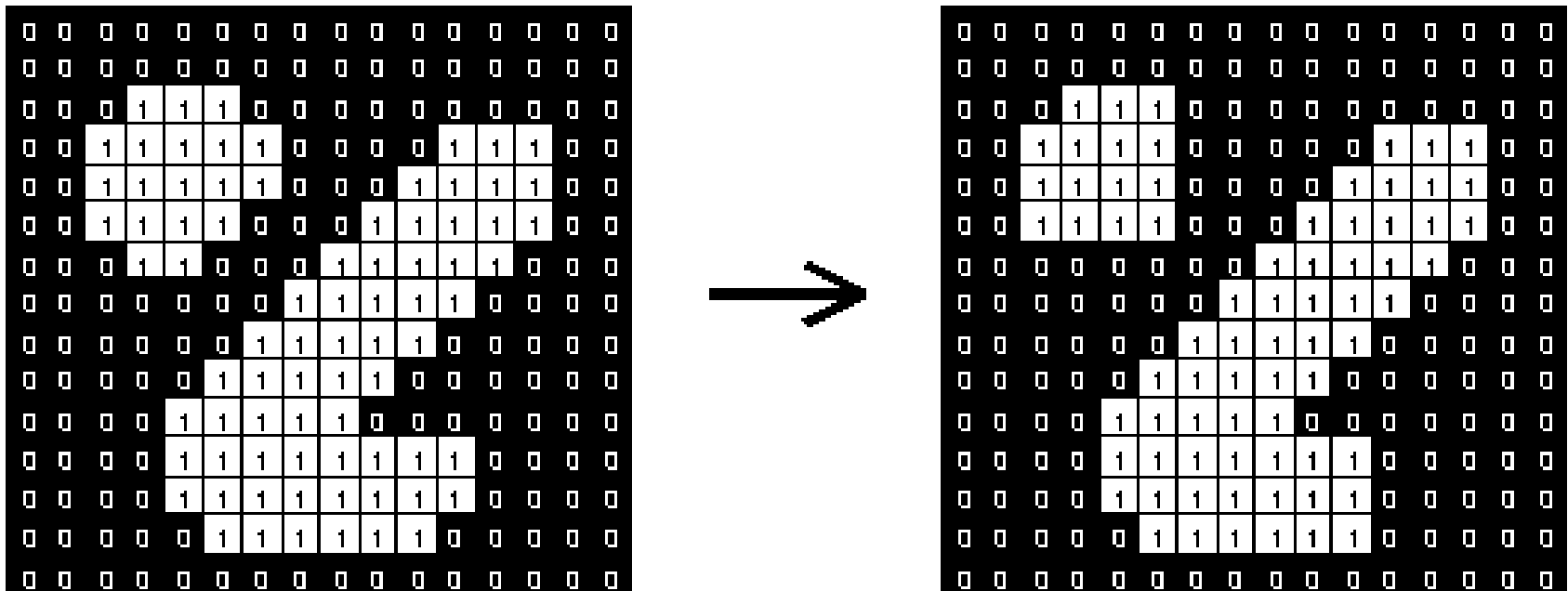
- **Closing**

- **Dilation**, followed by **erosion**.
- Less destructive than a dilation.
- Tends to **close** shape irregularities.



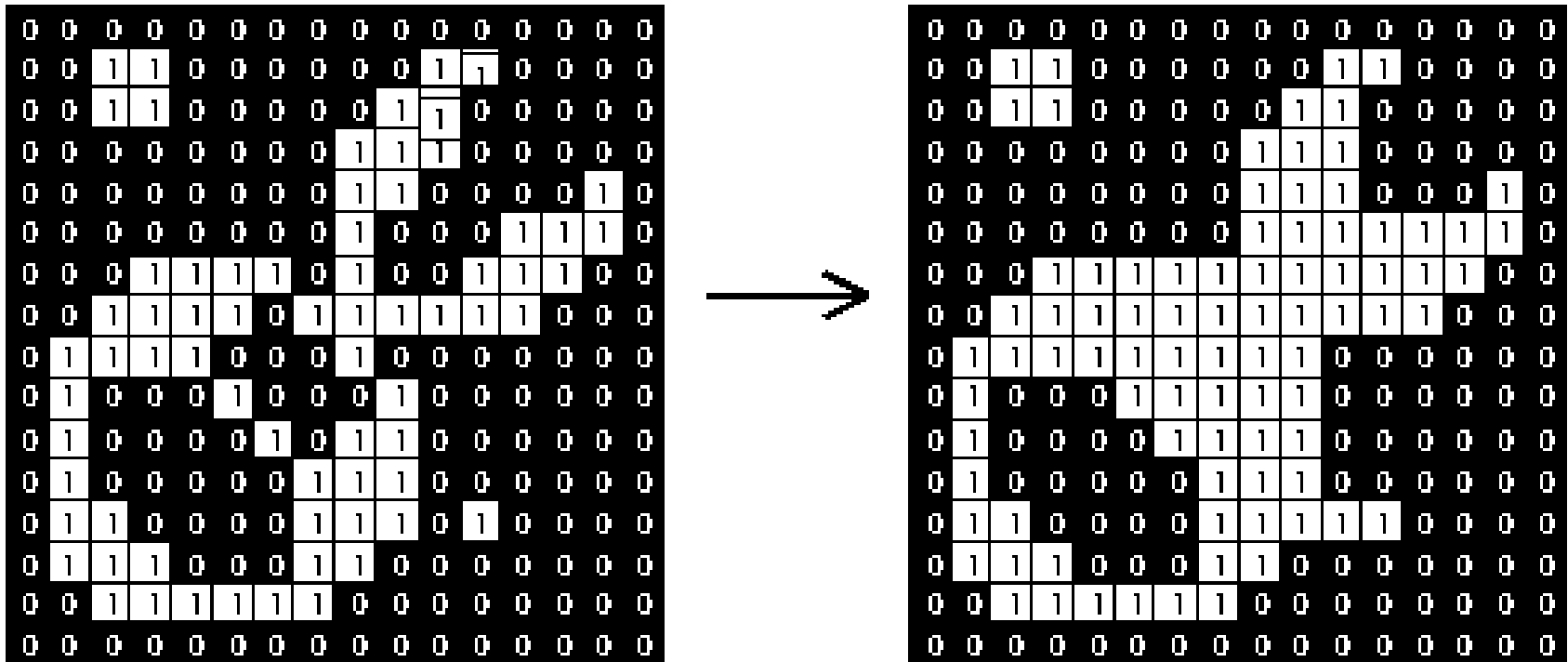
# Opening

- Example using a 3x3 morphological kernel



# Closing

- Example using a 3x3 morphological kernel



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# Core morphological operators

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Dilation



Erosion

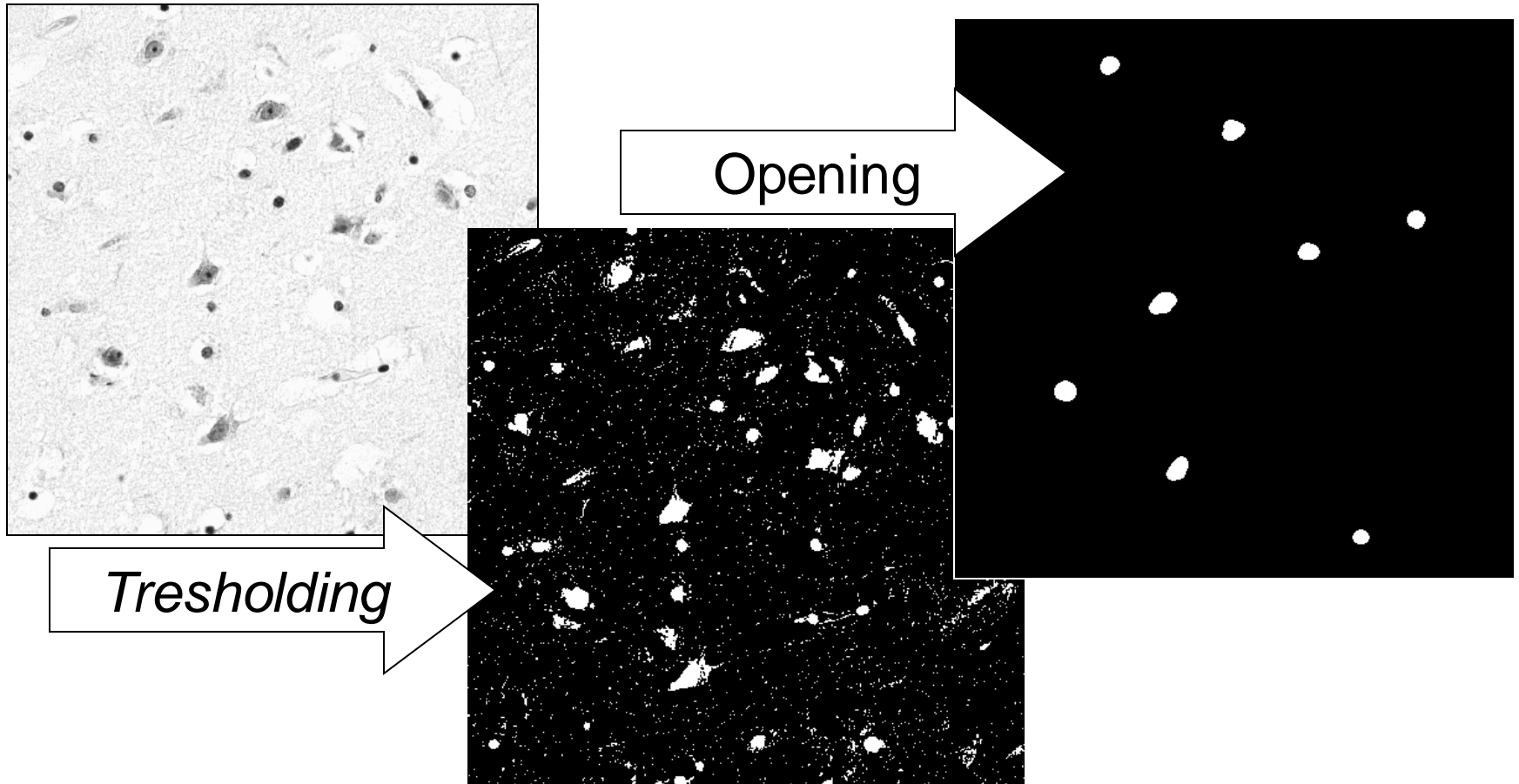


Closing



Opening

# Example: Opening

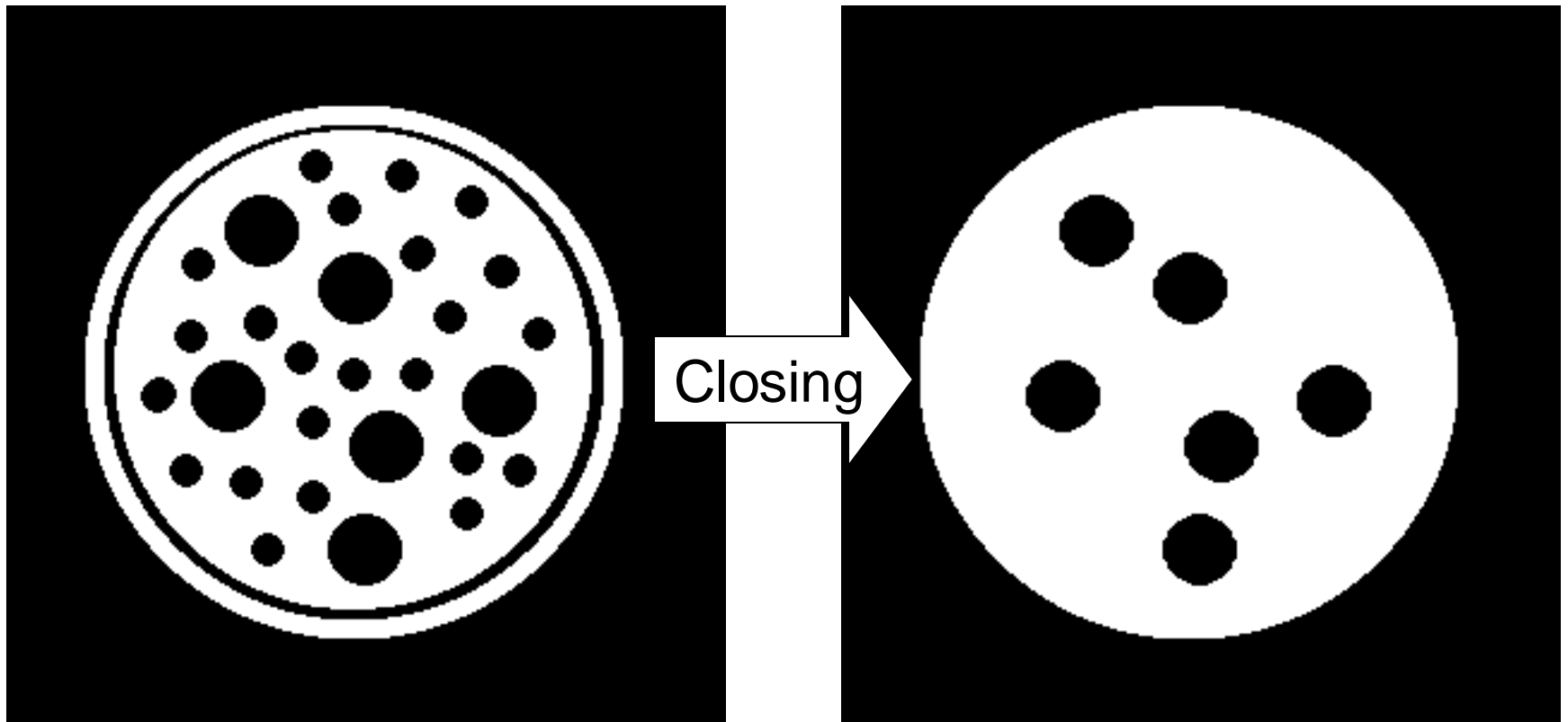




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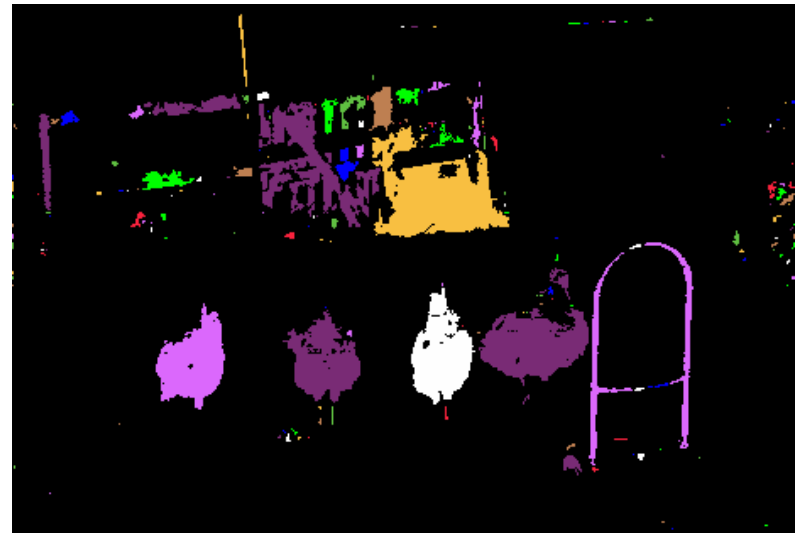
# Example: Closing

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# Connected Component Analysis

- Define '**connected**'.
  - 4 neighbors.
  - 8 neighbors.
- Search the image for **seed points**.
- Recursively obtain all **connected points** of the seeded region.



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# Resources

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- Gonzalez & Woods - Chapter 7 and 8