

# VC 19/20 – TP2

## Image Formation

Mestrado em Ciência de Computadores  
Mestrado Integrado em Engenharia de Redes e  
Sistemas Informáticos

***Miguel Tavares Coimbra***

# Outline

- ‘Computer Vision’?
- The Human Visual System
- Image Capturing Systems

# Topic: Computer Vision?

- 'Computer Vision'?
- The Human Visual System
- Image Capturing Systems

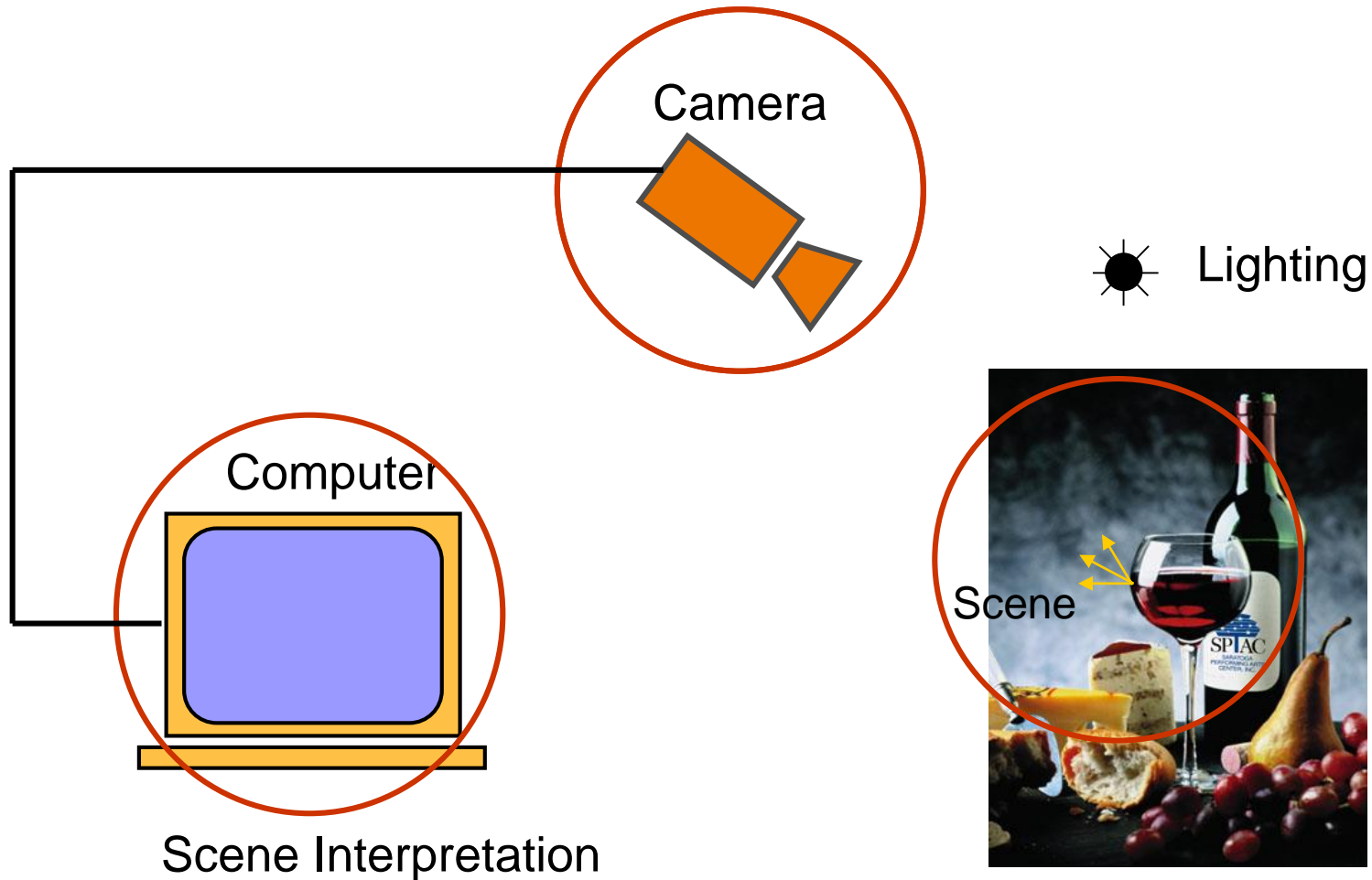
# Computer Vision

“The goal of **Computer Vision** is to make useful decisions about real physical objects and scenes based on sensed images”,

Shapiro and Stockman, “Computer Vision”, 2001



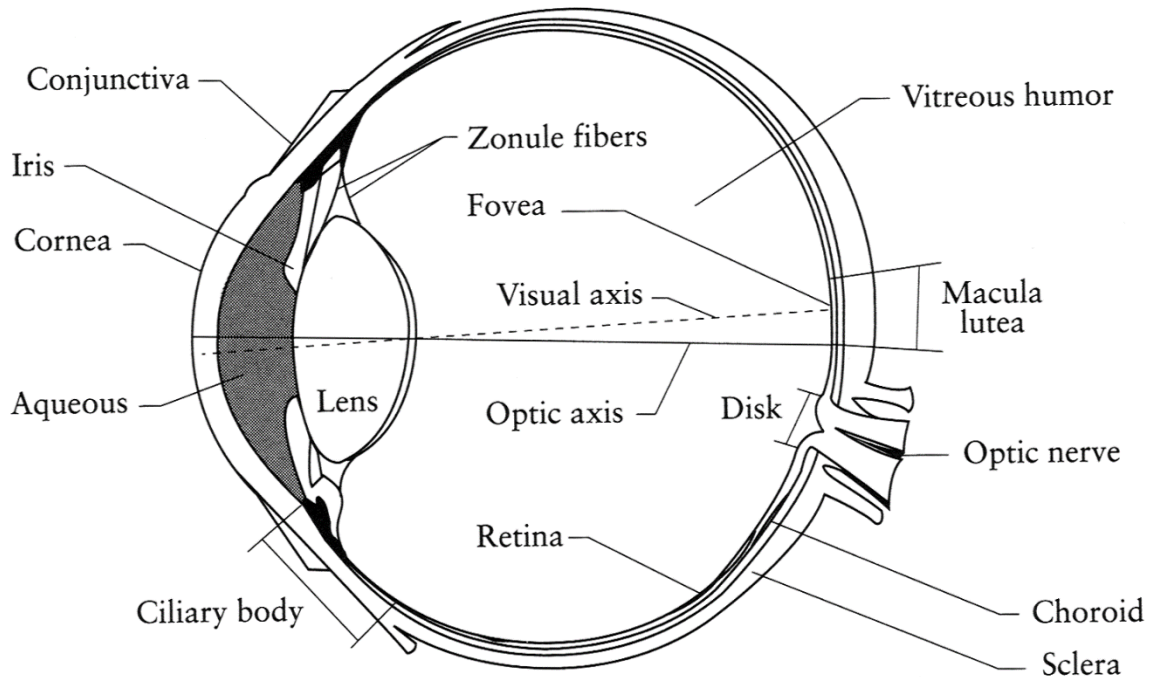
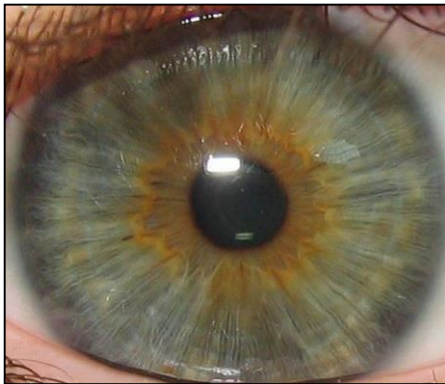
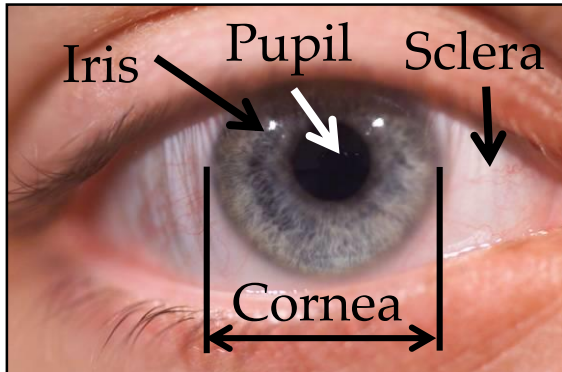
# Components of a Computer Vision System



# Topic: The Human Visual System

- 'Computer Vision'?
- **The Human Visual System**
- Image Capturing Systems

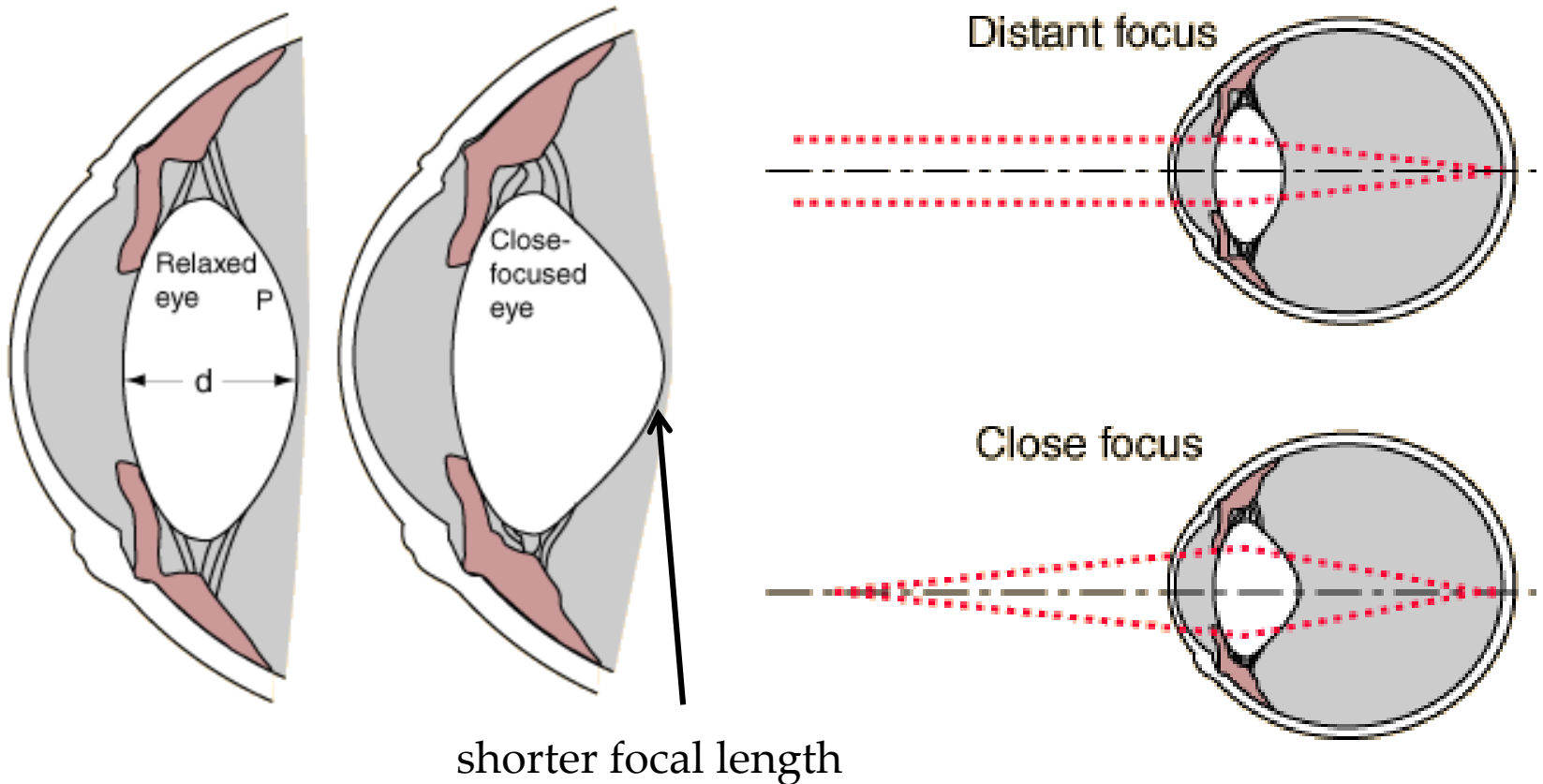
# Our Eyes



-Iris is the diaphragm that changes the aperture (pupil)

-Retina is the sensor where the fovea has the highest resolution

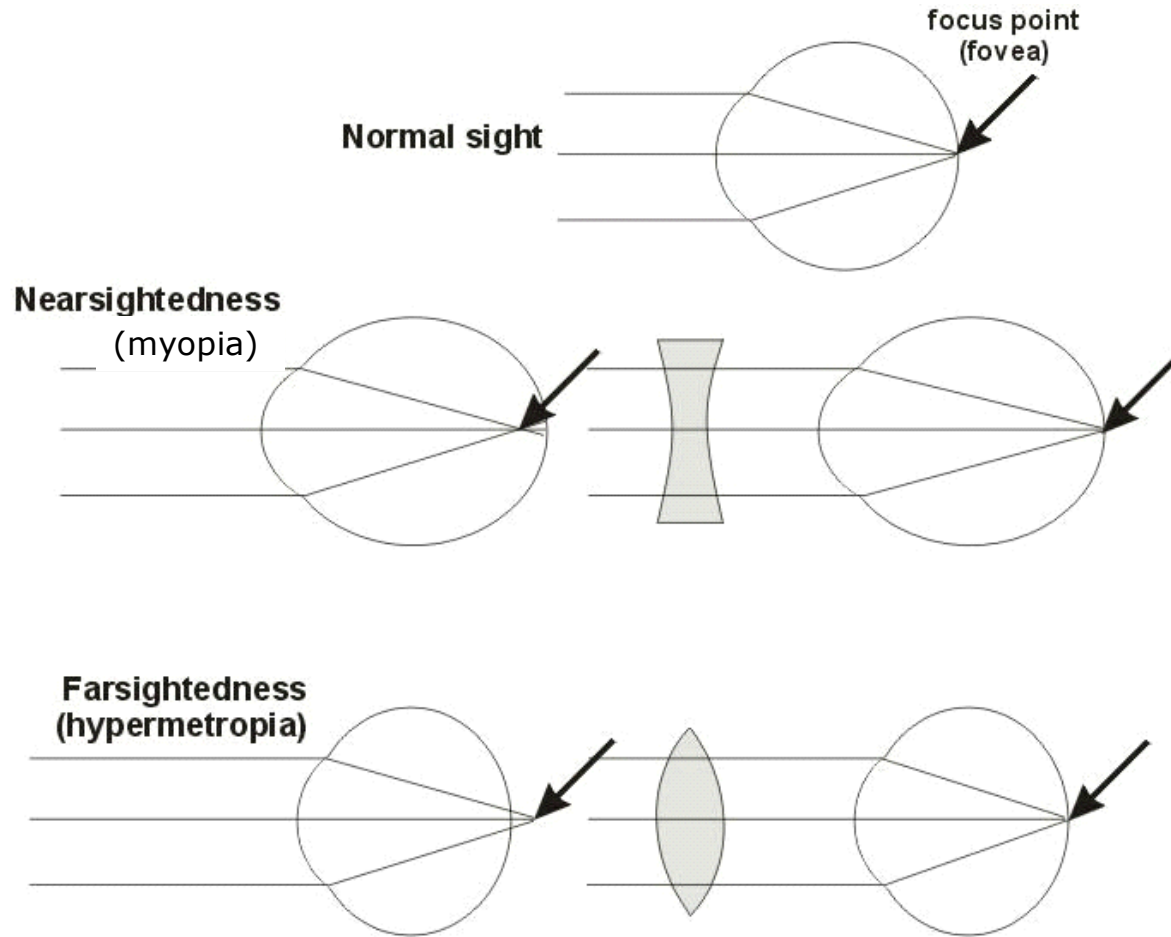
# Focusing



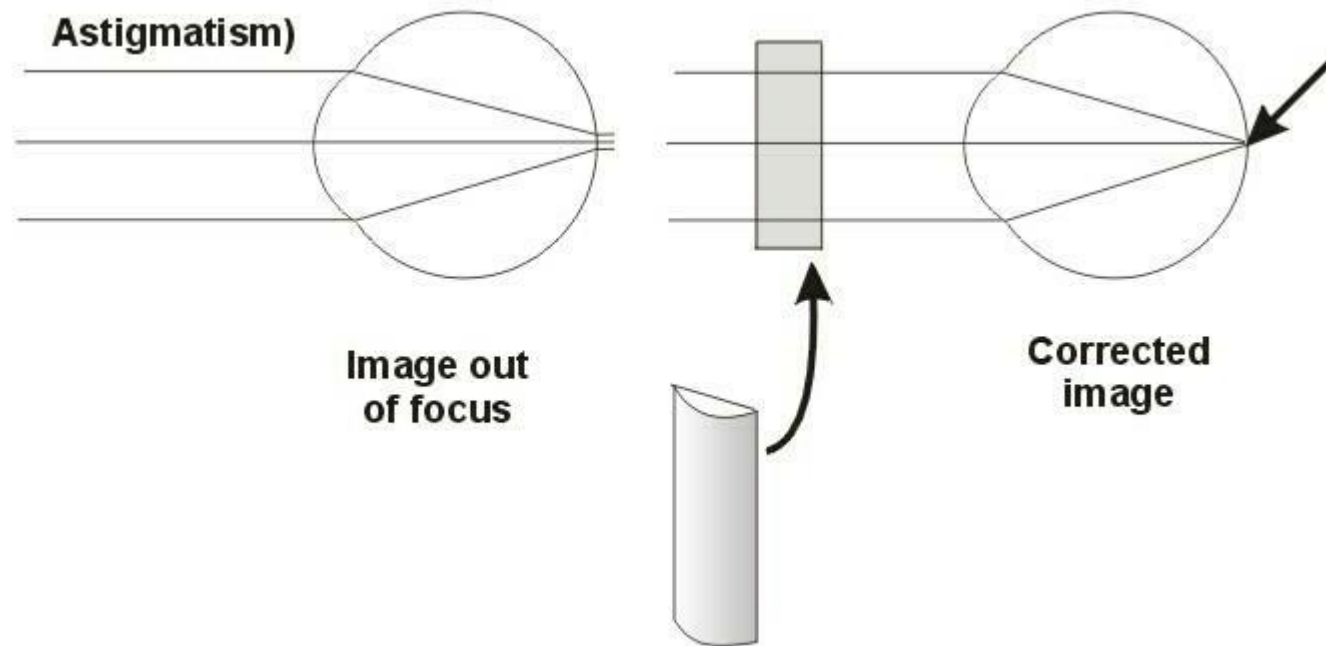
Changes the focal length of the lens



# Myopia and Hyperopia



# Astigmatism



The cornea is distorted causing images to be un-focused on the retina.

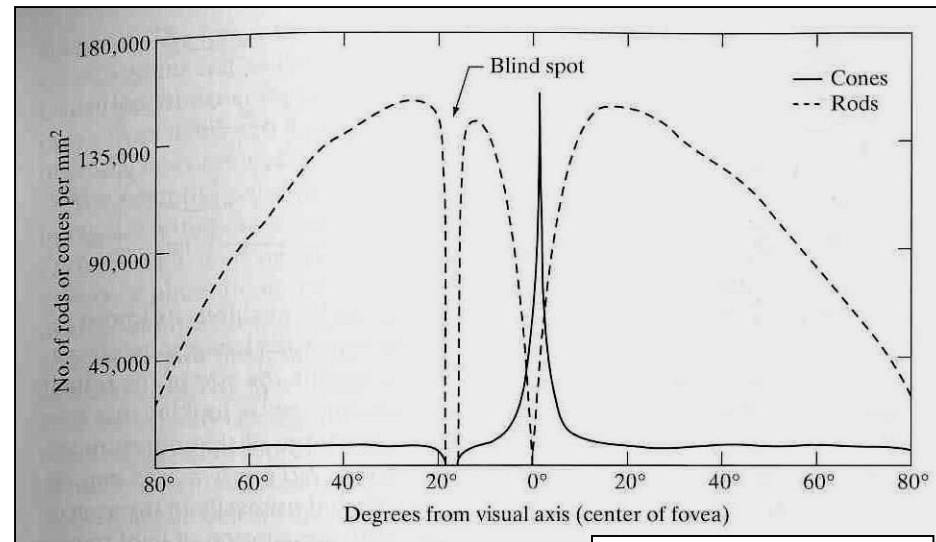
# Blind Spot in the Eye



Close your right eye and look directly at the “+”

# Colour

- **Our retina has:**
  - **Cones** – Measure the frequency of light (colour)
    - 6 to 7 millions
    - High-definition
    - Need high luminosity
  - **Rods** – Measure the intensity of light (luminance)
    - 75 to 150 millions
    - Low-definition
    - Function with low luminosity



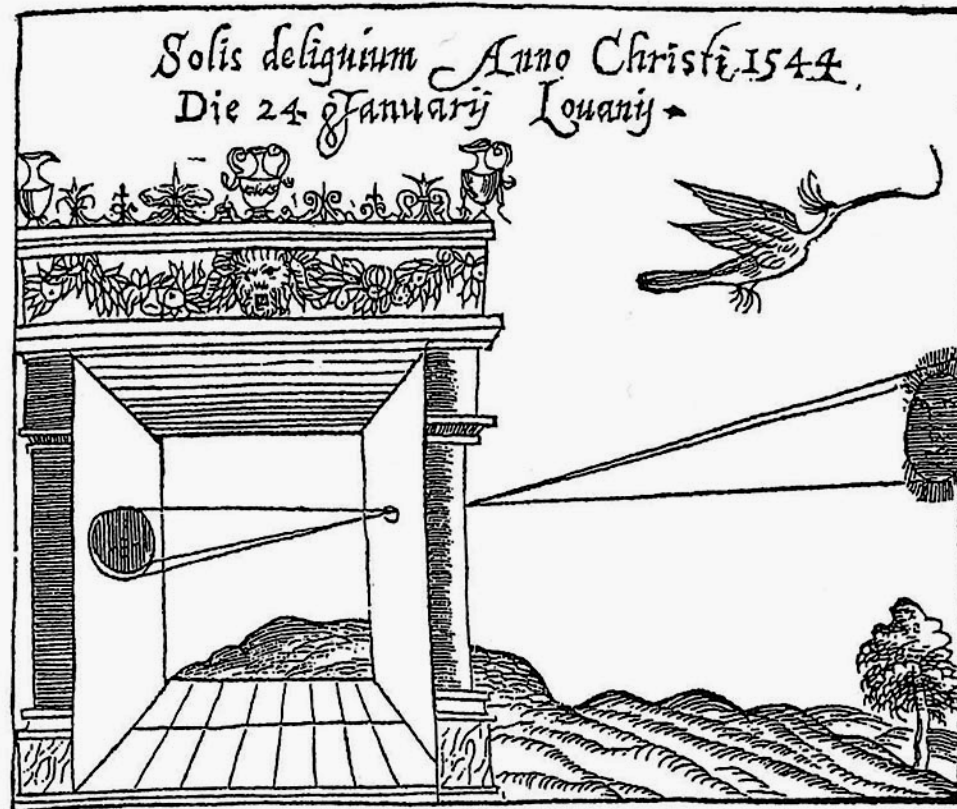
Gonzalez & Woods

We only see colour in the center of our retina!

# Topic: Image Capturing Systems

- 'Computer Vision'?
- The Human Visual System
- **Image Capturing Systems**

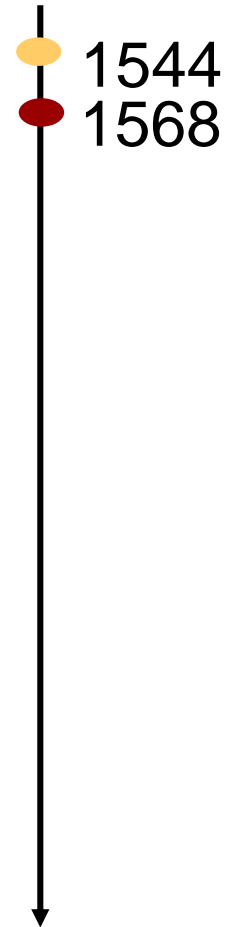
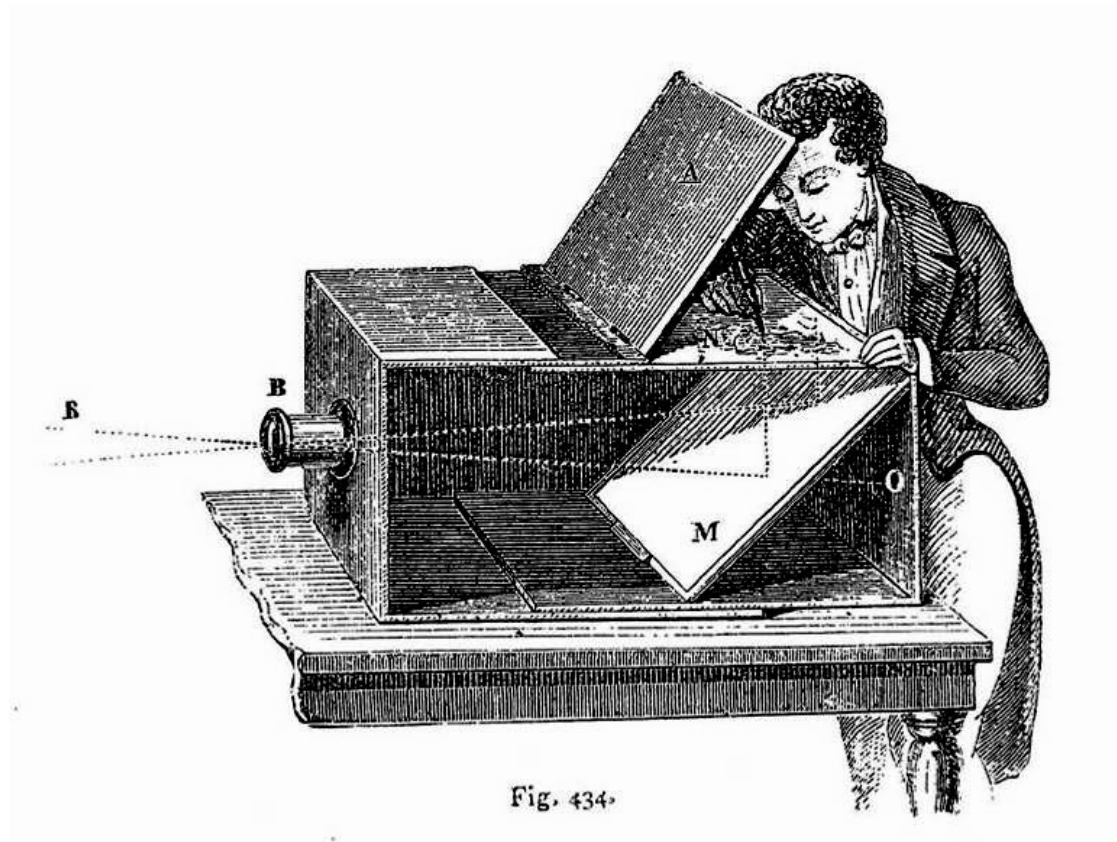
# A Brief History of Images



1544

*Camera Obscura*, Gemma Frisius, 1544

# A Brief History of Images

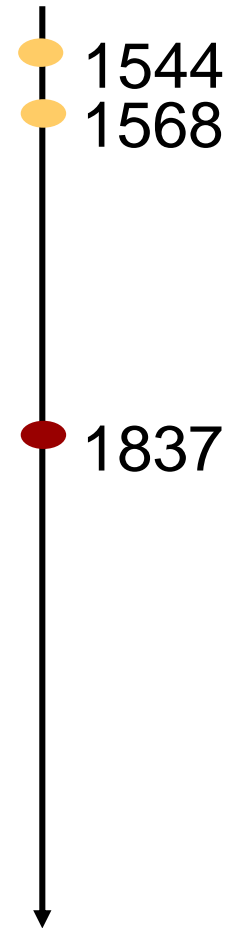


Lens Based Camera Obscura, 1568

# A Brief History of Images

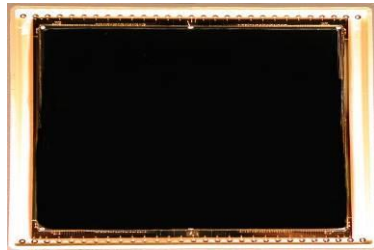


*Still Life*, Louis Jaques Mande Daguerre, 1837

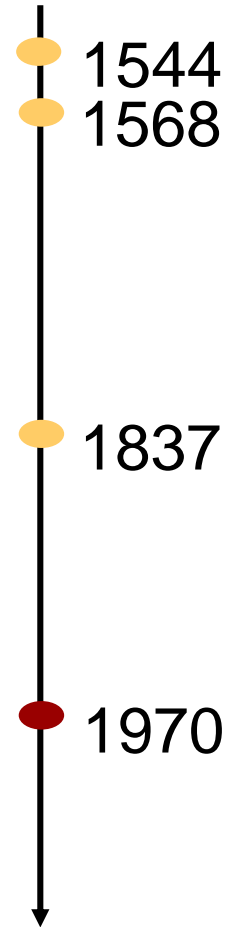




# A Brief History of Images



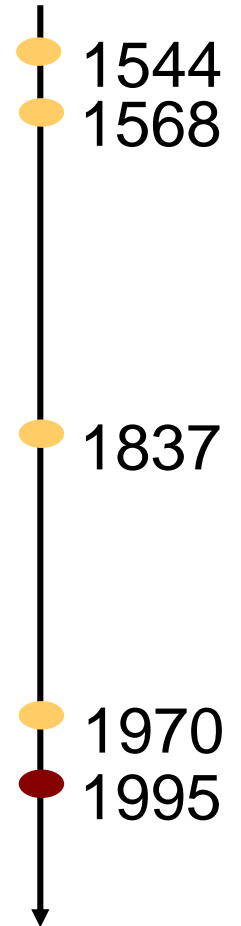
Silicon Image Detector, 1970



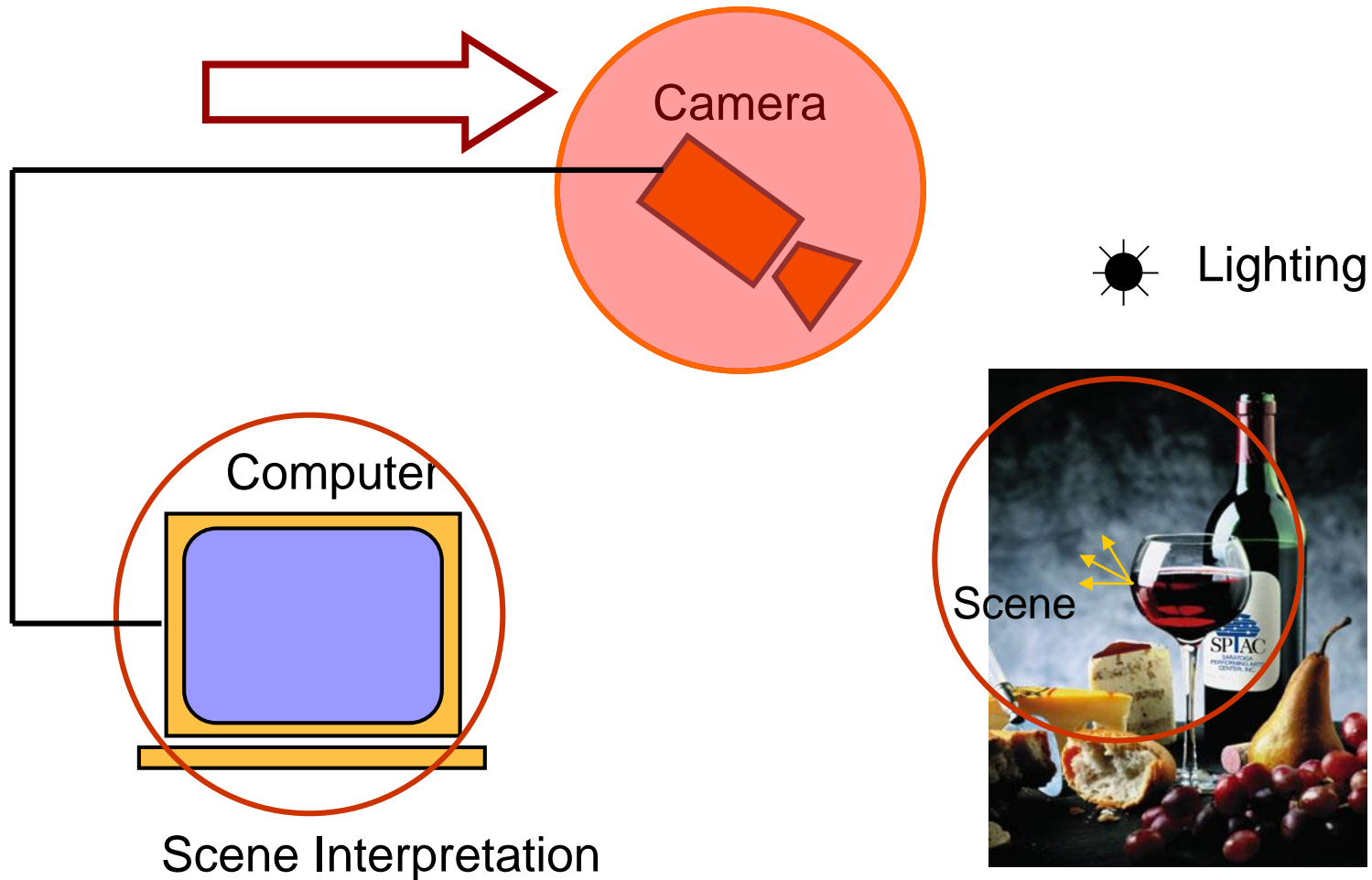
# A Brief History of Images



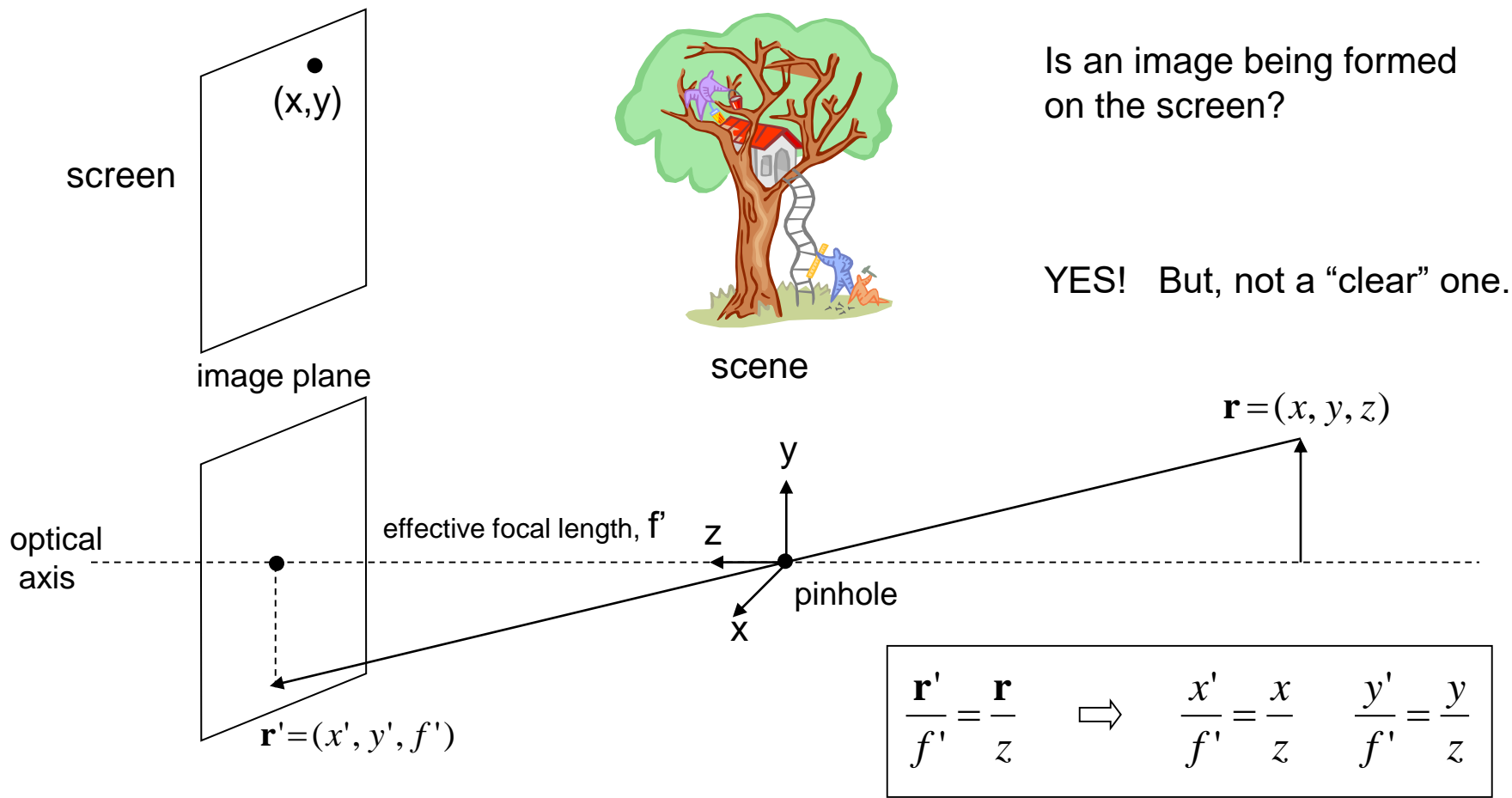
Digital Cameras



# Components of a Computer Vision System

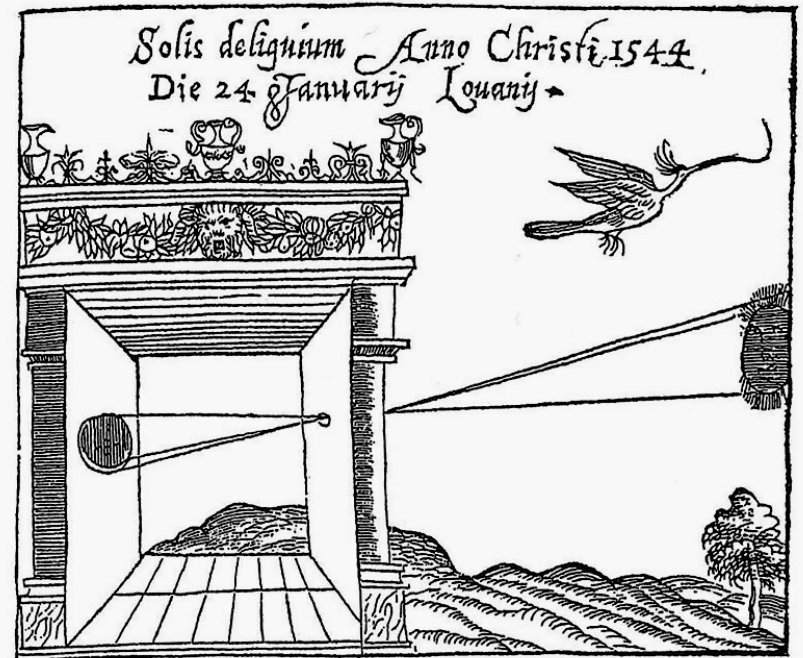


# Pinhole and the Perspective Projection



# Pinhole Camera

- Basically a pinhole camera is a box, with a tiny hole at one end and film or photographic paper at the other.
- Mathematically: out of all the light rays in the world, choose the set of light rays passing through a point and projecting onto a plane.



# Pinhole Photography



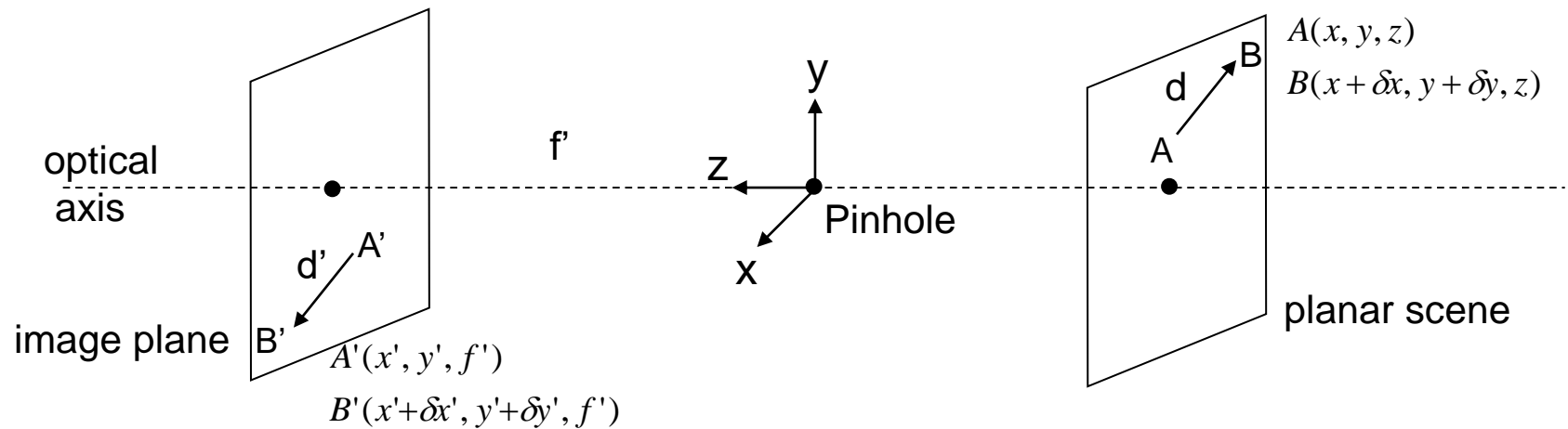
©Charlotte Murray Untitled, 4" x 5" pinhole photograph, 1992



Image Size inversely proportional to Distance

Reading: <http://www.pinholeresource.com/>

# Magnification



From perspective projection:

$$\frac{x'}{f'} = \frac{x}{z} \quad \frac{y'}{f'} = \frac{y}{z}$$



Magnification:

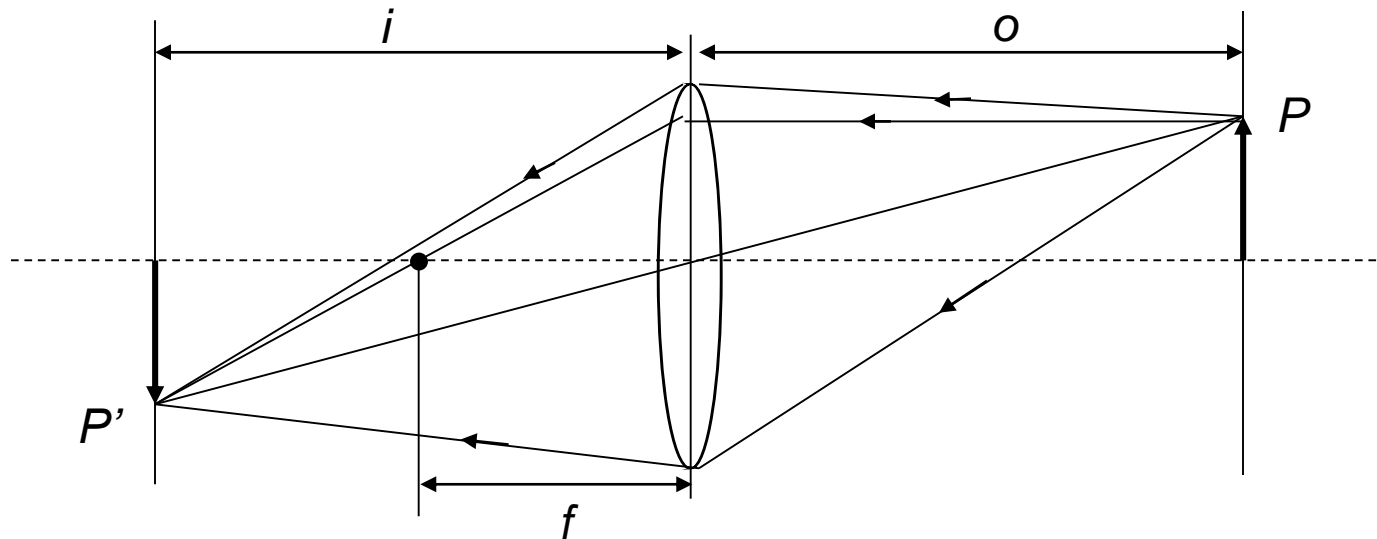
$$m = \frac{d'}{d} = \frac{\sqrt{(\delta x')^2 + (\delta y')^2}}{\sqrt{(\delta x)^2 + (\delta y)^2}} = \frac{f'}{z}$$

$$\frac{x' + \delta x'}{f'} = \frac{x + \delta x}{z} \quad \frac{y' + \delta y'}{f'} = \frac{y + \delta y}{z}$$

$$\frac{Area_{image}}{Area_{scene}} = m^2$$

# Image Formation using Lenses

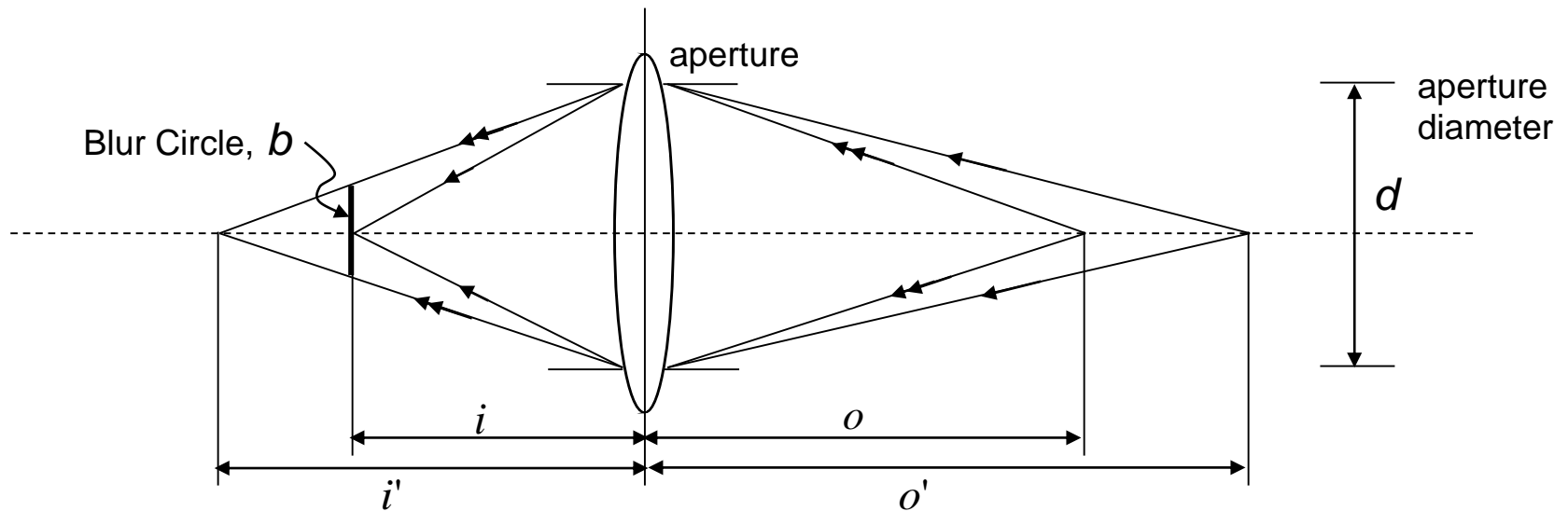
- Lenses are used to avoid problems with pinholes.
- Ideal Lens: Same projection as pinhole but gathers more light!



- Gaussian Thin Lens Formula:  $\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$
- $f$  is the focal length of the lens – determines the lens's ability to refract light



# Focus and Defocus



- Gaussian Law:

$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$$



$$(i' - i) = \frac{f}{(o' - f)} \frac{f}{(o - f)} (o - o')$$

$$\frac{1}{i'} + \frac{1}{o'} = \frac{1}{f}$$

- In theory, only one scene plane is in focus.

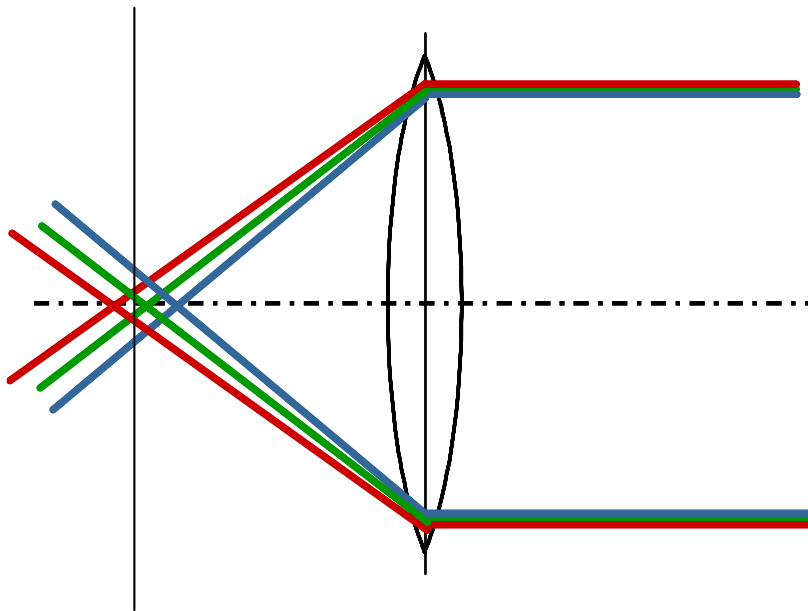
# Depth of Field

- Range of object distances over which image is sufficiently well focused.
- Range for which *blur circle* is less than the resolution of the sensor.

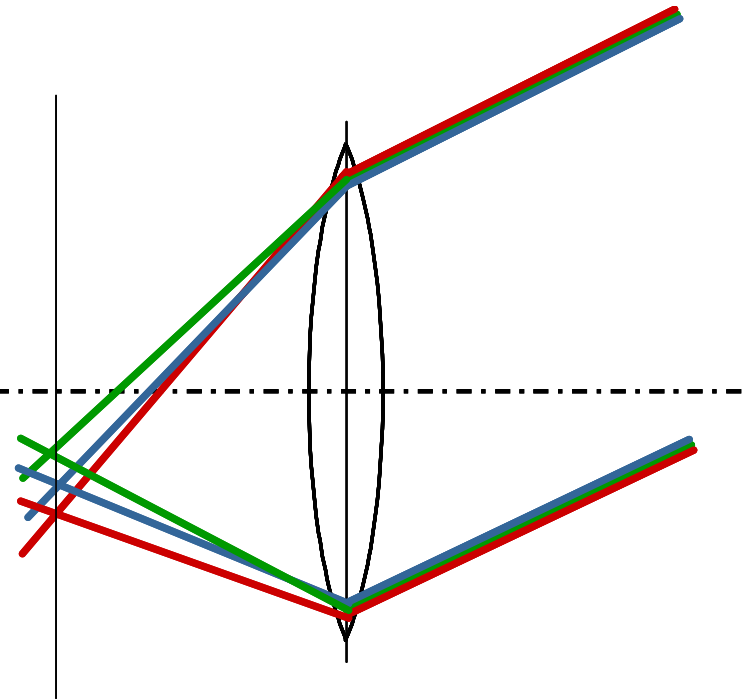


[http://images.dpchallenge.com/images\\_portfolio/27920/print\\_preview/116336.jpg](http://images.dpchallenge.com/images_portfolio/27920/print_preview/116336.jpg)

# Chromatic Aberration



longitudinal chromatic aberration  
(axial)



transverse chromatic aberration  
(lateral)

# Image Sensors

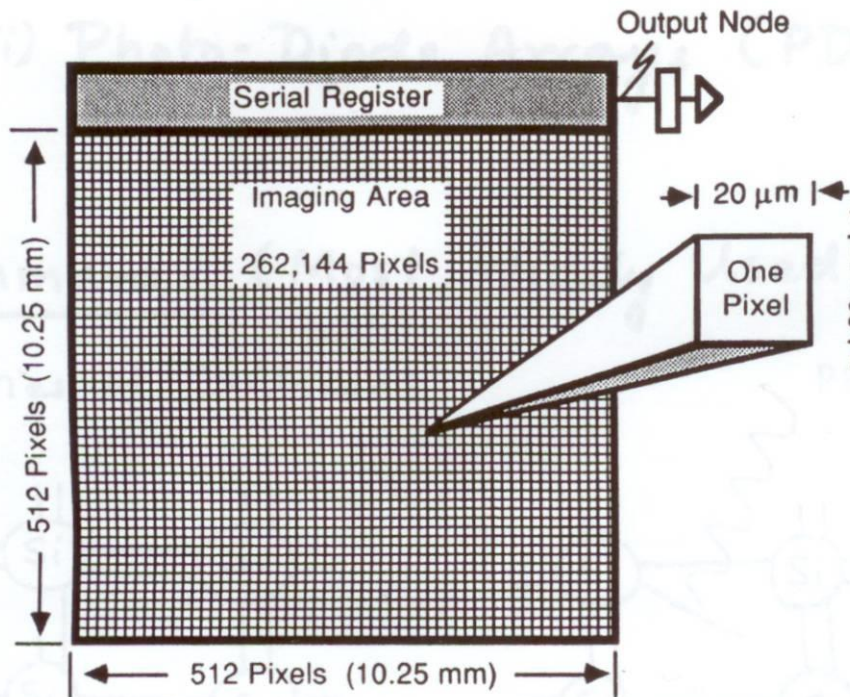


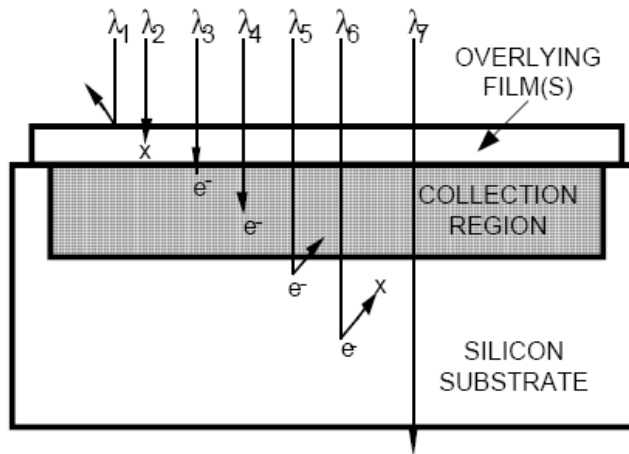
FIG. 4. Typical 512 × 512 CCD.

## Considerations

- Speed
- Resolution
- Signal / Noise Ratio
- Cost

# Image Sensors

- Convert light into an electric charge

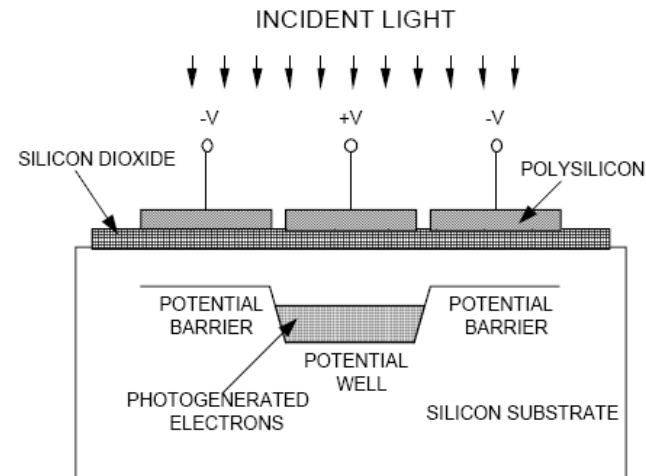
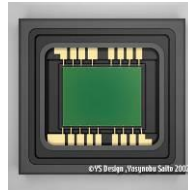


CCD (charge coupled device)

Higher dynamic range

High uniformity

Lower noise

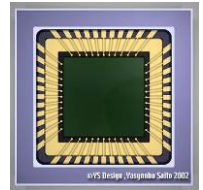


CMOS (complementary metal  
Oxide semiconductor)

Lower voltage

Higher speed

Lower system complexity

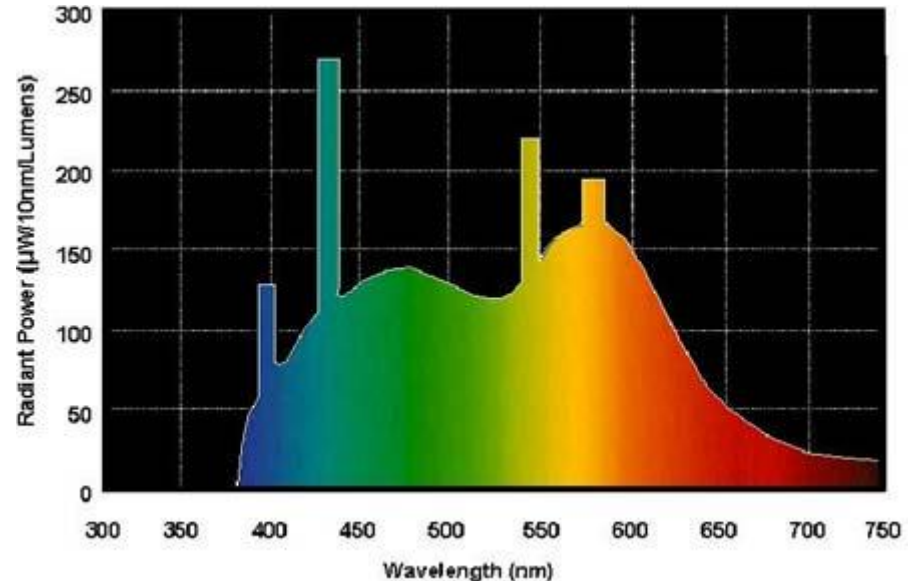
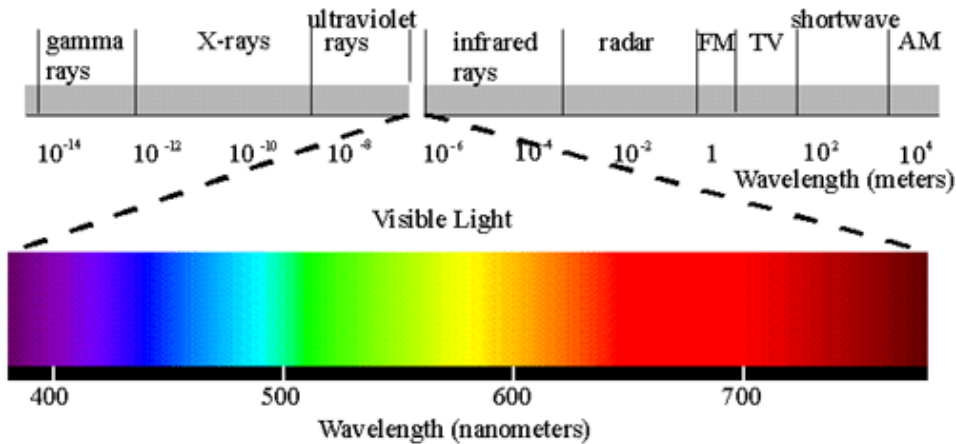


# CCD Performance Characteristics

- Linearity Principle: Incoming photon flux vs. Output Signal
  - Sometimes cameras are made non-linear on purpose.
  - Calibration must be done (using reflectance charts)---covered later
- Dark Current Noise: Non-zero output signal when incoming light is zero
- Sensitivity: Minimum detectable signal produced by camera

# Sensing Brightness

Incoming light has a spectral distribution  $p(\lambda)$

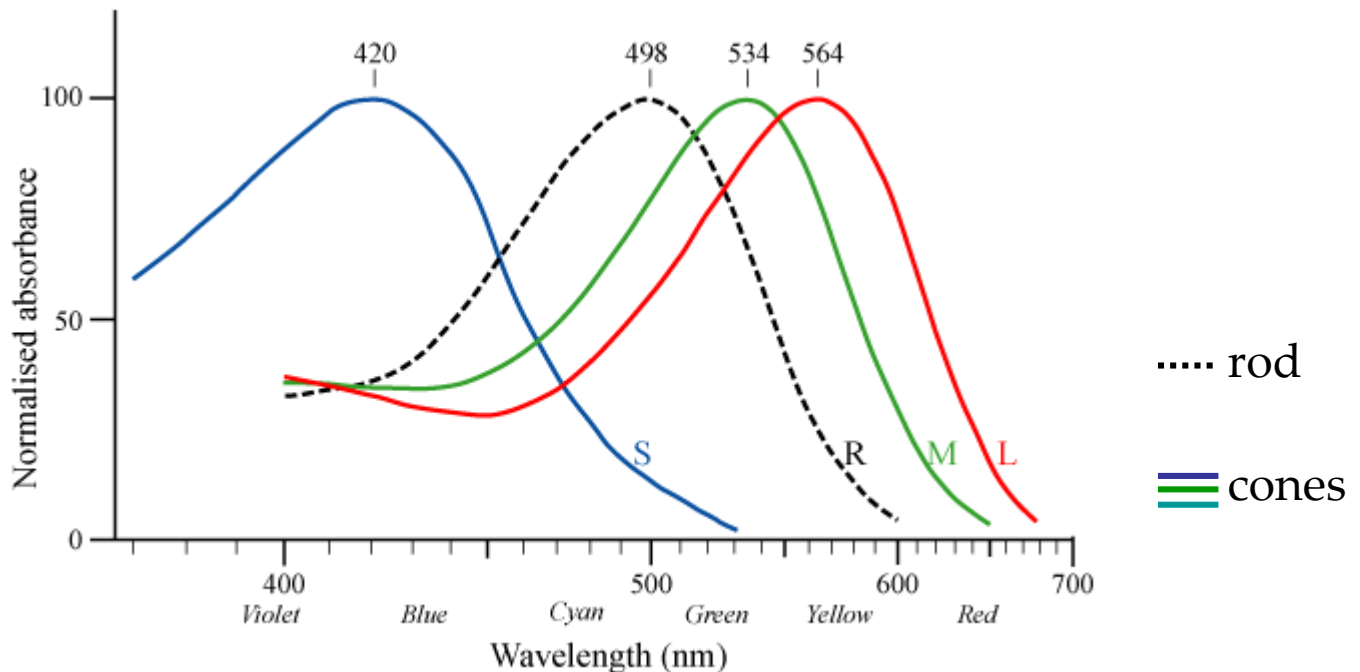


So the pixel intensity becomes

$$I = k \int_{-\infty}^{\infty} q(\lambda)p(\lambda)d\lambda$$

# How do we sense colour?

- Do we have infinite number of filters?



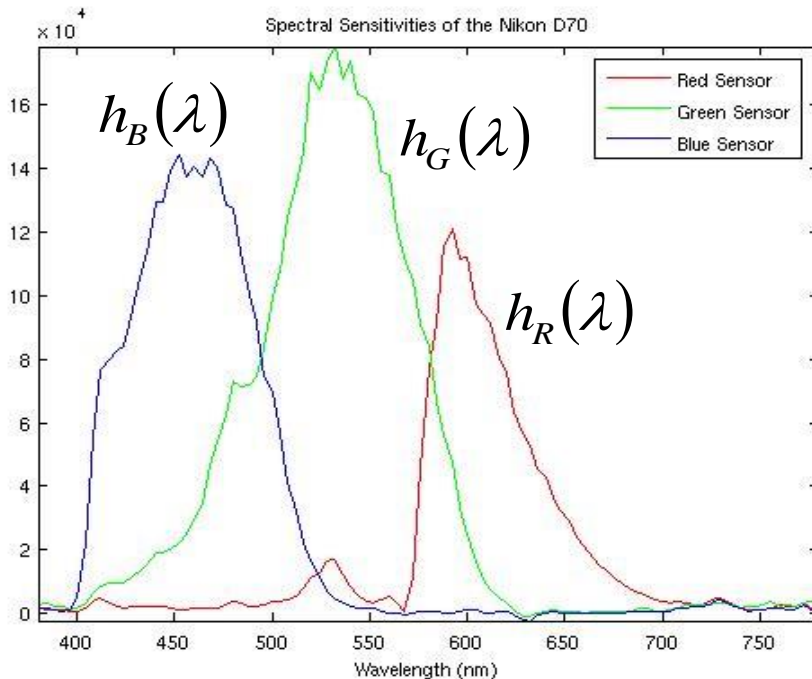
Three filters of different spectral responses



# Sensing Colour

- **Tristimulus (trichromatic) values**  $(I_R, I_G, I_B)$

Camera's spectral response functions:  $h_R(\lambda), h_G(\lambda), h_B(\lambda)$

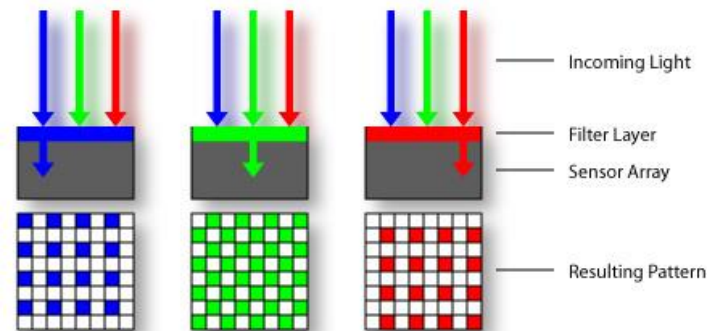
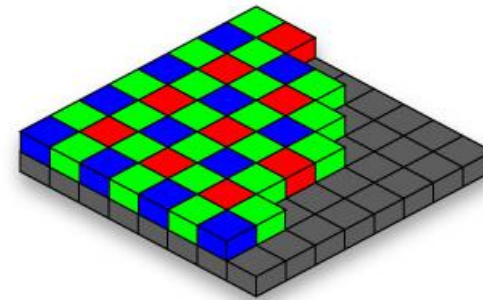
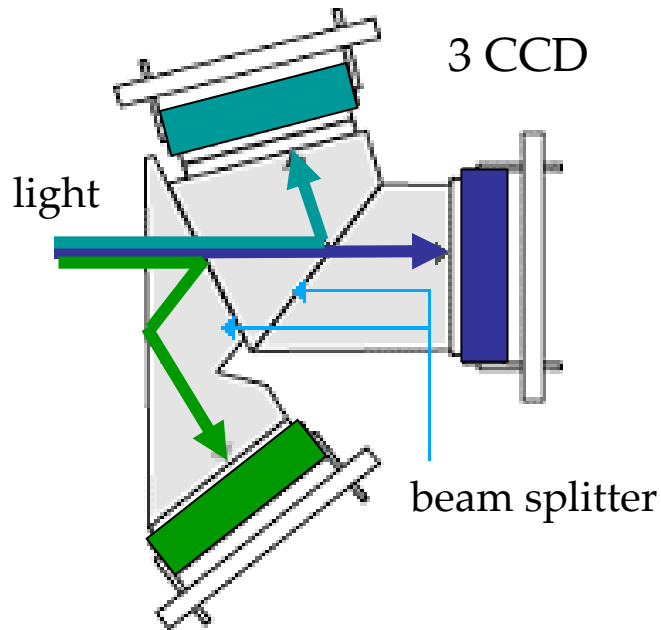


$$I_R = k \int_{-\infty}^{\infty} h_R(\lambda) p(\lambda) d\lambda$$

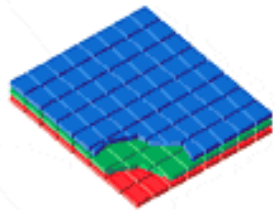
$$I_G = k \int_{-\infty}^{\infty} h_G(\lambda) p(\lambda) d\lambda$$

$$I_B = k \int_{-\infty}^{\infty} h_B(\lambda) p(\lambda) d\lambda$$

# Sensing Colour



Bayer pattern



Foveon X3™

# Resources

- “Color Vision: One of Nature's Wonders” in <http://www.diycalculator.com/sp-cvision.shtml>