VC 11/12 – T3 Digital Images

Mestrado em Ciência de Computadores Mestrado Integrado em Engenharia de Redes e Sistemas Informáticos

Miguel Tavares Coimbra



Outline

- Sampling and quantization
- Data structures for digital images
- Histograms

Acknowledgements: Most of this course is based on the excellent courses offered by Prof. Shree Nayar at Columbia University, USA and by Prof. Srinivasa Narasimhan at CMU, USA. Please acknowledge the original source when reusing these slides for academic purposes.

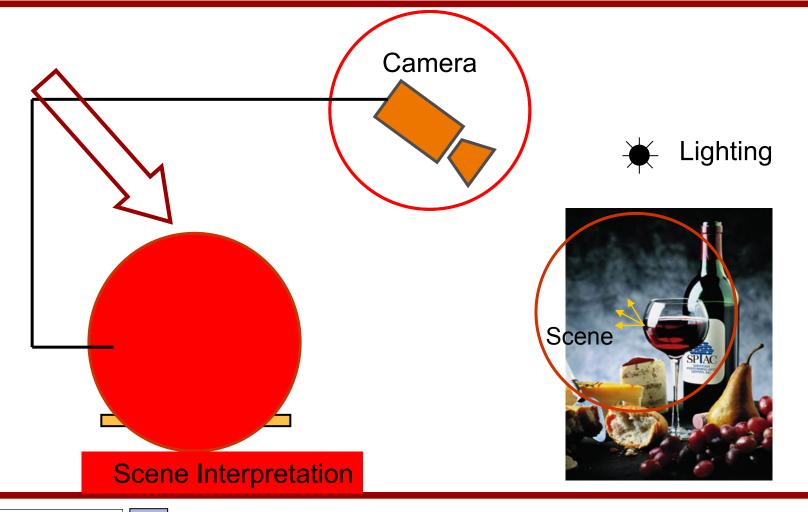


Topic: Sampling and quantization

- Sampling and quantization
- Data structures for digital images
- Histograms

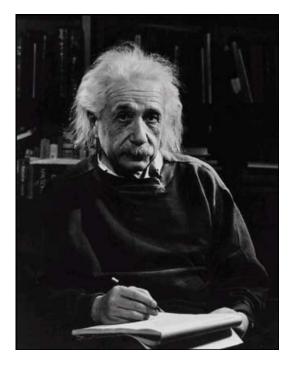


Components of a Computer Vision System

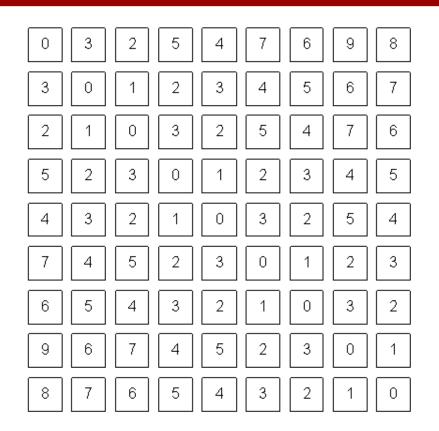


VC 11/12 - T3 - Digital Images

Digital Images



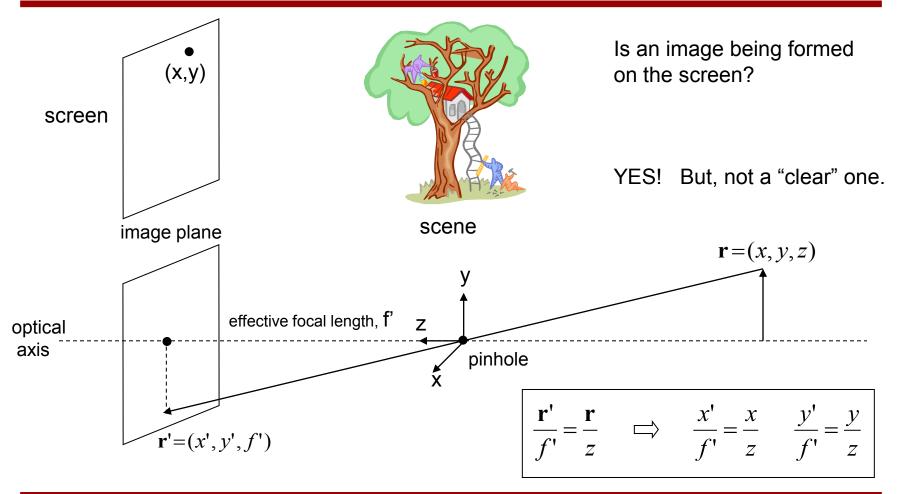
What we see



What a computer sees



Pinhole and the Perspective Projection



VC 11/12 - T3 - Digital Images

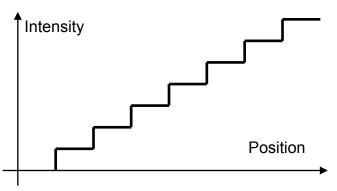
Simple Image Model

 Image as a 2D lightintensity function

f(x,y)

- Continuous
- Non-zero, finite value $0 < f(x, y) < \infty$





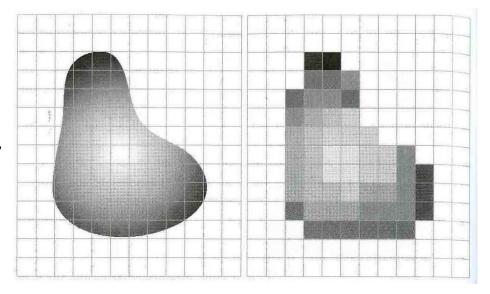
[Gonzalez & Woods]



Analog to Digital

The scene is:

- projected on a 2D plane,
- sampled on a regular grid, and each sample is
- quantized (rounded to the nearest integer)

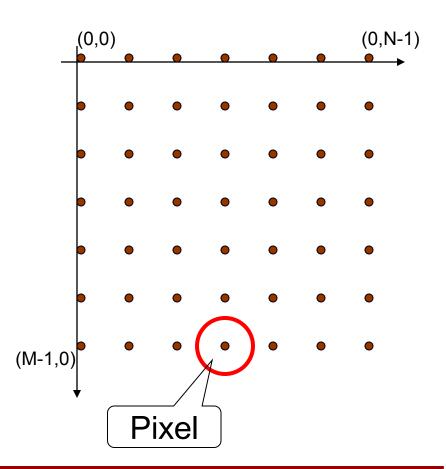


 $f(i, j) = \text{Quantize} \{ f(i\Delta, j\Delta) \}$

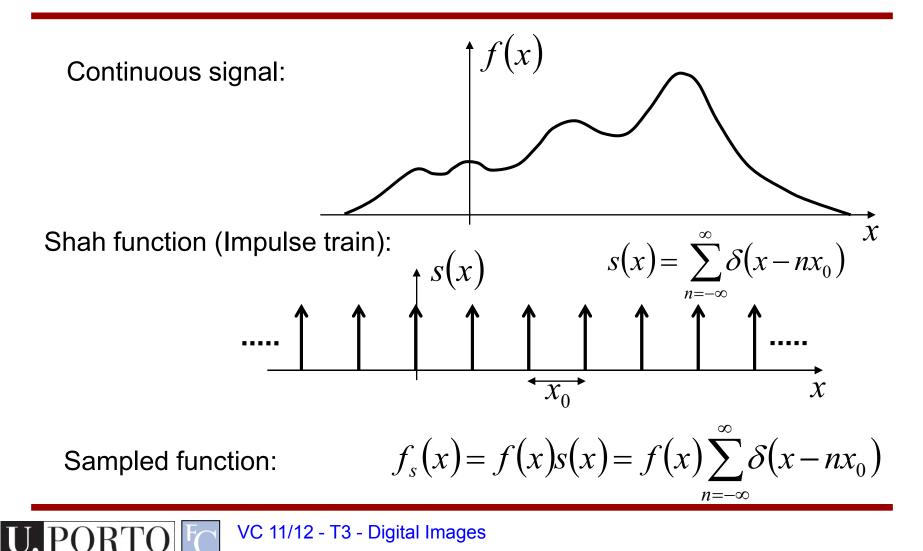
Images as Matrices

- Each point is a pixel with amplitude: – f(x,y)
- An image is a matrix with size N x M
- $M = [(0,0) (0,1) \dots [(1,0) (1,1) \dots$

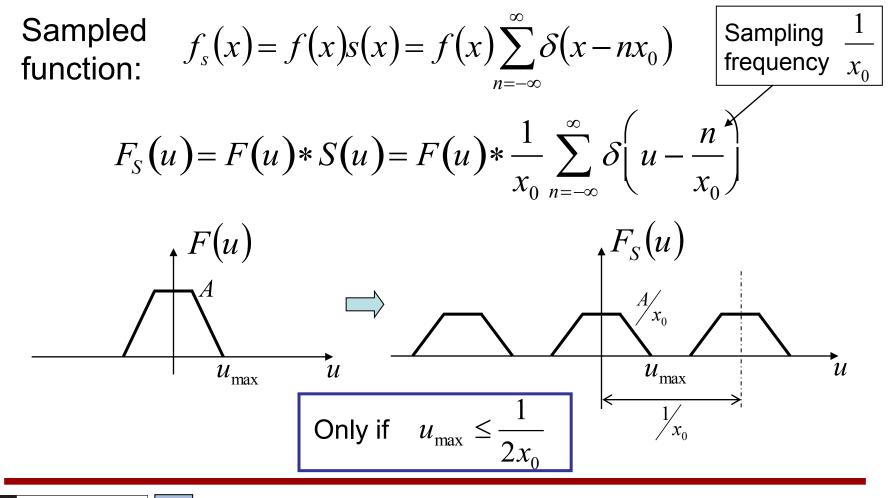
. . .



Sampling Theorem

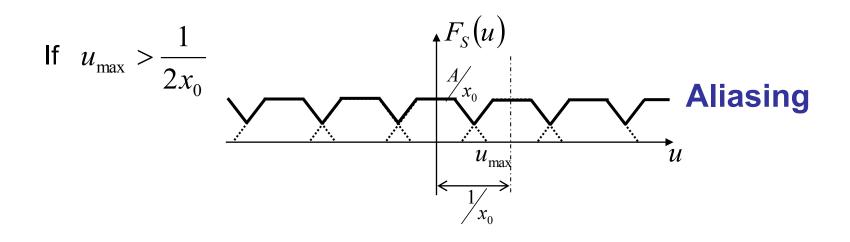


Sampling Theorem



VC 11/12 - T3 - Digital Images

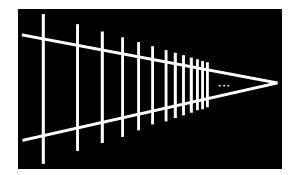
Nyquist Theorem



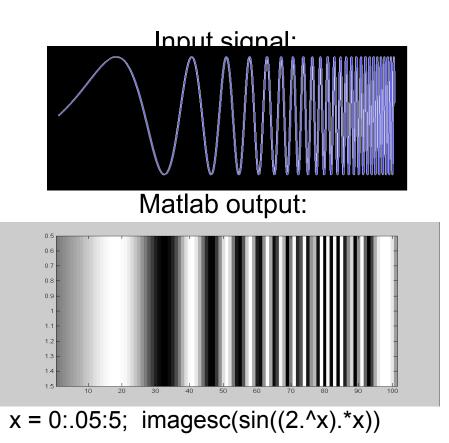
Sampling frequency must be greater than $2u_{\rm max}$



Aliasing



Picket fence receding into the distance will produce aliasing...

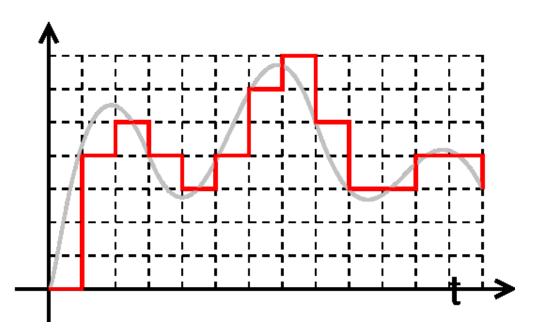


WHY?



Quantization

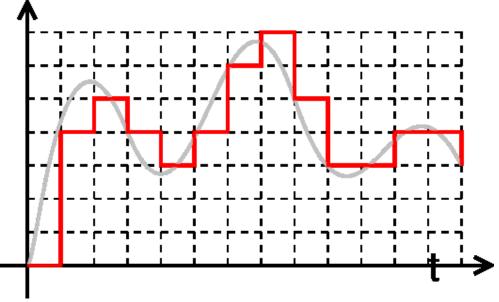
- Analog: $0 < f(x, y) < \infty$
- Digital: Infinite storage space per pixel!
- Quantization



Quantization Levels

- G number of levels
- m storage bits
- Round each value ¹/₁ its nearest level

$$G=2^m$$





Effect of quantization





Effect of quantization





Image Size

- Storage space
 - Spatial resolution: N x M
 - Quantization: m bits per pixel
 - Required bits b:

$$b = N \times M \times m$$

• Rule of thumb:

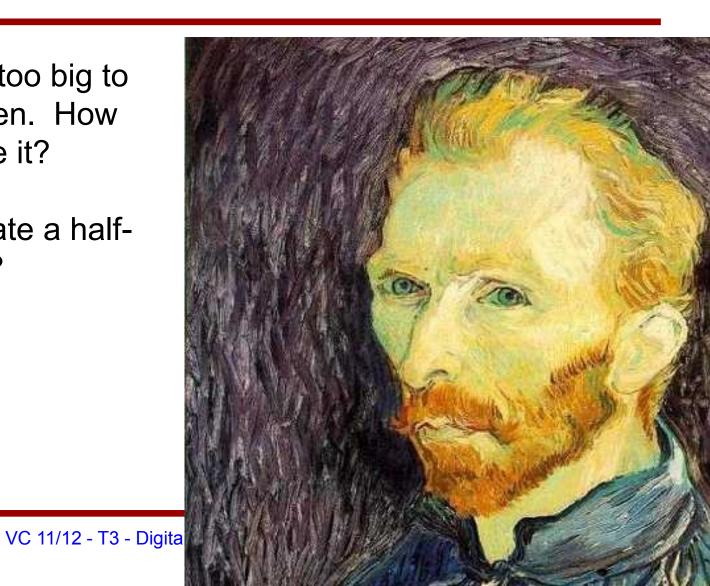
 More storage space means more image quality

Image Scaling

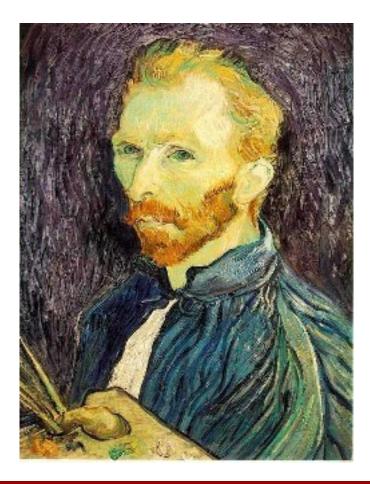
This image is too big to fit on the screen. How can we reduce it?

How to generate a halfsized version?

PORTO FC



Sub-sampling







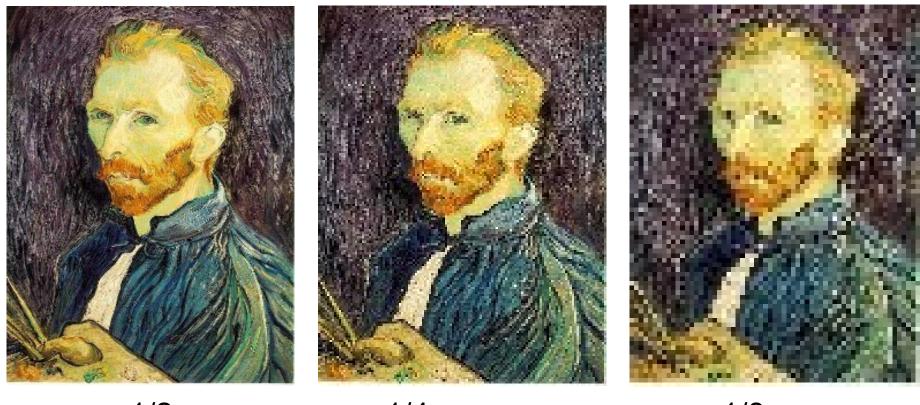
1/8

1/4

Throw away every other row and column to create a 1/2 size image - called *image sub-sampling*



Sub-sampling



1/2

1/4 (2x zoom)

1/8 (4x zoom)

U. PORTO C VC 11/12 - T3 - Digital Images

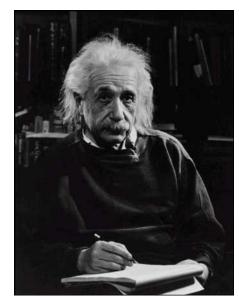
Topic: Data structures for digital images

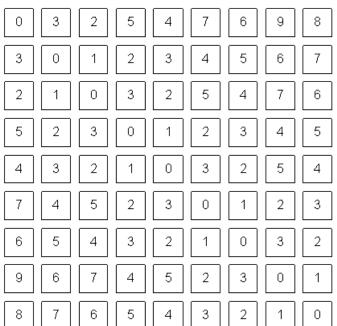
- Sampling and quantization
- Data structures for digital images
- Histograms



Data Structures for Digital Images

Are there other ways to represent digital images?





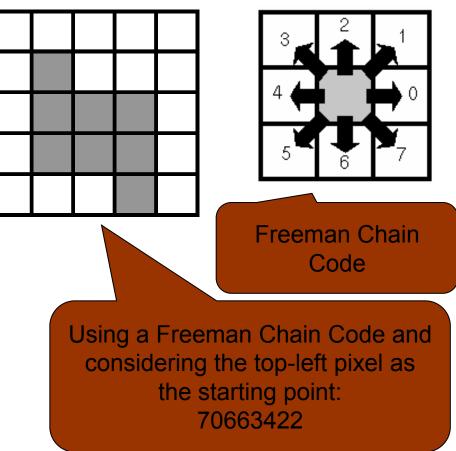
What a computer sees

What we see

VC 11/12 - T3 - Digital Images

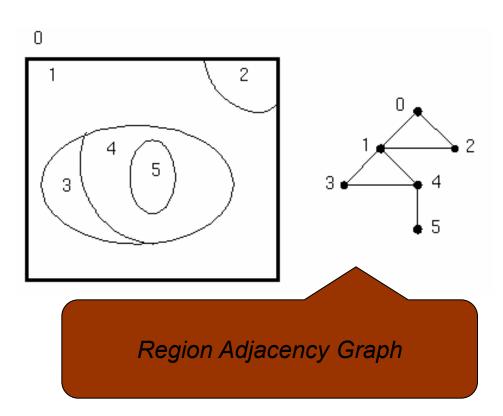
Chain codes

- Chains represent the borders of objects.
- Coding with *chain codes*.
 - Relative.
 - Assume an initial starting point for each object.
- Needs segmentation!



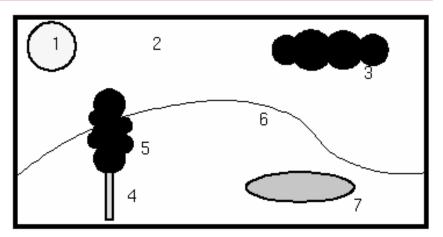
Topological Data Structures

- Region Adjacency
 Graph
 - Nodes Regions
 - Arcs Relationships
- Describes the elements of an image and their spatial relationships.
- Needs segmentation!



Relational Structures

- Stores relations between objects.
- Important semantic information of an image.
- Needs segmentation and an image description (features)!



No.	Object name	Colour	Mín. row	Min. col.	Insíde
1	БЦП	white	5	40	2
2	sky	blue	0	0	-
3	cloud	grey	20	180	2
4	tree trunk	brown	95	75	6
5	tree crown	green	53	63	-
6	hill	light green	97	0	-
7	\mathbf{pond}	blue	100	160	6

Relational Table

Topic: Histograms

- Sampling and quantization
- Data structures for digital images
- Histograms



Histograms

 "In statistics, a histogram is a graphical display of tabulated frequencies."

[Wikipedia]

• Typically represented as a bar chart:

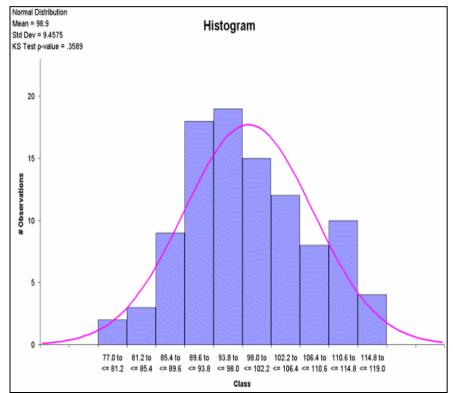
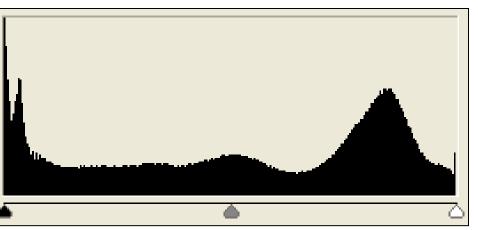


Image Histograms

- Colour or Intensity distribution.
- Typically:
 - Reduced number of bins.
 - Normalization.
- Compressed representation of an image.
 - No spatial information whatsoever!

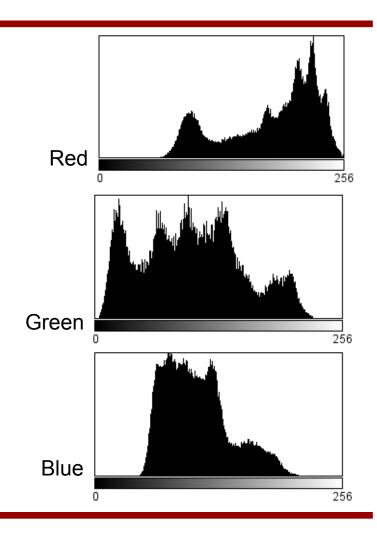




Colour Histogram

- As many histograms as axis of the colour space.
 - Ex: RGB Colour space
 - Red Histogram
 - Green Histogram
 - Blue Histogram
- Combined histogram.

VC 11/12 - T3 - Digital Images



Resources

• R. Gonzalez, and R. Woods – Chapter 2

