# VC 18/19 - TP9 <br> Region-Based Segmentation 

Mestrado em Ciência de Computadores
Mestrado Integrado em Engenharia de Redes e Sistemas Informáticos

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## Outline

- Region-based Segmentation
- Morphological Filters


## Topic: Region-based Segmentation

- Region-based Segmentation
- Morphological Filters


## Why Region-Based Segmentation?

- Segmentation
- Edge detection and Thresholding not always effective.
- Homogenous regions
- Region-based segmentation.
- Effective in noisy images.



## Definitions

- Based on sets.
- Each image $R$ is a set of regions $R_{i}$.
- Every pixel belongs to one region.
- One pixel can only belong to a single region.


$$
R=\bigcup_{i=1}^{S} R_{i} \quad R_{i} \bigcap R_{j}=\varnothing
$$



## Basic Formulation

Let R represent the entire image region. Segmentation partitions $R$ into $n$ subregions, $R_{1}, R_{2}, \ldots, R_{n}$, such that:
a) $\bigcup_{i=1}^{n} R_{i}=R$
b) $\quad R_{i}$ is a connected region, $i=1,2, \ldots, n$.
c) $\quad R_{i} \cap R_{j}=\phi$ for all $i$ and $j, i \neq j$
d) $\quad P\left(R_{i}\right)=$ TRUE for $i=1,2, \ldots, n$.
e) $\quad P\left(R_{i} \cup R_{j}\right)=F A L S E$ for $i \neq j$.
a) Every pixel must be in a region
b) Points in a region must be connected.
c) Regions must be disjoint.
d) All pixels in a region satisfy specific properties.
e) Different regions have different properties.

F

## How do we form regions?

- Region Growing
- Region Merging
- Region Splitting
- Split and Merge
- Watershed


What a computer sees

## Region growing

- Groups pixels into larger regions.
- Starts with a seed region.
- Grows region by merging neighboring pixels.
- Iterative process
- How to start?
- How to iterate?
- When to stop?

- Seed Fixel
$\uparrow$ Direction of Growth
(a) Start of Growing a Region

- Gown Fivels
* Fixels Being

Considered
(b) Growing Process After a Few Iterations

## Region merging

- Algorithm
- Divide image into an initial set of regions.
- One region per pixel.
- Define a similarity criteria for merging regions.
- Merge similar regions.
- Repeat previous step until no more merge operations are possible.


## Similarity Criteria

- Homogeneity of regions is used as the main segmentation criterion in region growing.
- gray level
- color, texture
- shape

- model
- etc.


## Gray-Level Criteria

- Comparing to Original Seed Pixel - Very sensitive to choice of seed point.
- Comparing to Neighbor in Region
- Allows gradual changes in the region.
- Can cause significant drift.
- Comparing to Region Statistics
- Acts as a drift dampener.
- Other possibilities!


## Region splitting

- Algorithm
- One initial set that includes the whole image.

- Similarity criteria.
- Iteratively split regions into sub-regions.
- Stop when no more splittings are possible.


The segmentation problem


Figure 5.23 A quad-tree representation of an $8 \times 8$ binary image.
[Machine Vision; David Vernon]

## Split and Merge

- Combination of both algorithms.
- Can handle a larger variety of shapes.
- Simply apply previous algorithms consecutively.



## The Watershed Transform

- Geographical inspiration.
- Shed water over rugged terrain.
- Each lake corresponds to a region.
- Characteristics
- Computationally complex.
- Great flexibility in segmentation.
- Risk of over-segmentation.



## The Drainage Analogy

## - Two points are in the same region if they drain to the same point.



Courtesy of Dr. Peter Yim at National Institutes of Health, Bethesda, MD

## The Immersion Analogy

Catchment


[Milan Sonka, Vaclav Hlavac, and Roger Boyle]

Figure 5.51: Watershed segmentation: (a) original; (b) gradient image, $3 \times 3$ Sobel edge detection, histogram equalized; (c) raw watershed segmentation; (d) watershed segmentation using region markers to control oversegmentation. Courtesy W. Higgins, Penn State University.

## Over-Segmentation

- Over-segmentation.
- Raw watershed segmentation produces a severely oversegmented image with hundreds or thousands of catchment basins.
- Post-Processing.
- Region merging.
- Edge information.
- Etc.


## Topic: Morphological Filters

- Region-based Segmentation
- Morphological Filters


## Mathematical Morphology

- Provides a mathematical description of geometric structures.
- Based on sets.
- Groups of pixels which define an image region.
- What is this used for?
- Binary images.
- Can be used for postprocessing segmentation results!
- Core techniques
- Erosion, Dilation.
- Open, Close.


Tumor Segmentation using Morphologic Filtering

## Dilation, Erosion

- Two sets:
- Image
- Morphological kernel.
- Dilation (D)
- Union of the kernel with the image set.
- Increases resulting area.
- Erosion (E)
- Intersection.
- Decreases resulting area.

$$
\begin{gathered}
D(\mathrm{~A}, \mathrm{~B})=\mathrm{A} \oplus \mathrm{~B}=\bigcup_{\beta \in \mathrm{B}}(\mathrm{~A}+\beta) \\
E(\mathrm{~A}, \mathrm{~B})=\mathrm{A}(-\mathrm{B})=\bigcap_{\beta \in \mathrm{B}}(\mathrm{~A}-\beta) \\
\end{gathered}
$$



## Dilation

## - Example using a $3 \times 3$ morphological kernel

|  | 00 | 0 | 0 | 6 | 6 | ¢ | 0 | 0 | 6 | 0 | 0 | 0 | 00 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 06 | 0 | 0 | 6 | ¢ | ¢ | 0 | Q | 6 | 0 | 0 | 0 | 00 |
| 0 | 00 | 1 | 1 | 1 | 4 | ¢ | 0 | Q | ¢ | 0 | 0 | 0 | 0 0 |
| 0 | 01 | 1 | 1 | 1 | 1 | 6 | 0 | 0 | 0 | 0 | 0 | 0 | 06 |
| 0 | 01 | 1 | 1 | 1 | 1 | ¢ | 0 | 0 | 0 | 1 | 1 |  | 00 |
| 0 | 01 | 1 |  | 1 | 0 | ¢ | 0 | 0 | 1 | 1 | 1 |  | 06 |
| ¢ | 08 | 1 | 1 | 6 | ¢ | 6 | 0 | 1 | 1 | 1 | 1 |  | 60 |
| 0 | 00 | 0 | ¢ | 6 | ¢ | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 00 |
| 0 | 06 | 6 | 0 | Q | Q | 1 | 1 | 1 | 1 |  | 0 |  | 60 |
| ¢ | 06 | ¢ | 0 | 6 | 1 | 1 | 1 | 1 | 1 | ¢ | 0 | 0 | 00 |
|  | 06 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 6 | 0 | ¢ | 0 | 06 |
| ¢ | 06 | 0 | 1 | 1 | 1 | 1 | 1 | 6 | ¢ |  | ¢ | 0 | 06 |
| 0 | 06 | ¢ | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | ¢ | Q | 6 0 |
| ¢ | 06 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 06 |
| 0 | 00 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 06 |
|  | 00 | 0 | 0 | 0 | 4 | 0 | 0 | 0 | Q | 0 | 0 |  | 00 |


|  |  |  |  |  | ¢ | 6 | 0 | ¢ | ¢ | 0 |  | 6 | Q | 0 | 0 | 0 | ) | \% | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 |  | 6 | 1 | 1 | 1 | 1 | 1 | O | 0 | 0 | 9 | 0 | 0 | 6 | 0 |  | ¢ | 6 |
|  | 0 |  | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |  | - | 0 | 6 | 0 | 0 |  |  | 0 |
|  | 0 |  | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |  | ¢ | 1 | 1 | 1 | 1 | 1 |  | 0 |
|  | 0 |  | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | T | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
|  | 0 |  | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | , | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
|  | - |  | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | , | 1 | 1 | 1 | 1 | 1 | 1 |  | 0 |
| - | 0 |  | Q | 1 | 1 | 1 | 1 | 1 | 1 | 1 | , | 1 | 1 | 1 | 1 | 1 |  |  | 0 |
| $\cdots$ | 0 |  | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | , | 1 | 1 | 1 | 1 | 1 | 1 |  | 0 |
|  | 0 |  | 0 | 6 | 0 | 1 | 1 | 1 | 1 | 1 | , | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
|  | 0 |  | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | - | 1 | 1 | 1 | 0 | 0 |  |  | 0 |
|  | 0 |  | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | , | 1 | 1 | 1 | 1 | 0 |  |  | 0 |
|  | 0 |  | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 |  | 1 | 1 | 1 | 1 | 0 | ) | ¢ | 0 |
|  | 0 |  | 0 | Q | 1 | 1 | 1 | 1 | 1 | 1 |  | 1 | 1 | 1 | 1 | 0 | ) | 0 | 0 |
|  | 0 |  | 0 |  | 1 | 1 | 1 | 1 | 1 | 1 |  | 1 | 1 | 1 |  | 0 | ) | 0 | 0 |
|  |  |  | 0 |  | 0 | 1 | 1 | 1 | 1 | 1 |  | 1 | 1 | 1 | 0 | 0 | - |  | 0 |

## Erosion

## - Example using a $3 \times 3$ morphological kernel

|  |  |  |  | 0 | Q | 0 | 0 | 0 | 0 | 0 | 0 | ¢ |  |  | $\square$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | b | 0 | ¢ | - | 0 | 0 | ¢ | 0 | 0 | 0 | ¢ | ¢ | 0 | 0 |
| Q | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |  | 0 |
| ¢ | ¢ | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | Q | 0 | 0 |  |  | 0 |
| ¢ | Q | 1 | 1 | 1 | 1 | 1 | ¢ | ¢ | ¢ | 0 | 1 | 1 | 1 |  | 6 |
| ¢ | 0 | 1 | 1 | 1 | 1 | 0 | 0 | O | 0 | 1 | 1 | 1 | 1 |  | 0 |
| ¢ | 0 | 0 | 1 | 1 | ¢ | ¢ | 0 | ¢ | 1 | 1 | 1 | 1 |  |  | 0 |
| ¢ | 0 | ¢ | 0 | 0 | ¢ | 0 | Q | 1 | 1 | 1 | 1 | 1 | 4 |  | 0 |
| ¢ | Q | ¢ | 0 | ¢ | Q | Q | 1 | 1 | 1 | 1 | 1 | 6 |  |  | \% |
| ¢ | 0 | ¢ | O | 0 | 6 | 1 | 1 | 1 | 1 | 1 | ¢ | 0 | 0 |  | 0 |
| 6 | 0 | ¢ | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | ¢ | 0 |  | 0 |
| ¢ | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 6 | 0 |  | 0 |
| ¢ | 0 | 0 | Q | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 6 | 0 |  | 6 |
| 6 | 0 | ¢ | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |  |  |  | 6 |
| ¢ | 0 | ¢ | Q | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 6 |
| 6 | 0 | ¢ | 0 | 0 | ¢ | \% | Q | Q |  | 6 | Q | ¢ |  | 0 |  |


| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

## Opening, Closing

- Opening
- Erosion, followed by dilation.
- Less destructive than an erosion.

- Adapts image shape to kernel shape.
- Closing
- Dilation, followed by erosion.
- Less destructive than a dilation.
- Tends to close shape irregularities.



## Opening

## - Example using a $3 \times 3$ morphological kernel




## Closing

## - Example using a $3 \times 3$ morphological kernel

| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 |
| 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 1 | 1 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |


$\quad$| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 |
| 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

## Core morphological operators



Dilation


Closing


Erosion


Opening

## Example: Opening




## Example: Closing



## Connected Component Analysis

- Define 'connected'.
- 4 neighbors.
- 8 neighbors.

- Search the image for seed points.
- Recursively obtain all connected points of the seeded region.



## Resources

- Gonzalez \& Woods - Chapter 7 and 8

