

# Computer Vision – TP2

## Digital Images

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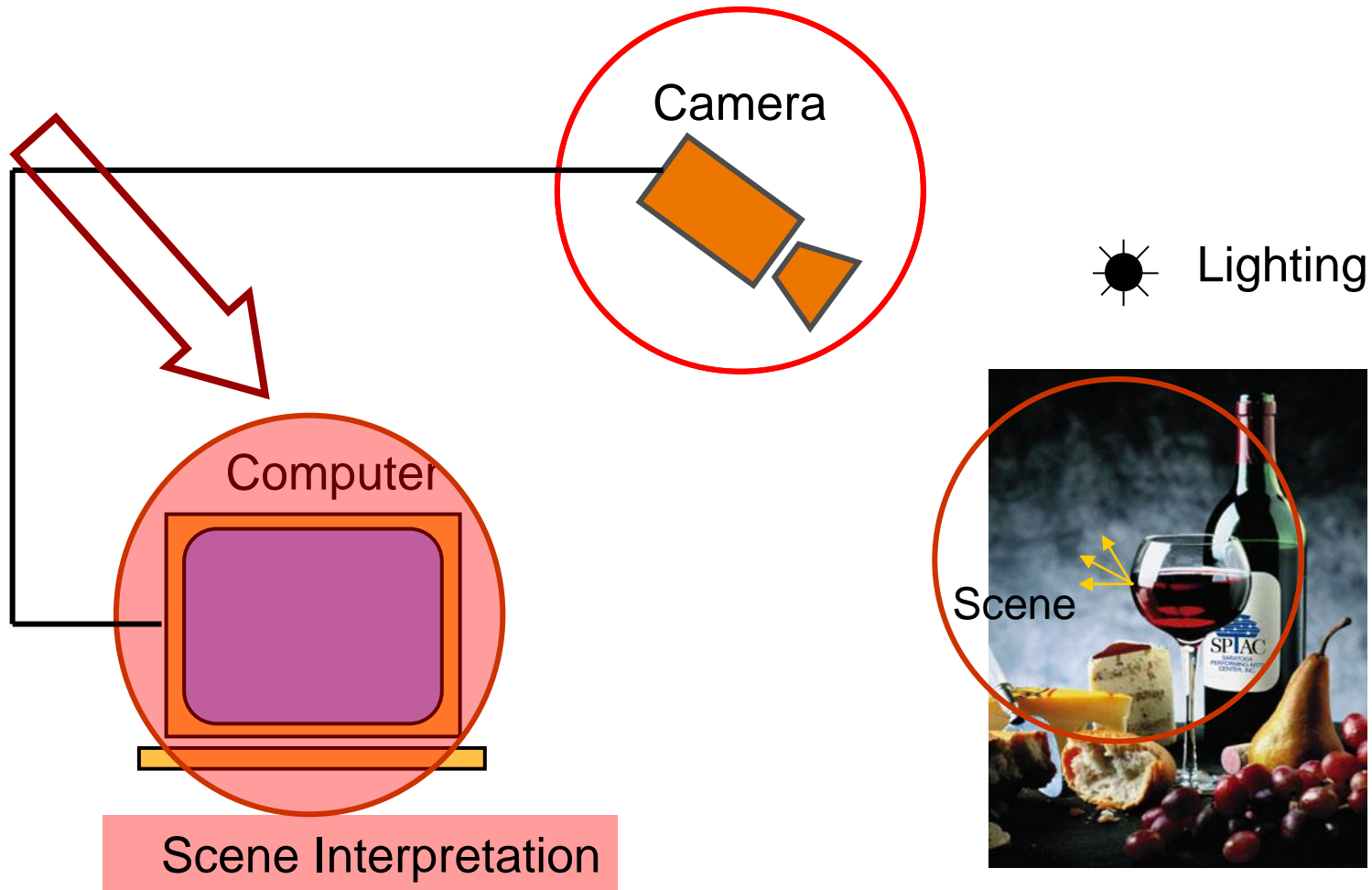
# Outline

- Sampling and quantization
- Data structures for digital images

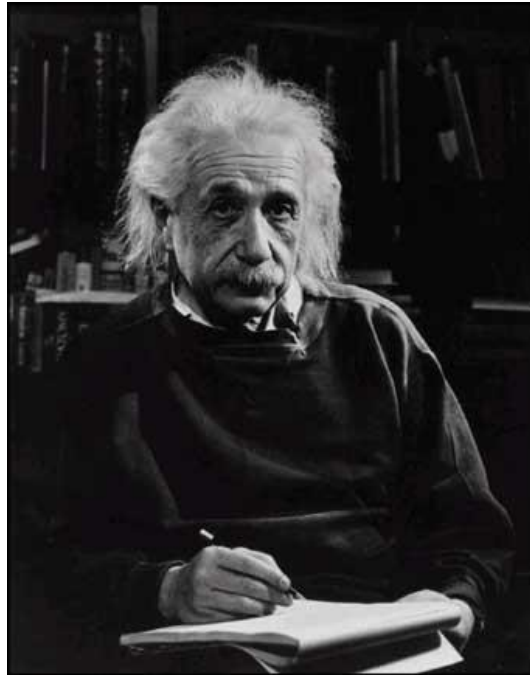
# Topic: Sampling and quantization

- Sampling and quantization
- Data structures for digital images

# Components of a Computer Vision System



# Digital Images

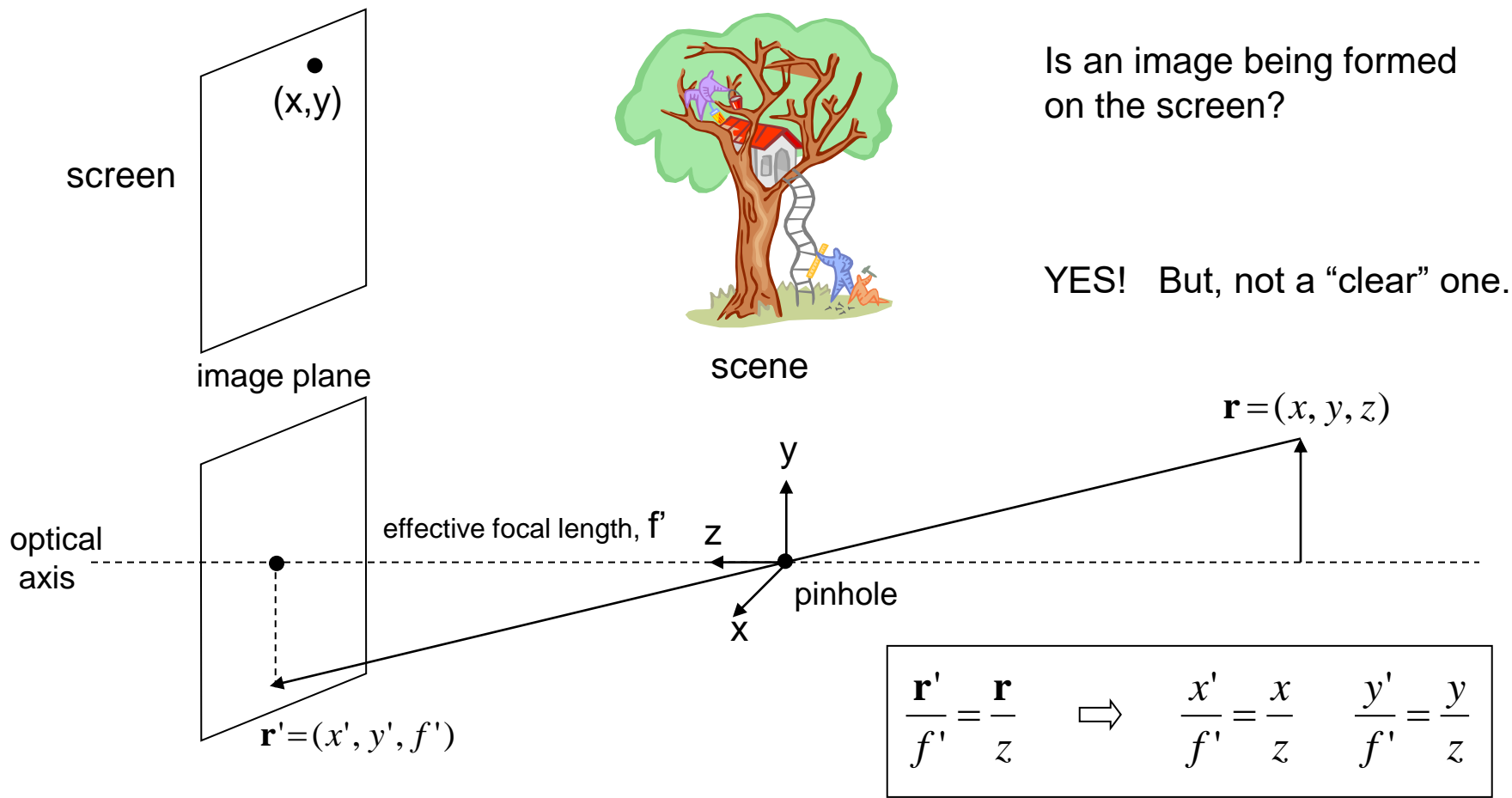


What we see

0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

What a computer sees

# Pinhole and the Perspective Projection



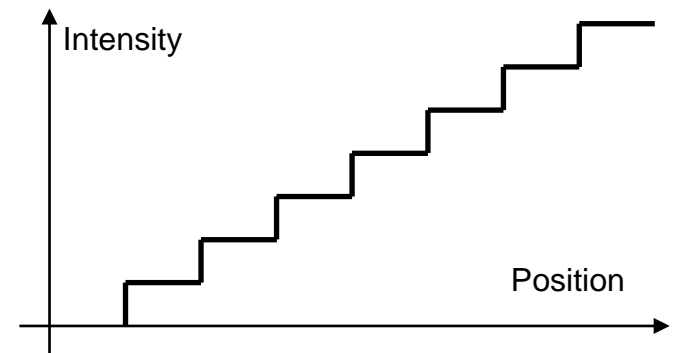
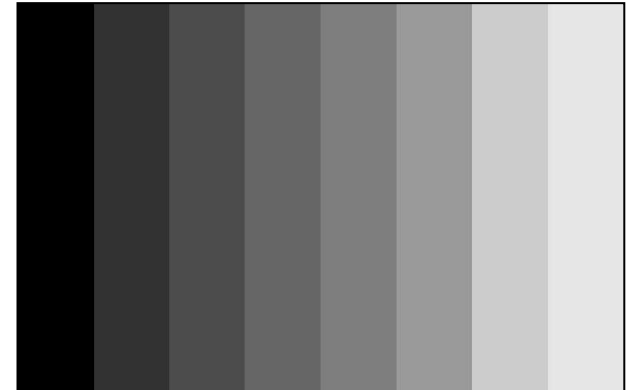
# Simple Image Model

- Image as a 2D light-intensity function

$$f(x, y)$$

- Continuous
- Non-zero, finite value

$$0 < f(x, y) < \infty$$

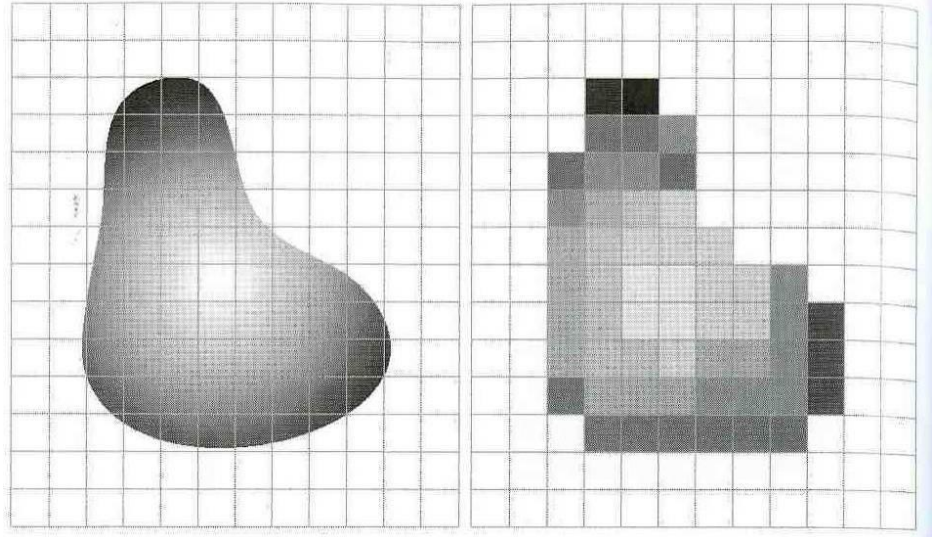


[Gonzalez & Woods]

# Analog to Digital

The scene is:

- **projected** on a 2D plane,
- **sampled** on a regular grid, and each sample is
- **quantized** (rounded to the nearest integer)



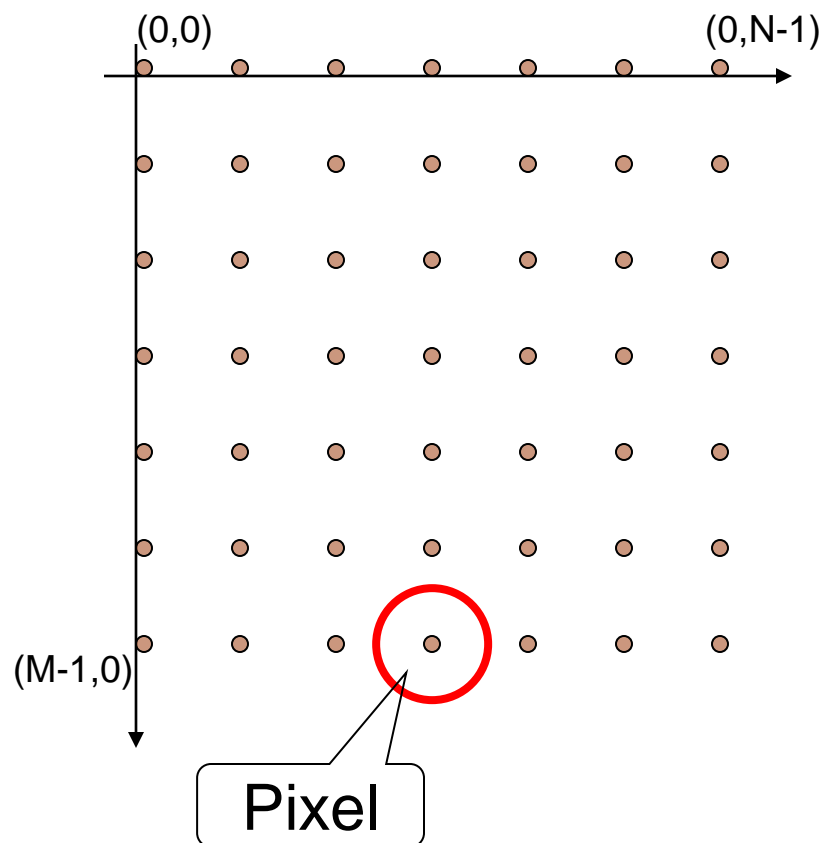
$$f(i, j) = \text{Quantize}\{f(i\Delta, j\Delta)\}$$



# Images as Matrices

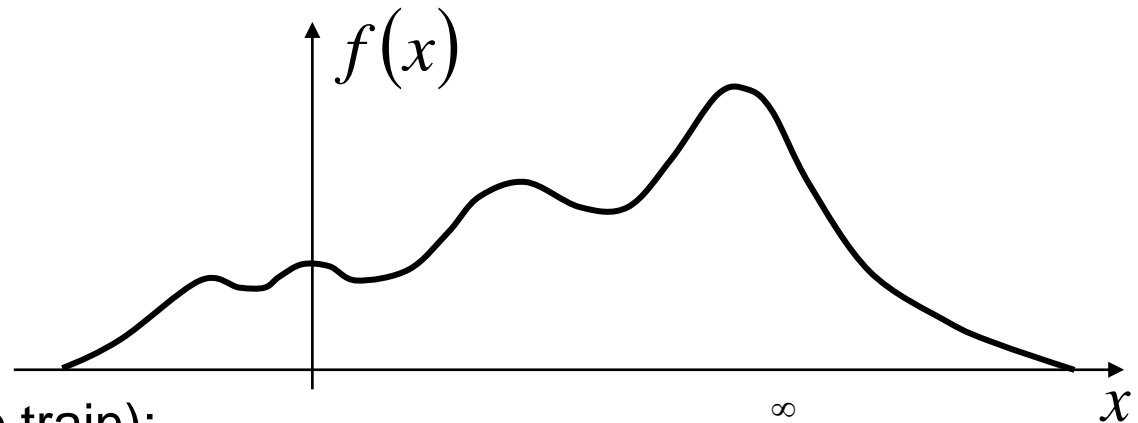
- Each point is a **pixel** with amplitude:
  - $f(x,y)$
- An image is a matrix with size  $N \times M$

$$M = \begin{bmatrix} (0,0) & (0,1) & \dots \\ (1,0) & (1,1) & \dots \\ \dots & & \dots \end{bmatrix}$$

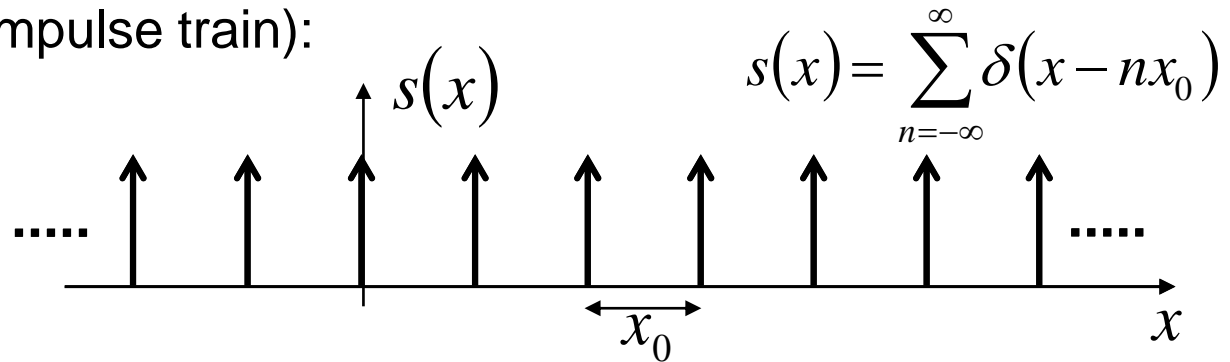


# Sampling Theorem

Continuous signal:



Shah function (Impulse train):



Sampled function:

$$f_s(x) = f(x)s(x) = f(x) \sum_{n=-\infty}^{\infty} \delta(x - nx_0)$$

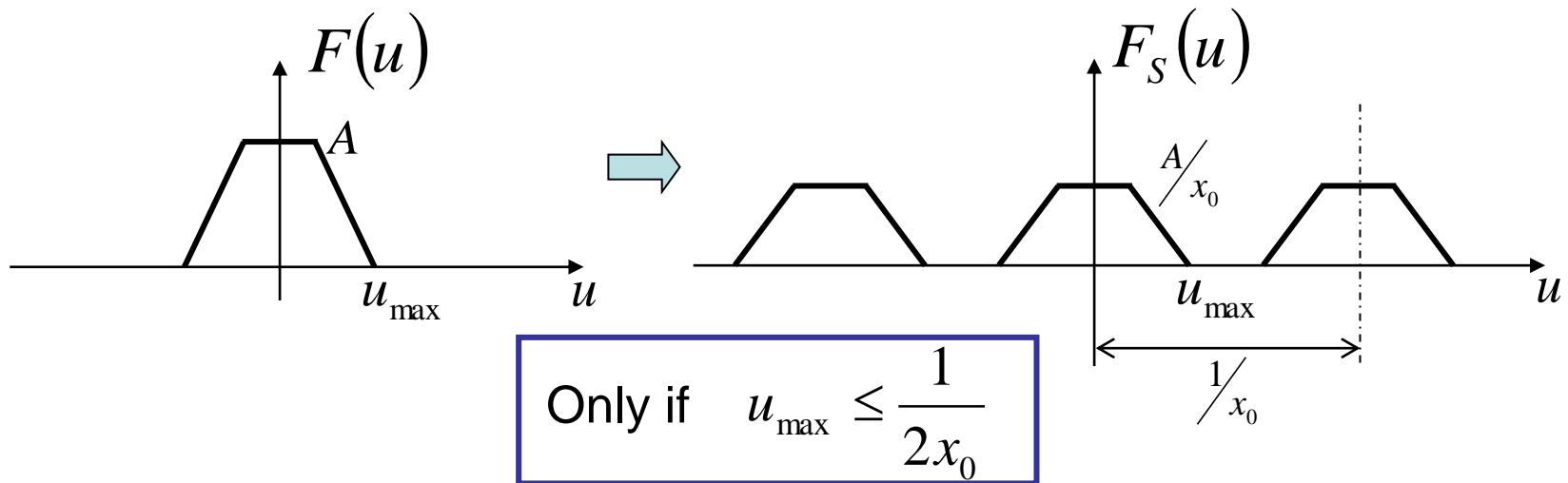
# Sampling Theorem

Sampled function:

$$f_s(x) = f(x)s(x) = f(x) \sum_{n=-\infty}^{\infty} \delta(x - nx_0)$$

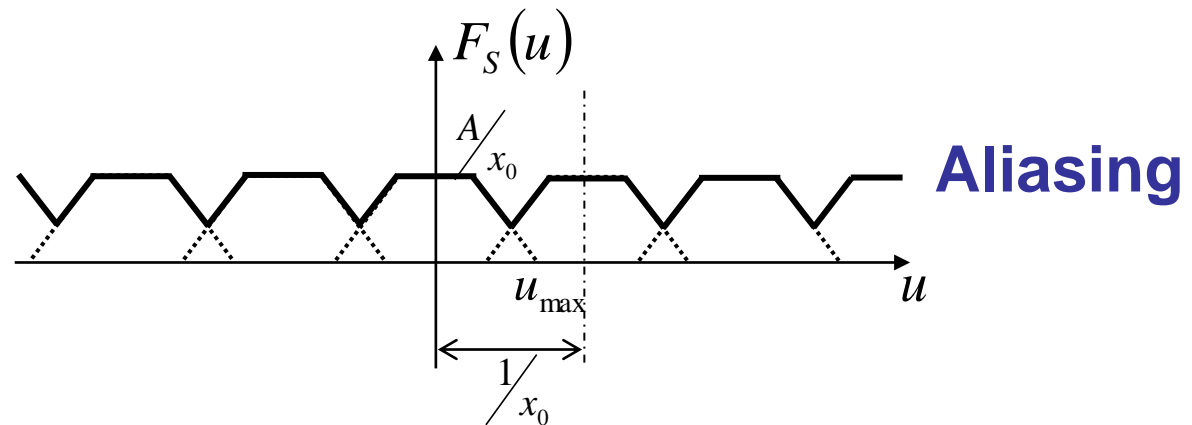
Sampling frequency  $\frac{1}{x_0}$

$$F_S(u) = F(u) * S(u) = F(u) * \frac{1}{x_0} \sum_{n=-\infty}^{\infty} \delta\left(u - \frac{n}{x_0}\right)$$



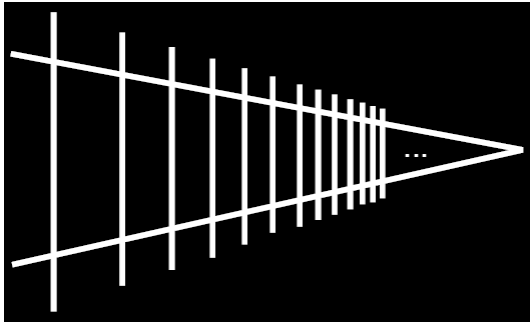
# Nyquist Theorem

If  $u_{\max} > \frac{1}{2x_0}$



Sampling frequency must be greater than  $2u_{\max}$

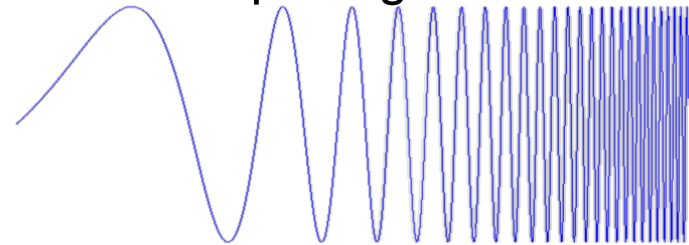
# Aliasing



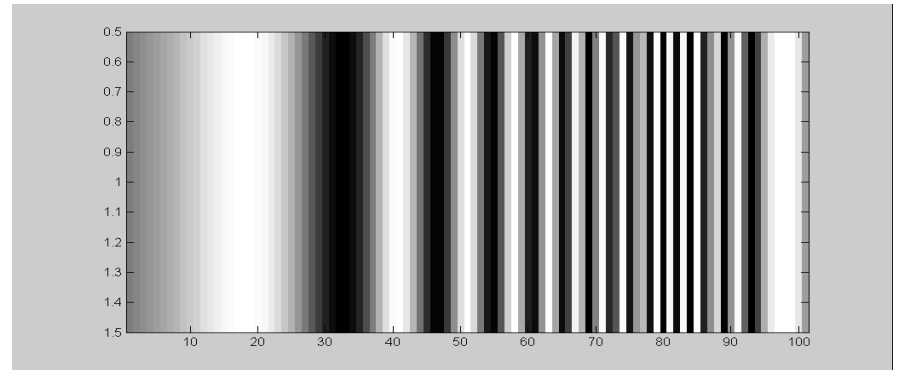
Picket fence receding into the distance will produce aliasing...

WHY?

Input signal:



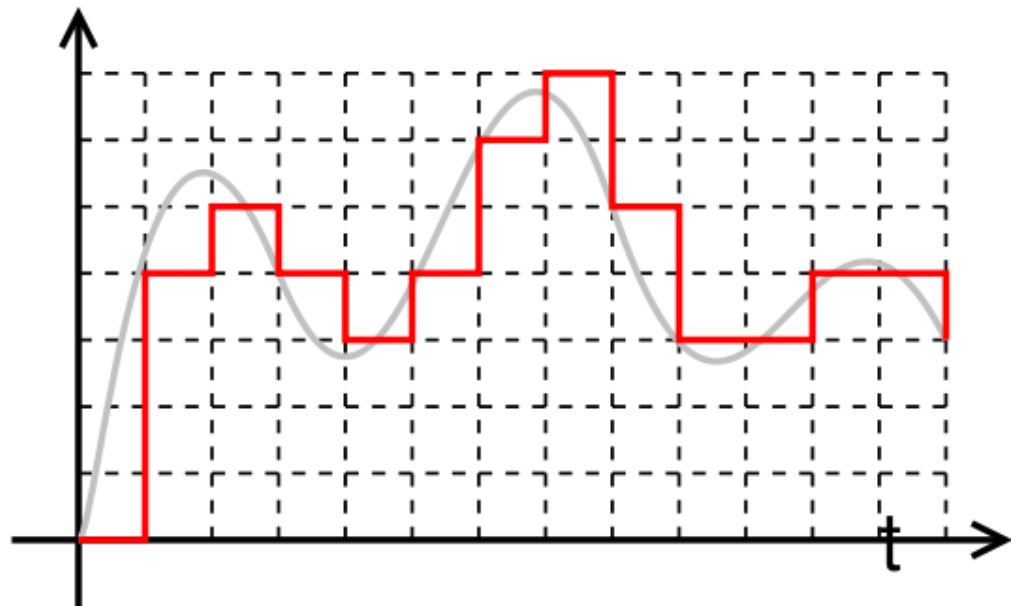
Matlab output:



```
x = 0:.05:5; imagesc(sin((2.^x).*x))
```

# Quantization

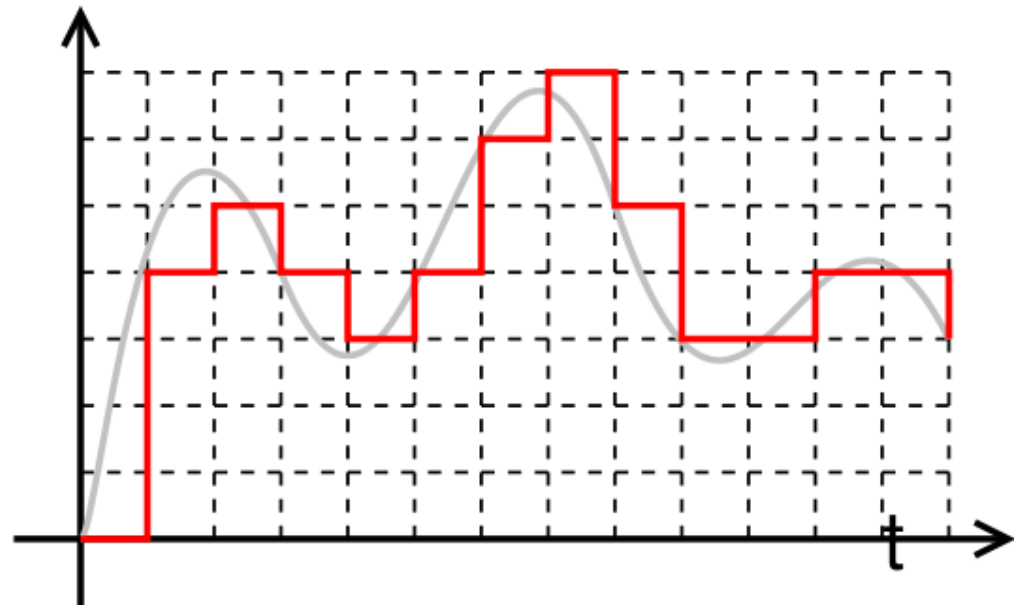
- Analog:  $0 < f(x, y) < \infty$
- Digital: Infinite storage space per pixel!
- Quantization



# Quantization Levels

- $G$  - number of levels
- $m$  – storage bits
- Round each value to its nearest level

$$G = 2^m$$



# Effect of quantization





# Effect of quantization



# Image Size

- Storage space

- Spatial resolution:  $N \times M$
- Quantization:  $m$  bits per pixel
- Required bits  $b$ :

$$b = N \times M \times m$$

- Rule of thumb:

- More storage space means more image quality

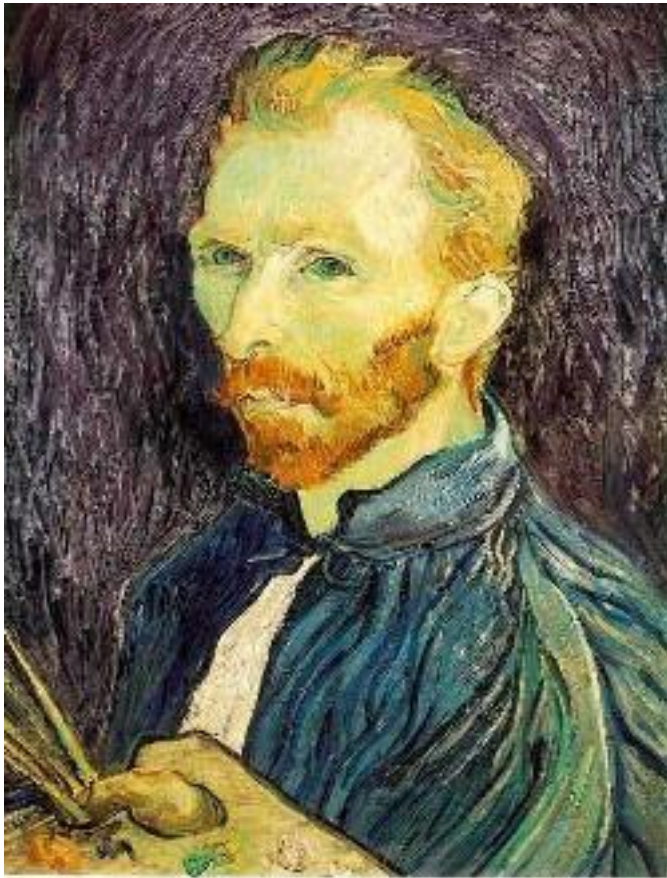
# Image Scaling

This image is too big to fit on the screen. How can we reduce it?

How to generate a half-sized version?



# Sub-sampling



1/4

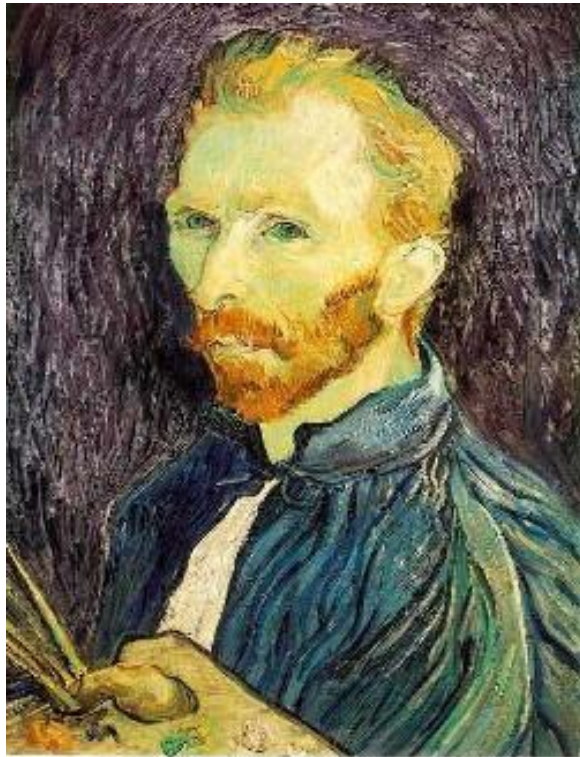


1/8

Throw away every other row and column to create a 1/2 size image - called *image sub-sampling*



# Sub-sampling



1/2



1/4 (2x zoom)



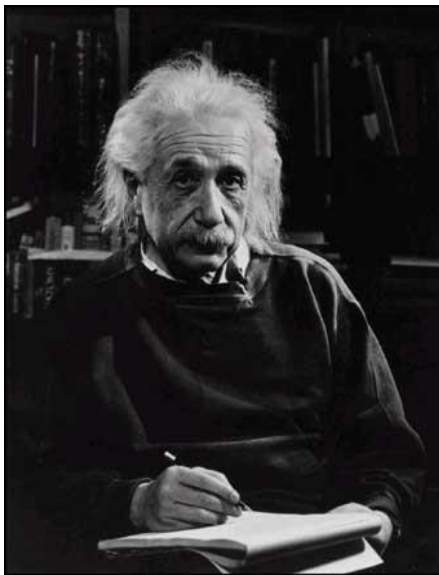
1/8 (4x zoom)

# Topic: Data structures for digital images

- Sampling and quantization
- **Data structures for digital images**

# Data Structures for Digital Images

- Are there other ways to represent digital images?



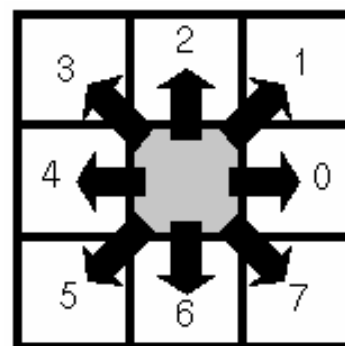
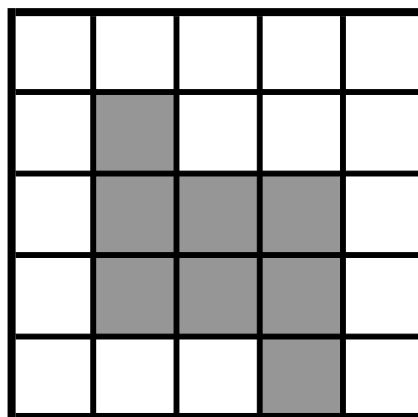
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7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

What a computer sees

# Chain codes

- Chains represent the borders of objects.
- Coding with *chain codes*.
  - Relative.
  - Assume an initial starting point for each object.
- Needs segmentation!



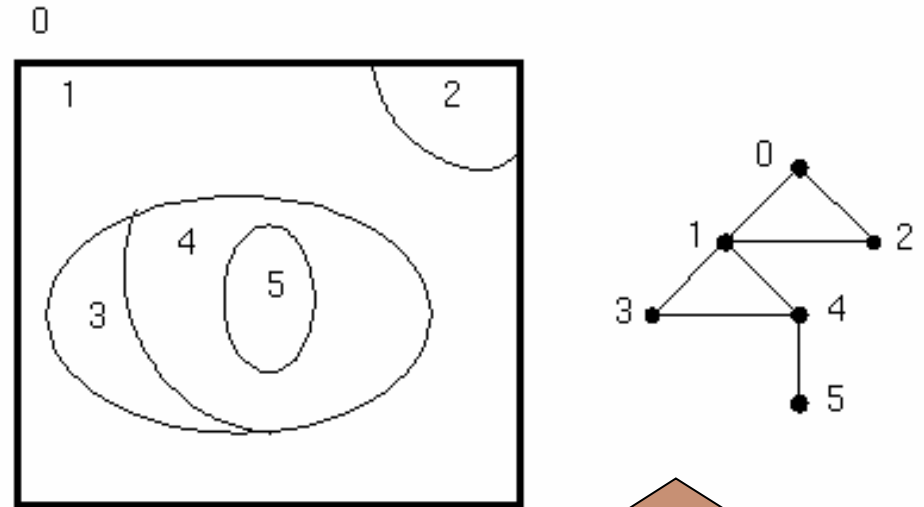
Freeman Chain Code

Using a Freeman Chain Code and considering the top-left pixel as the starting point:  
70663422



# Topological Data Structures

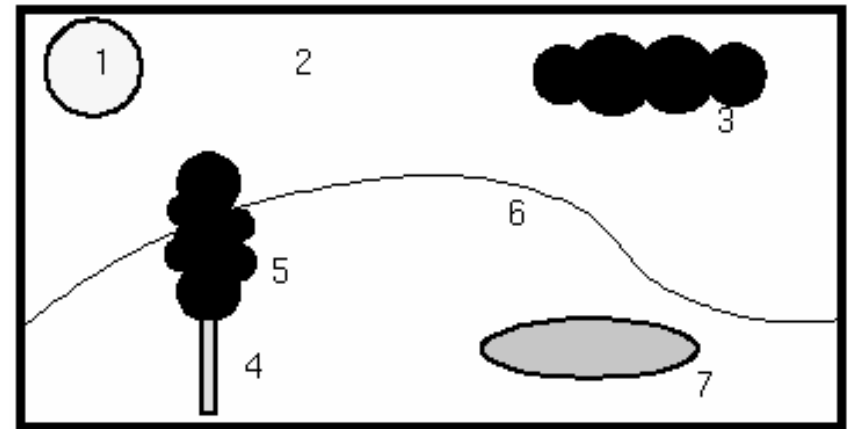
- *Region Adjacency Graph*
  - **Nodes** - Regions
  - **Arcs** – Relationships
- Describes the elements of an image and their spatial relationships.
- Needs segmentation!



*Region Adjacency Graph*

# Relational Structures

- Stores **relations** between **objects**.
- Important **semantic information** of an image.
- Needs **segmentation** and an image description (**features**)!



No.	Object name	Colour	Min. row	Min. col.	Inside
1	sun	white	5	40	2
2	sky	blue	0	0	-
3	cloud	grey	20	180	2
4	tree trunk	brown	95	75	6
5	tree crown	green	53	63	-
6	hill	light green	97	0	-
7	pond	blue	100	160	6

*Relational Table*

# Resources

- Szeliski, “Computer Vision: Algorithms and Applications”, Springer, 2011
  - Chapter 2 – “Image Formation”