
VC 11/12 – T5

Single Pixel Manipulation

Mestrado em Ciência de Computadores
Mestrado Integrado em Engenharia de Redes e
Sistemas Informáticos

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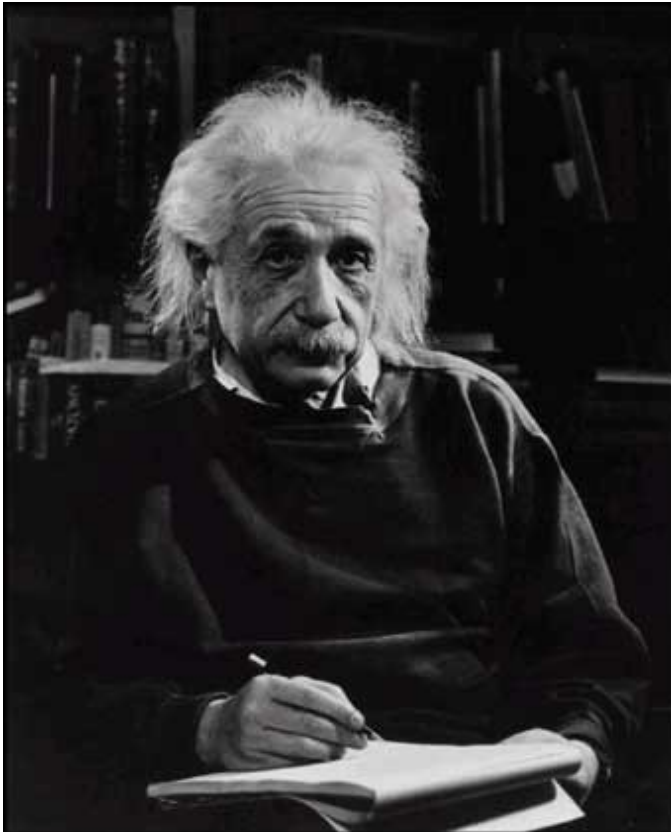
Outline

- Dynamic Range Manipulation
- Neighborhoods and Connectivity
- Image Arithmetic
- Example: Background Subtraction

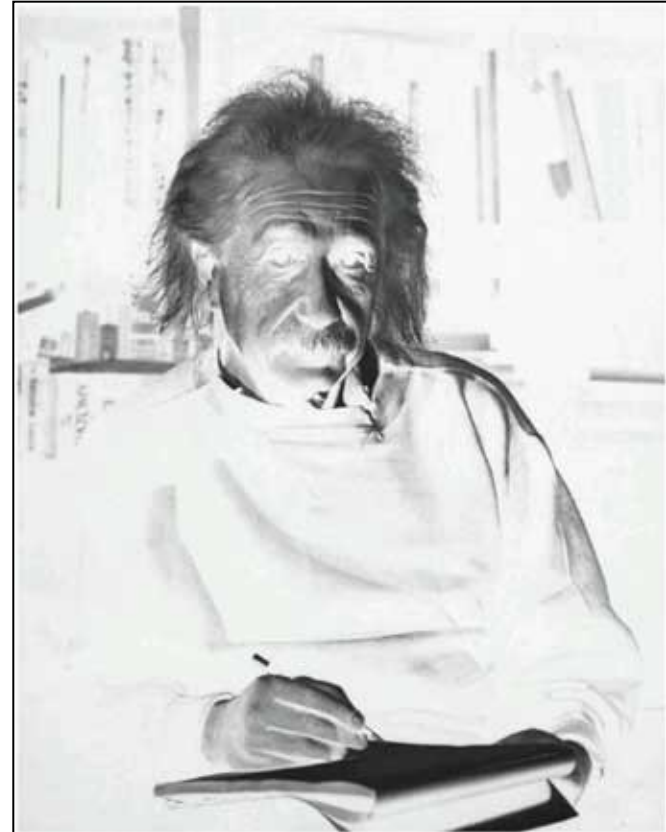
Topic: Dynamic Range Manipulation

- **Dynamic Range Manipulation**
- Neighborhoods and Connectivity
- Image Arithmetic
- Example: Background Subtraction

Manipulation

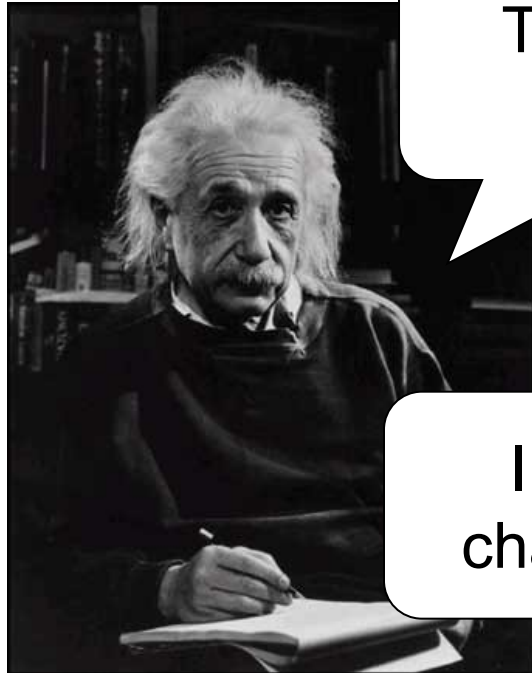


What I see



What I want to see

Digital Images



To change this...

I need to change this!

2	5	4	7	6	9	8		
1	2	3	4	5	6	7		
0	3	2	5	4	7	6		
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
3	2	3	0	1	2	3		
4	3	2	1	0	3	2		
7	4	5	2	3	0	1		
8	7	6	5	4	3	2	1	0

What we see

What a computer sees

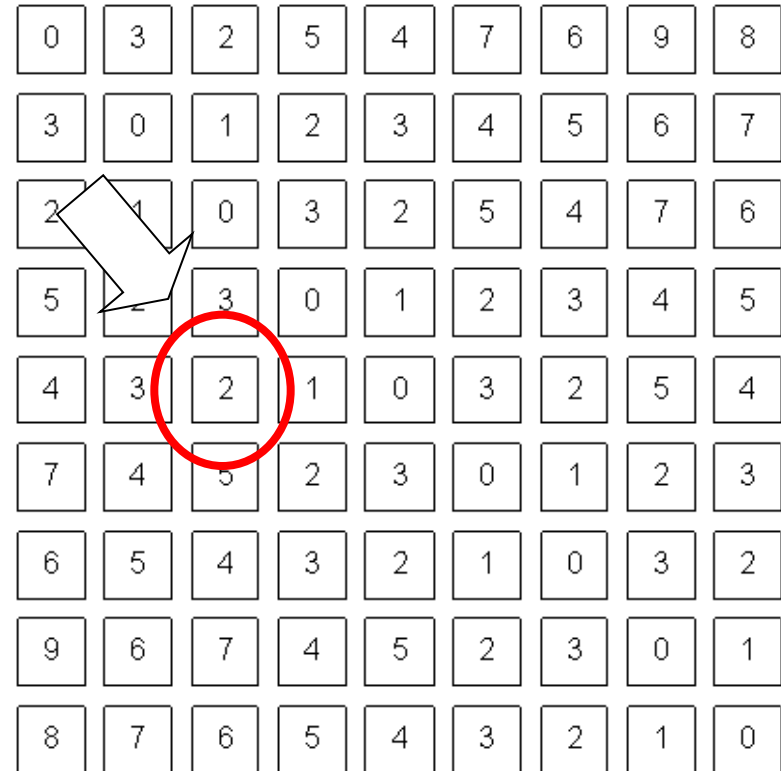
Pixel Manipulation

- Let's start simple
- I want to change a single Pixel.

$$f(X, Y) = MyNewValue$$

- Or, I can apply a transformation T to all pixels individually.

$$g(x, y) = T[f(x, y)]$$



0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	4	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0


Image Domain

- I am directly changing values of the image matrix.

$$g = T(f)$$

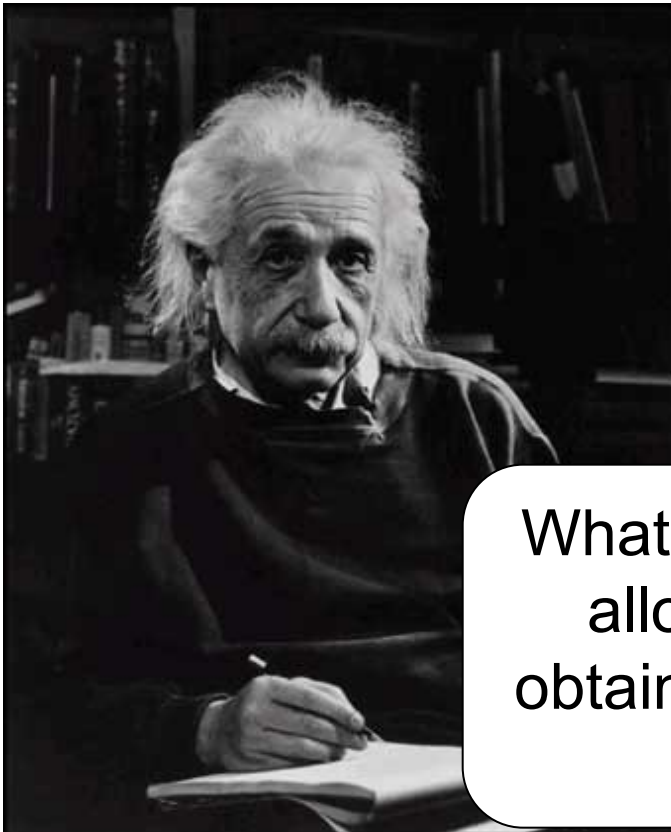
- Image Domain
- So, what is the other possible 'domain'?

0	1	2	3
1	0	3	2
2	3	0	1
3	2	1	0

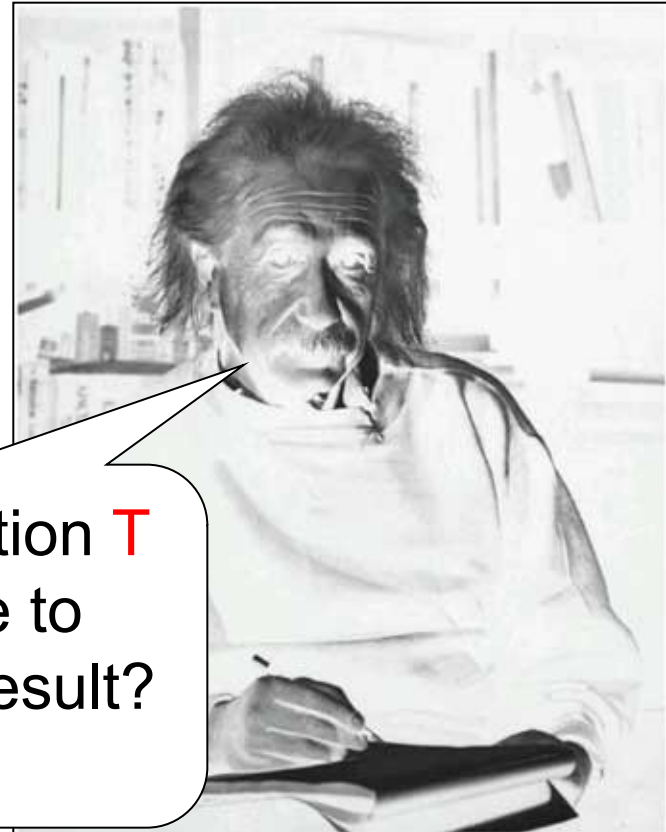


0	1	2	3
1	3	3	2
2	3	3	1
3	2	1	0

Image Negative



What I see



What I want to see

What operation **T**
allows me to
obtain this result?

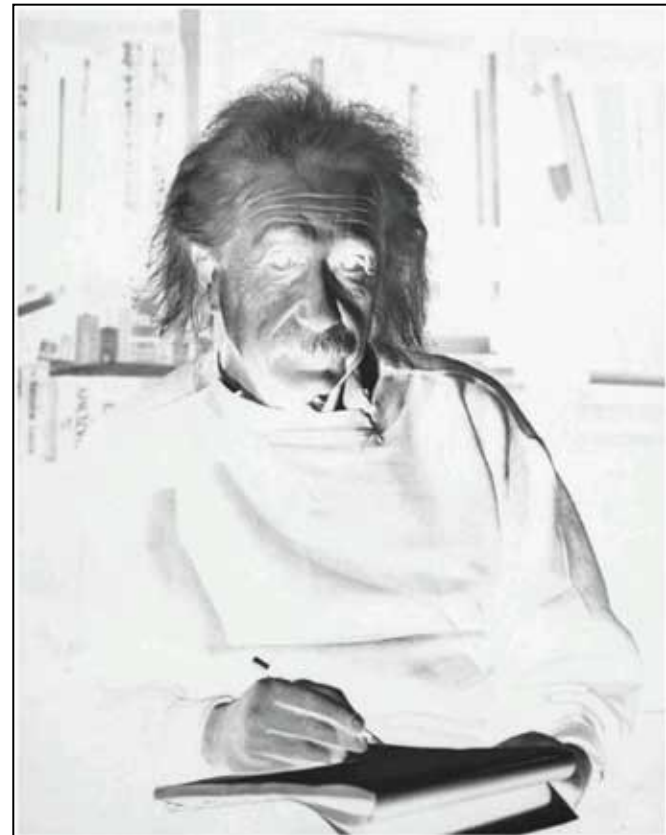
$$g=T(f)$$

Image Negative

- Consider the maximum value allowed by quantization (*max*).
- For 8 bits: 255
- Then:

$$g(x, y) = \text{max} - f(x, y)$$

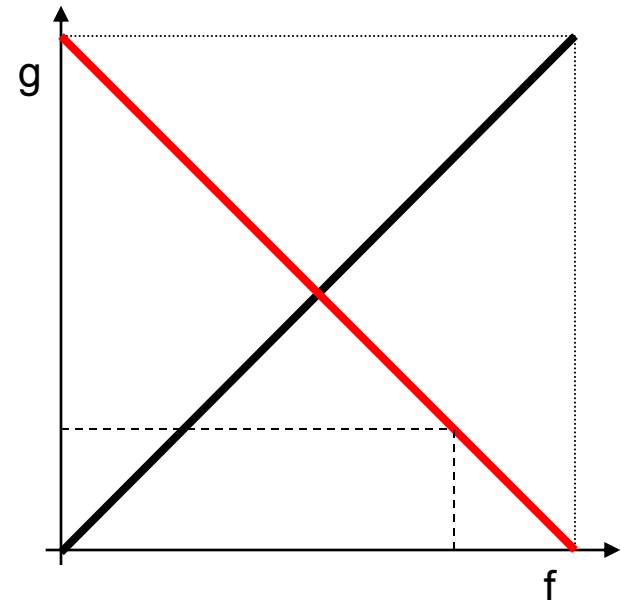
$$g(x, y) = 255 - f(x, y)$$



What I want to see

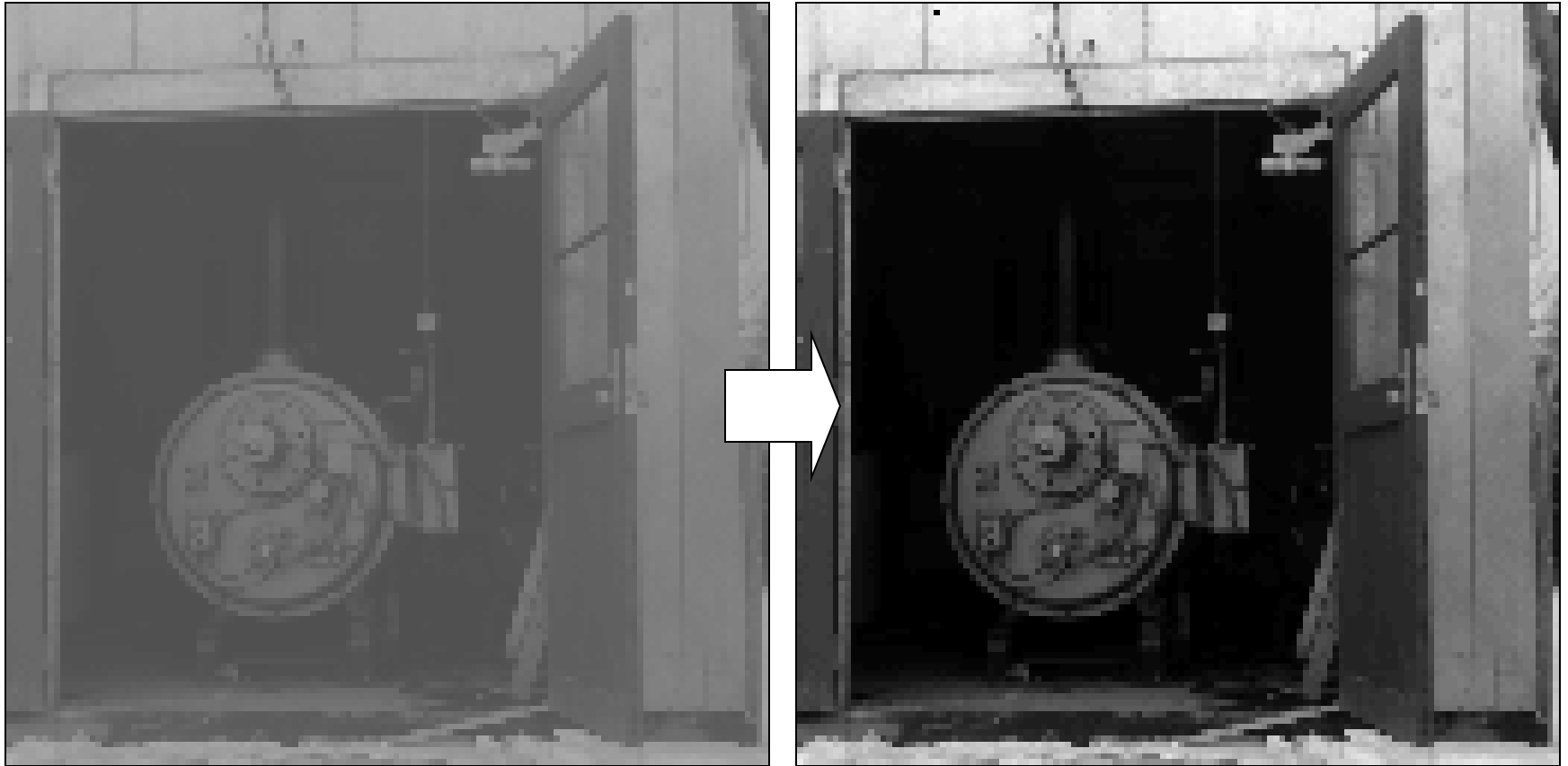
Dynamic Range Manipulation

- What am I really doing?
 - Changing the response of my image to the received brightness.
- Dynamic Range Manipulation
 - Represented by a 2D Plot.

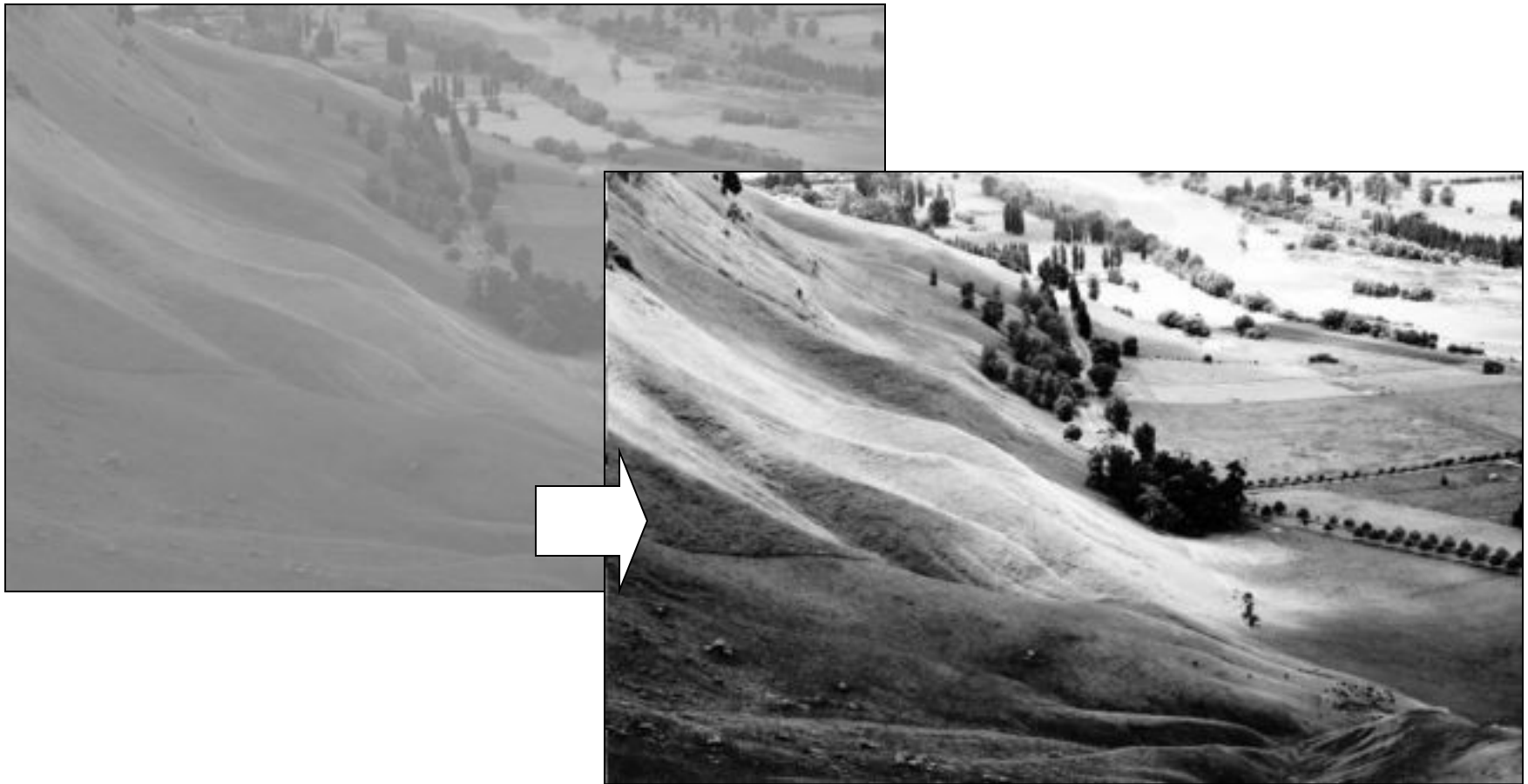


— Normal
— Inverted

Why DRM?

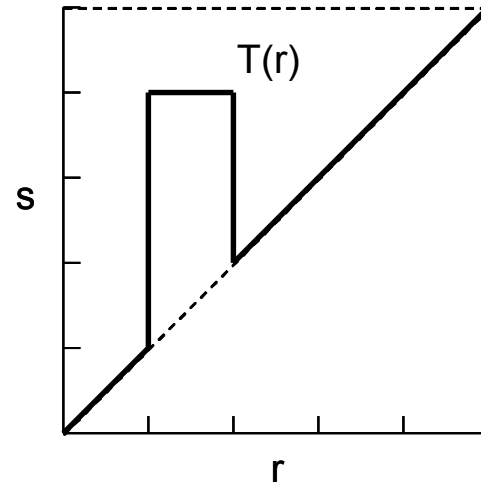
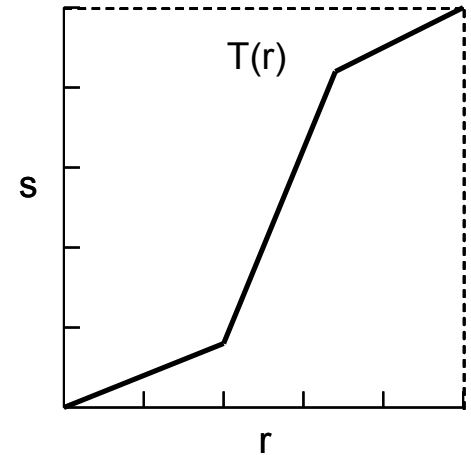


Why DRM?



Other DRM functions

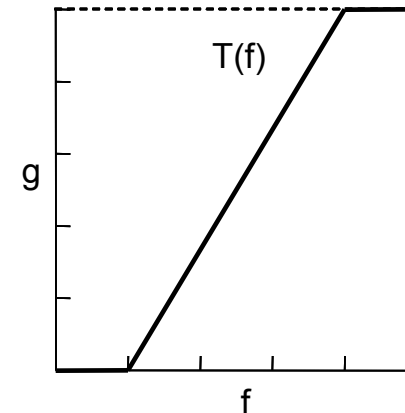
- By manipulating our function we can:
 - Enhance generic image visibility.
 - Enhance specific visual features.
 - Use quantization space a lot better.



Contrast Stretching

- ‘Stretches’ the dynamic range of an image.
- Corrects some image capture problems:
 - Poor illumination, aperture, poor sensor performance, etc.

$$g = \max \frac{f - \min}{\max - \min}$$



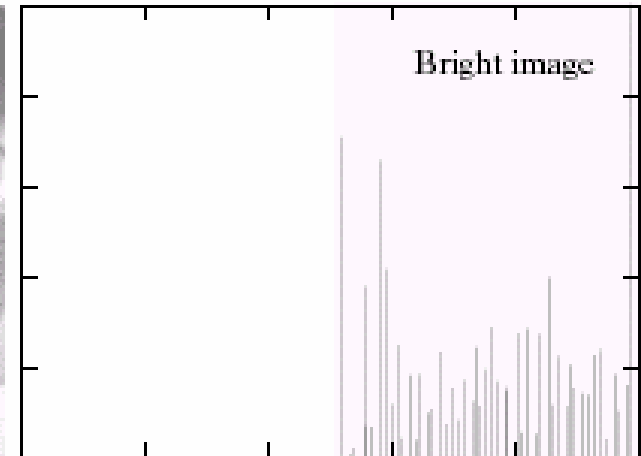
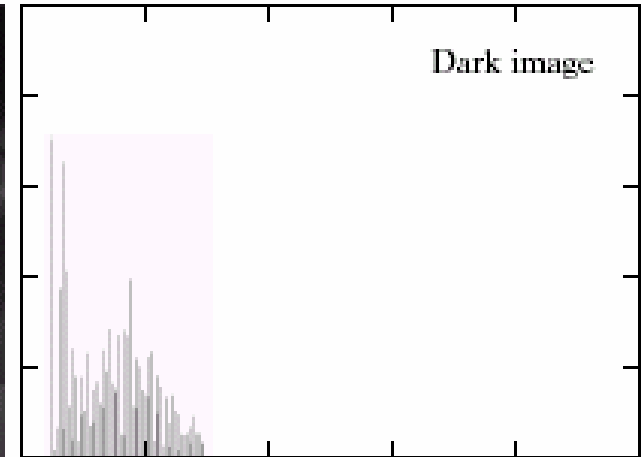
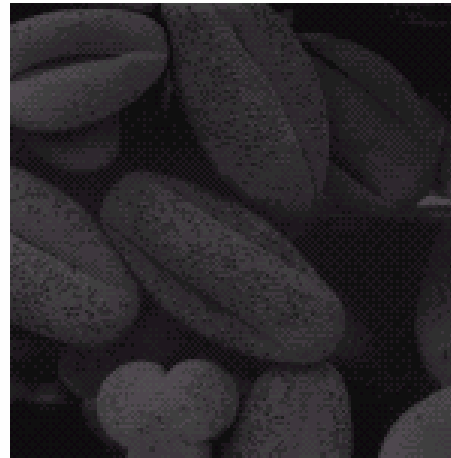
Histogram Processing

- Histograms give us an idea of how we are using our dynamic range

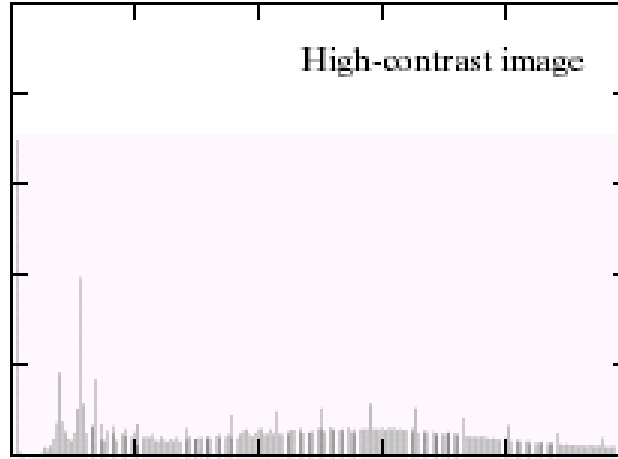
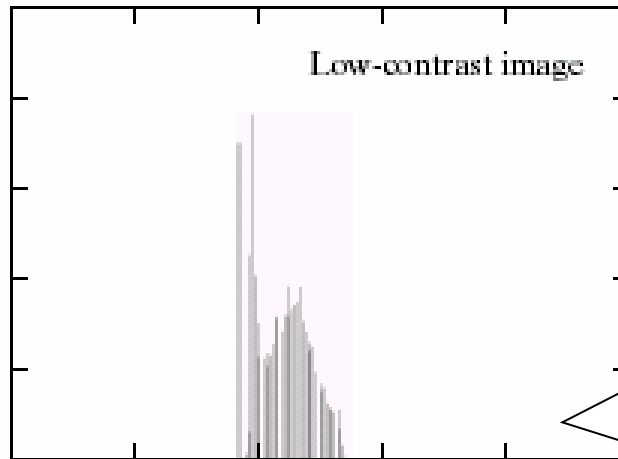


Types of Image Histograms

- Images can be classified into types according to their histogram
 - Dark
 - Bright
 - Low-contrast
 - High-contrast



Types of Image Histograms

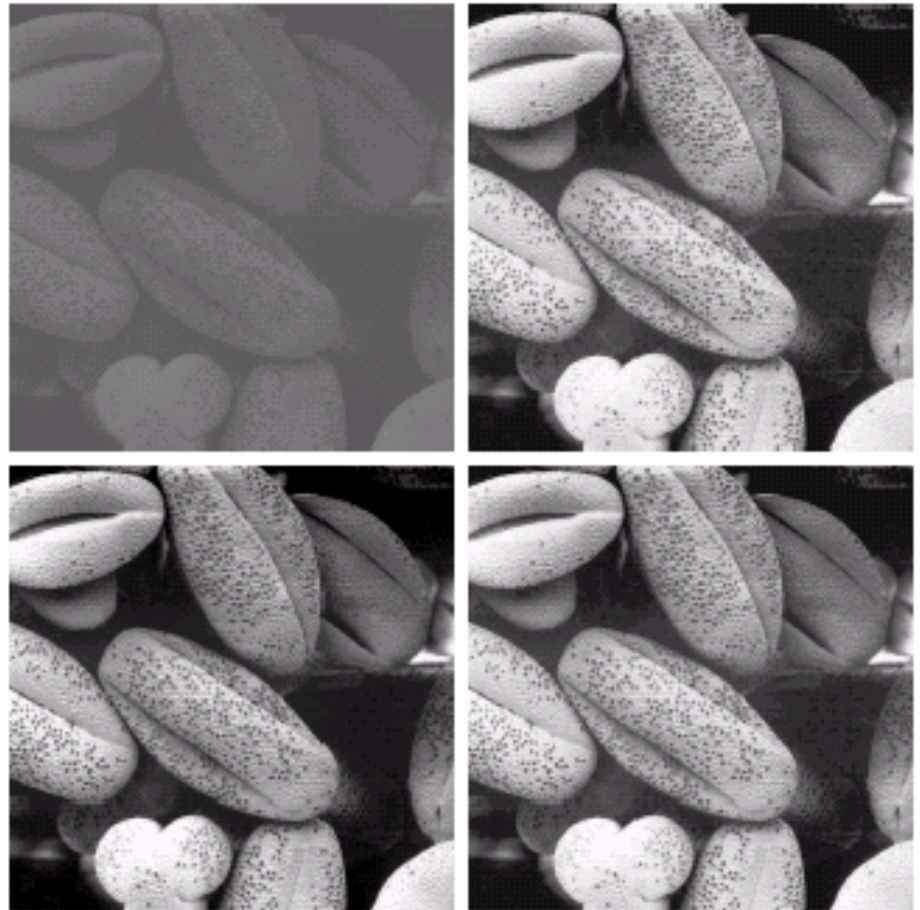


I can
manipulate
this using
single Pixel
operations!

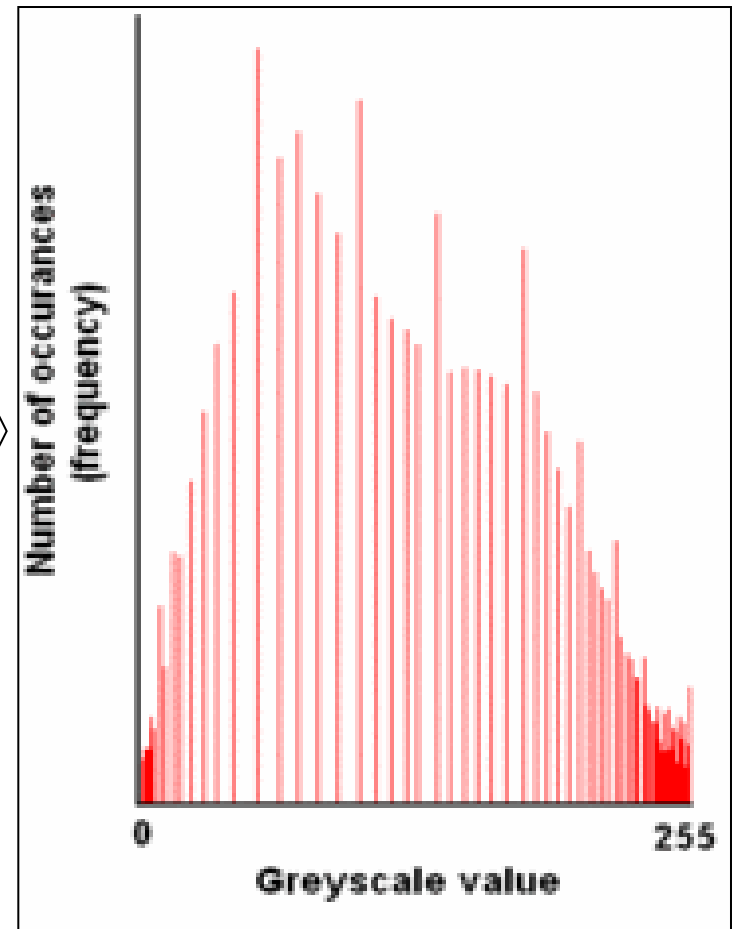
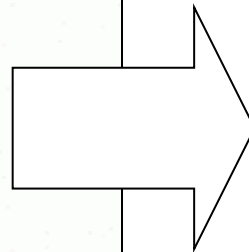
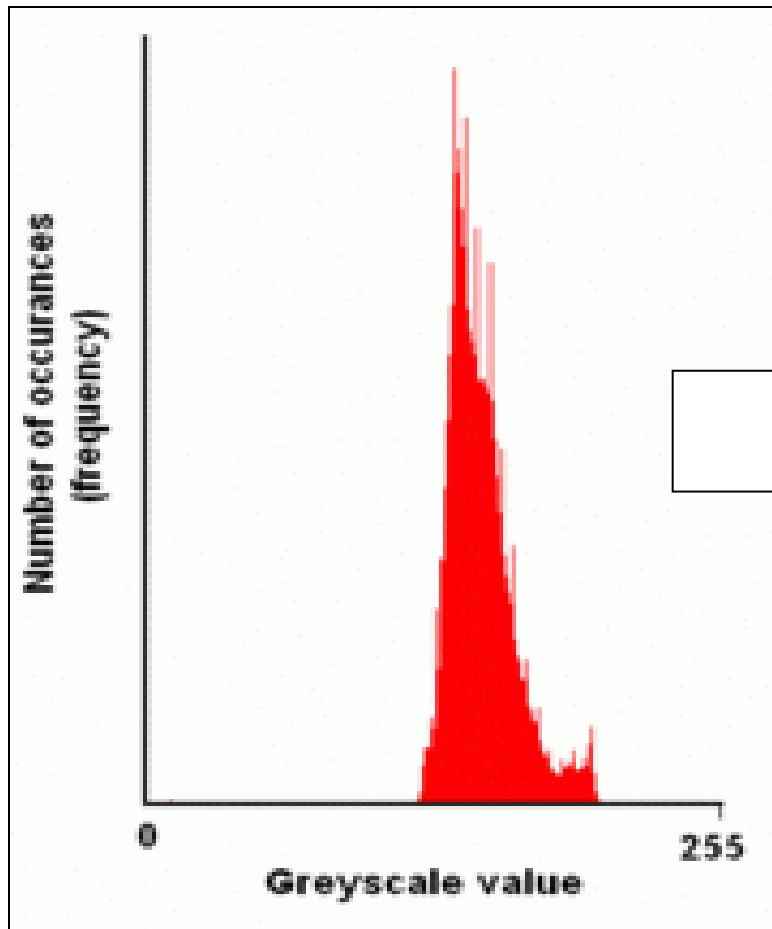
Histogram Equalization

$$s_k = T(r_k) = \sum_{j=0}^k \frac{n_j}{n} = \sum_{j=0}^k p_r(r_j)$$

- **Objective:**
 - Obtain a ‘flat’ histogram.
 - Enhance visual contrast.
- **Digital histogram**
 - Result is a ‘flat-ish’ histogram.
 - Why?



Histogram Equalization

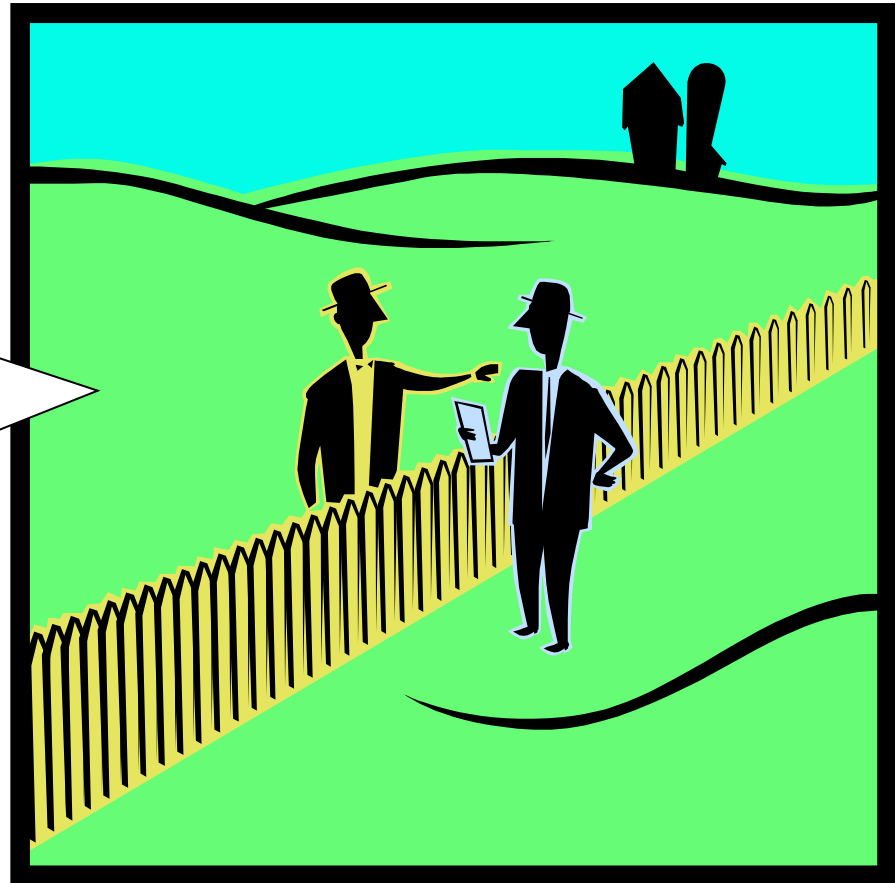


Topic: Neighborhoods and Connectivity

- Dynamic Range Manipulation
- **Neighborhoods and Connectivity**
- Image Arithmetic
- Example: Background Subtraction

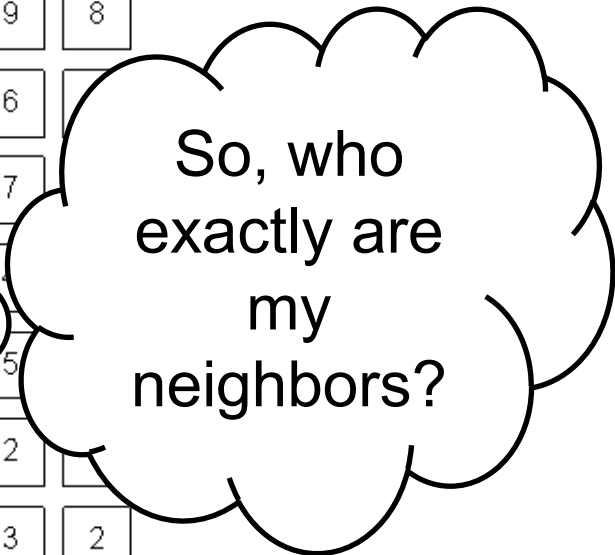
Neighbors

Why do we care at all?



Digital Images

0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
5	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

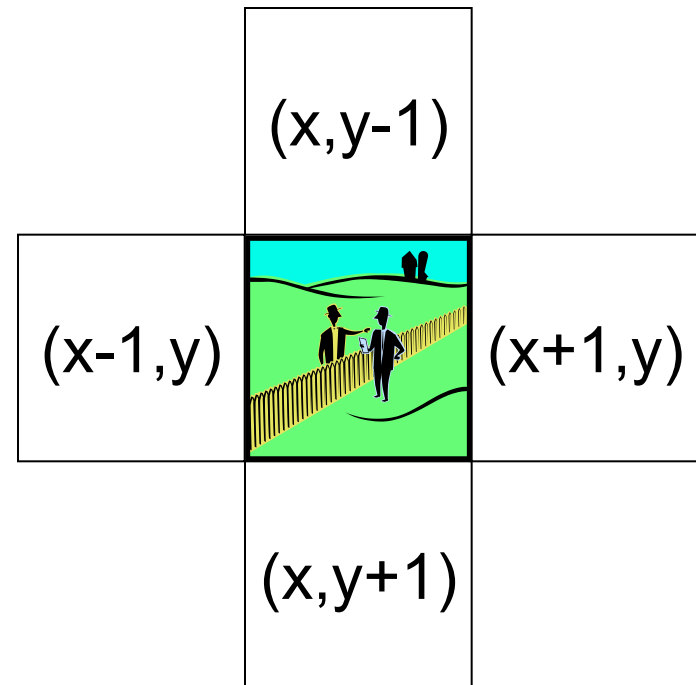


So, who exactly are my neighbors?

What a computer sees

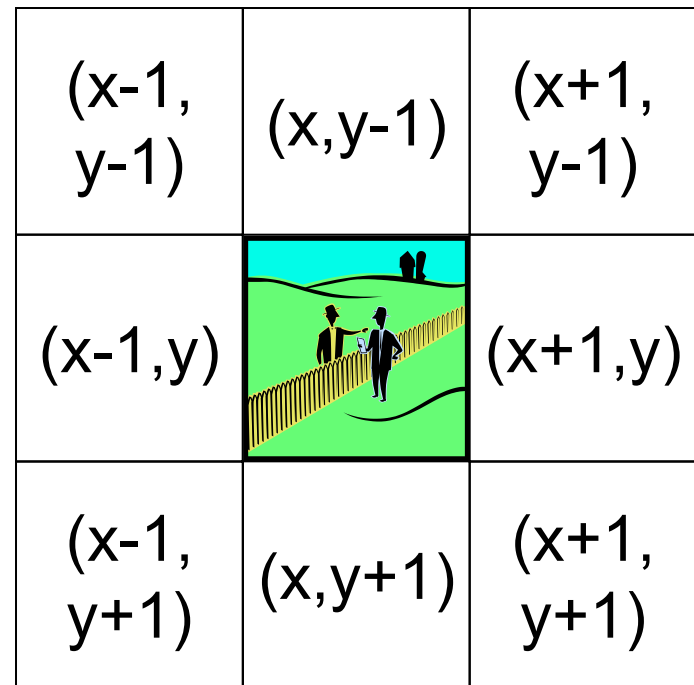
4-Neighbors

- A pixel p at (x,y) has 2 horizontal and 2 vertical neighbors:
 - $(x+1,y)$, $(x-1,y)$,
 $(x,y+1)$, $(x,y-1)$
 - $N_4(p)$: Set of the 4-neighbors of p .
- Limitations?



8-Neighbors

- A pixel has 4 diagonal neighbors
 - $(x+1, y+1)$, $(x+1, y-1)$,
 $(x-1, y+1)$, $(x-1, y-1)$
 - $N_D(p)$: Diagonal set of neighbors
- $N_8(p) = N_4(p) + N_D(p)$
- Limitations?

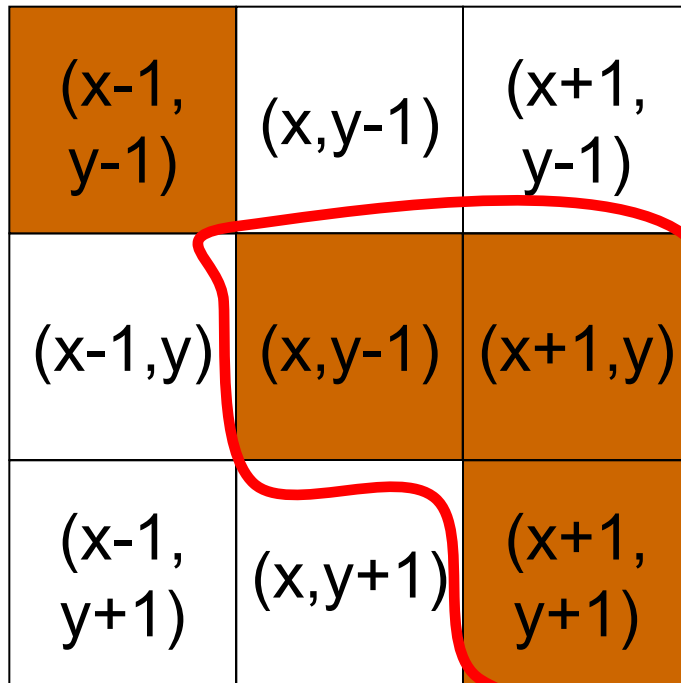


Connectivity

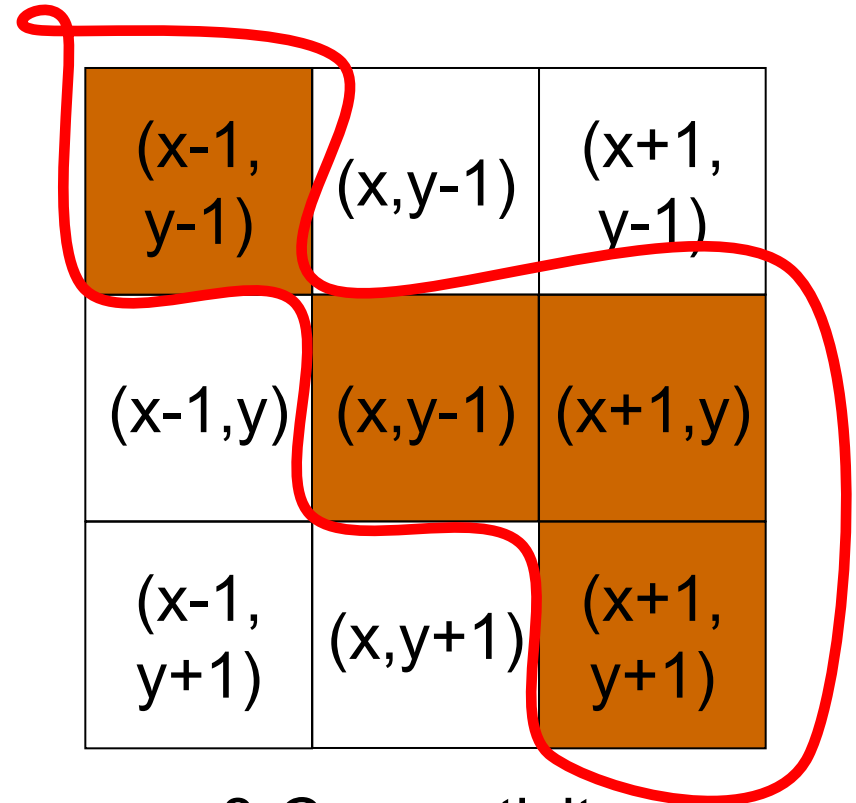
- Two pixels are connected if:
 - They are neighbors (i.e. adjacent in some sense -- e.g. $N_4(p)$, $N_8(p)$, ...)
 - Their gray levels satisfy a specified criterion of similarity (e.g. equality, ...)

$(x-1, y-1)$	$(x, y-1)$	$(x+1, y-1)$
$(x-1, y)$	(x, y)	$(x+1, y)$
$(x-1, y+1)$	$(x, y+1)$	$(x+1, y+1)$

4 and 8-Connectivity

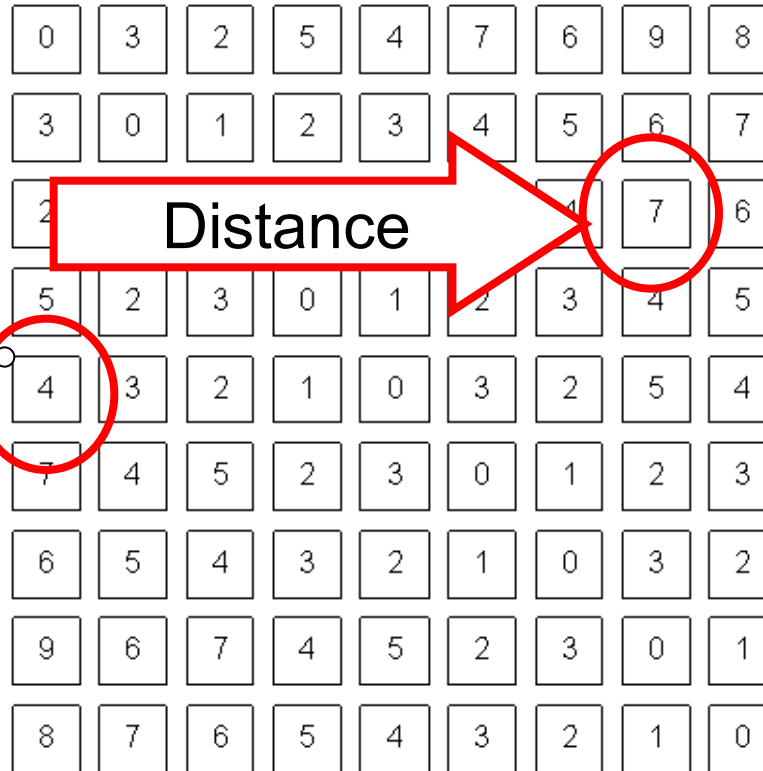
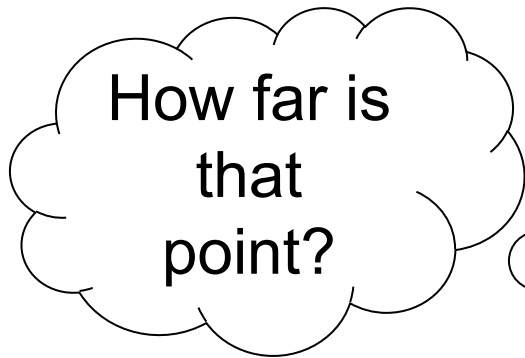


4-Connectivity



8-Connectivity

Distances



D4 Distance

- D_4 distance (city-block distance):

- $D_4(p,q) = |x-s| + |y-t|$

- forms a diamond centered at (x,y)

- e.g. pixels with $D_4 \leq 2$ from p

```
      2
     2 1 2
    2 1 0 1 2
     2 1 2
      2
```

$D_4 = 1$ are the 4-neighbors of p

D8 Distance

- D_8 distance (chessboard distance):
 - $D_8(p,q) = \max(|x-s|, |y-t|)$
 - Forms a square centered at p
 - e.g. pixels with $D_8 \leq 2$ from p

```
2 2 2 2 2
2 1 1 1 2
2 1 0 1 2
2 1 1 1 2
2 2 2 2 2
```

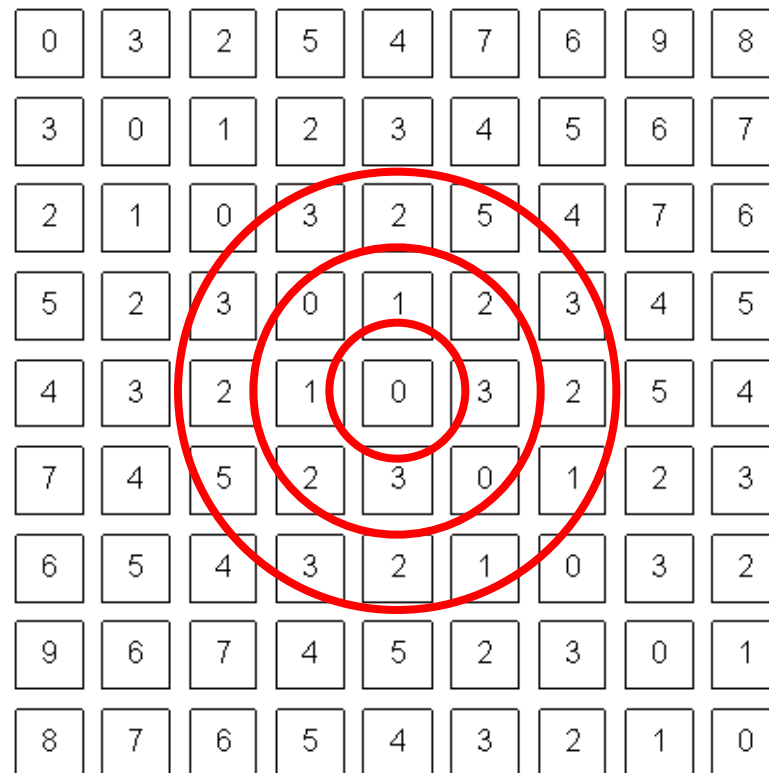
$D_8 = 1$ are the 8-neighbors of p

Euclidean Distance

- Euclidean distance:

- $D_e(p,q) = [(x-s)^2 + (y-t)^2]^{1/2}$

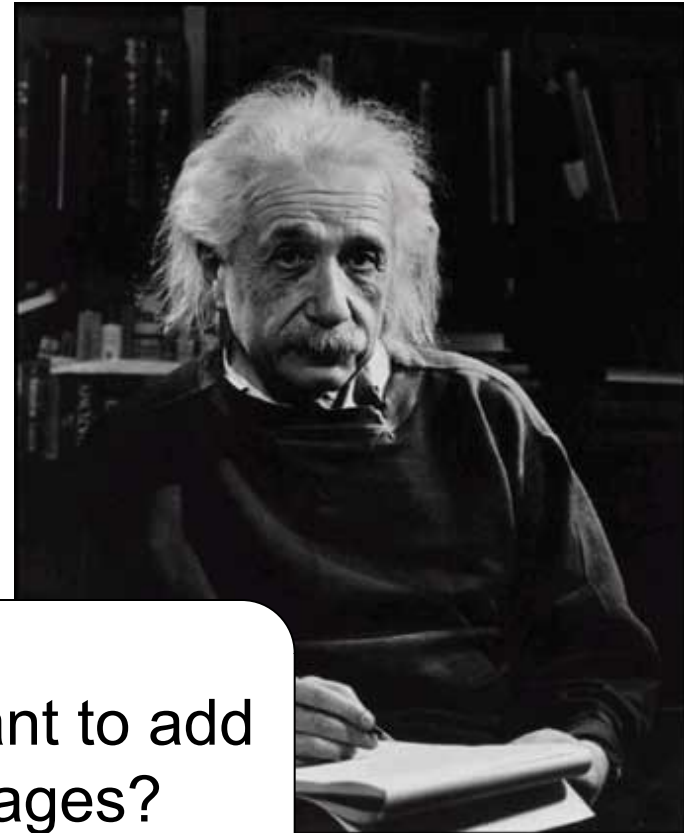
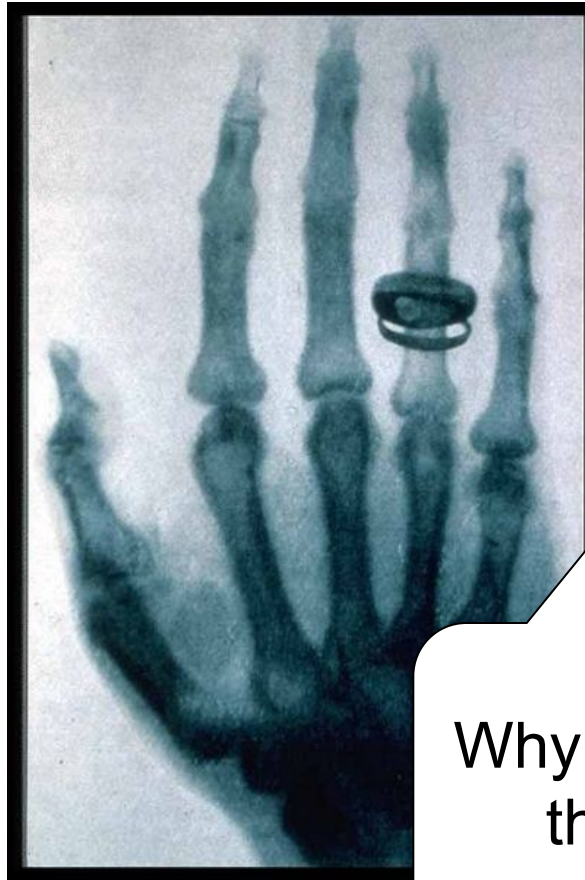
- Points (pixels) having a distance less than or equal to r from (x,y) are contained in a disk of radius r centered at (x,y) .



Topic: Image Arithmetic

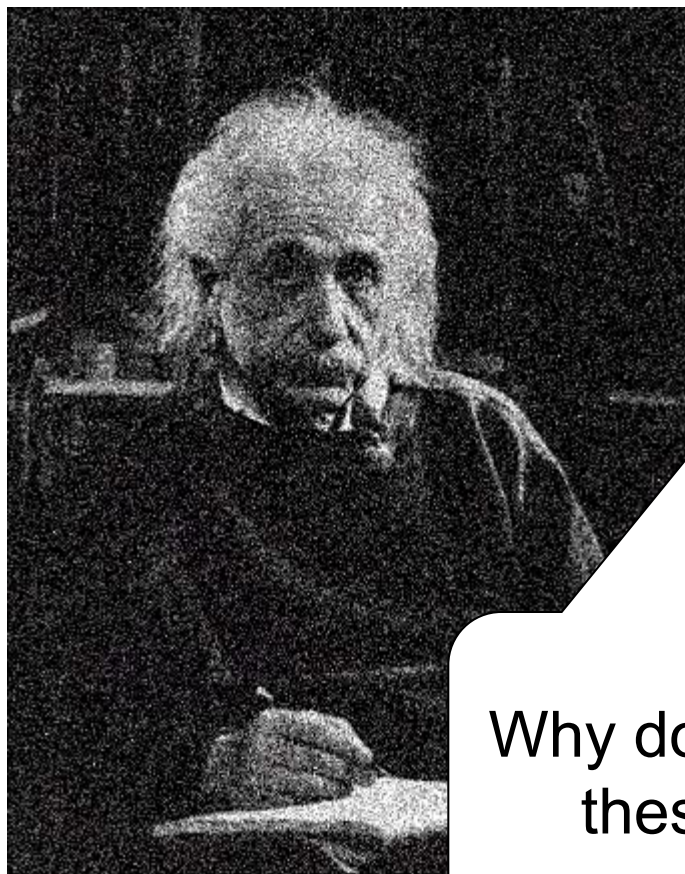
- Dynamic Range Manipulation
- Neighborhoods and Connectivity
- **Image Arithmetic**
- Example: Background Subtraction

Arithmetic operations between images



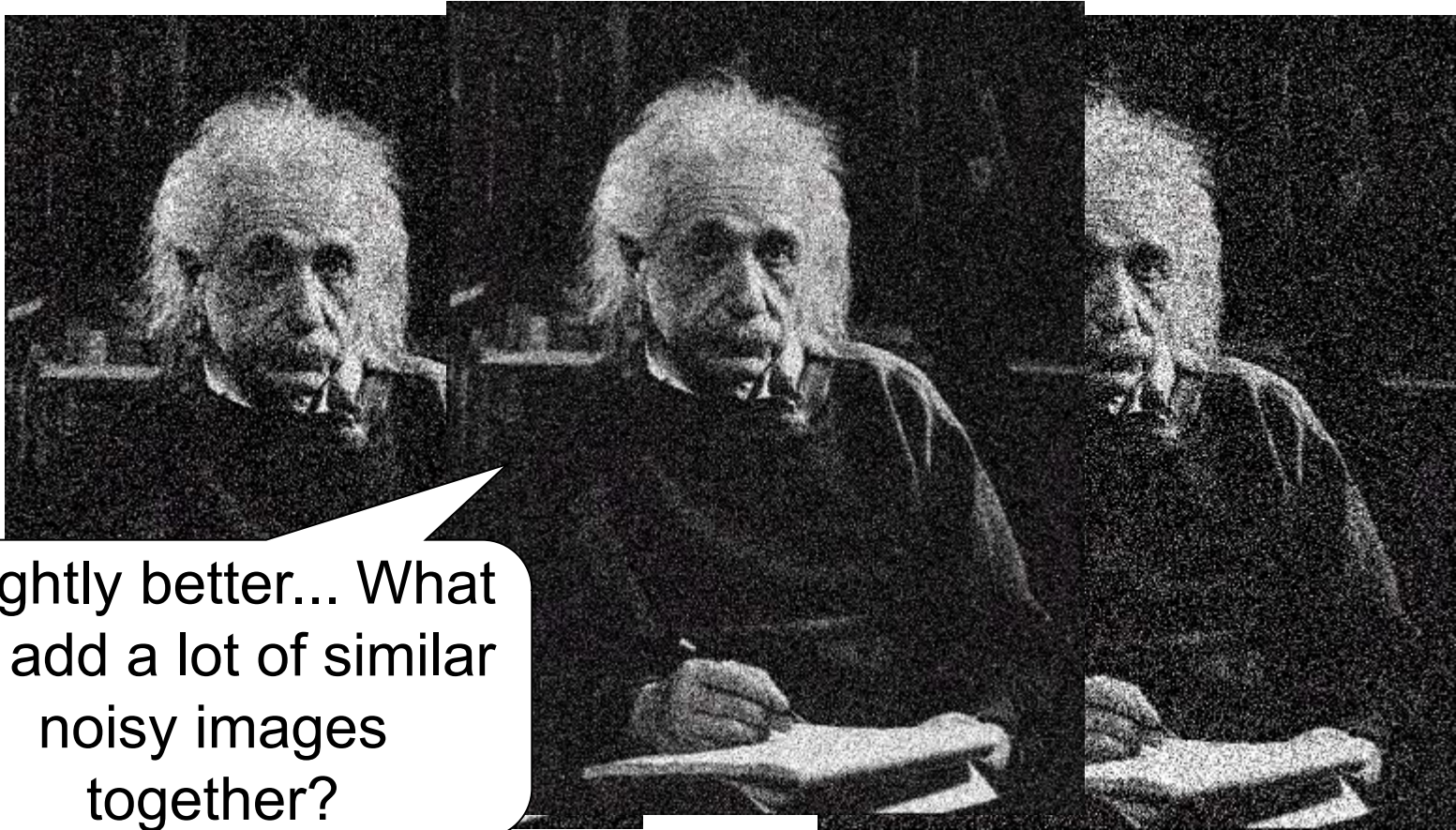
Why do I want to add these images?

Arithmetic operations between images



Why do I want to add these images?

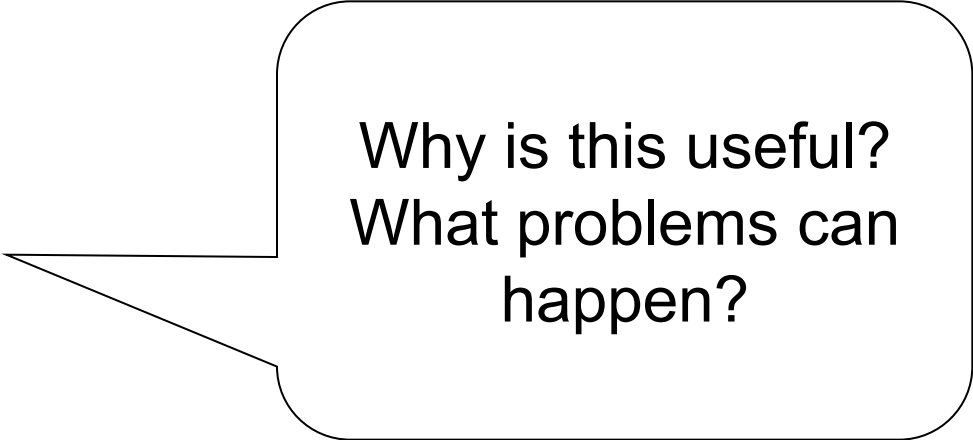
Arithmetic operations between images



Slightly better... What if I add a lot of similar noisy images together?

Image Arithmetic

- Image 1: $a(x,y)$
- Image 2: $b(x,y)$
- Result: $c(x,y) = a(x,y)$ OPERATION $b(x,y)$
- Possibilities:
 - Addition
 - Subtraction
 - Multiplication
 - Division
 - Etc..



Why is this useful?
What problems can
happen?

Example

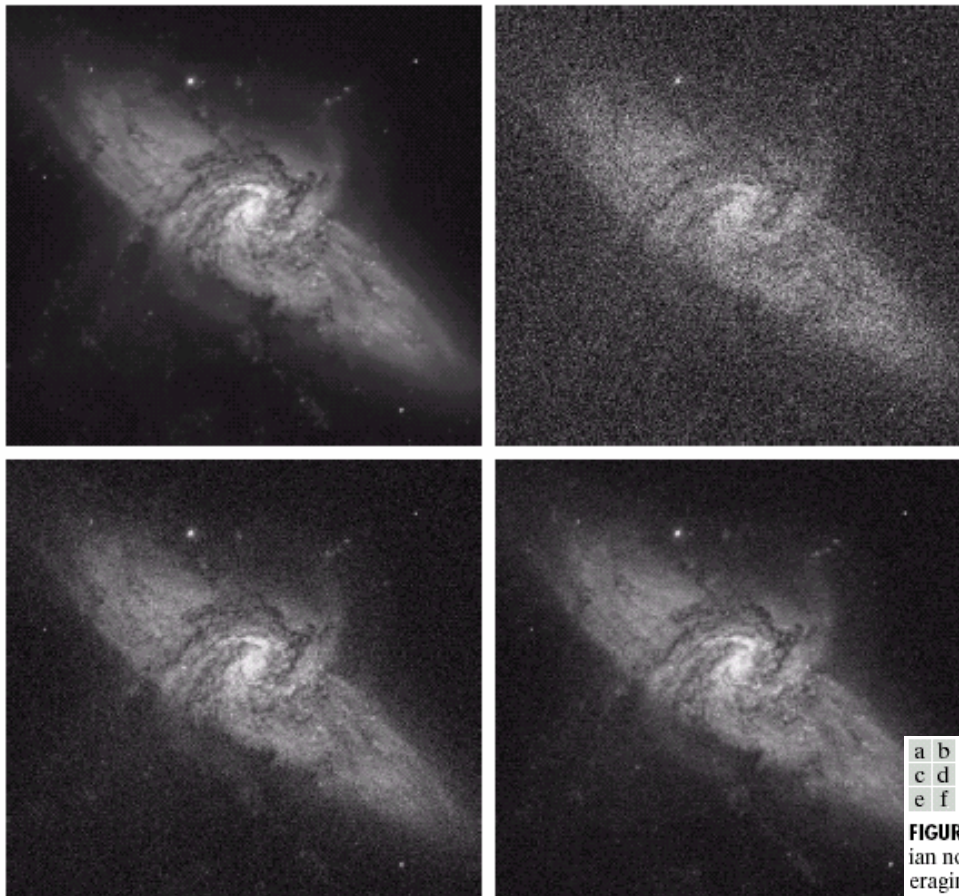


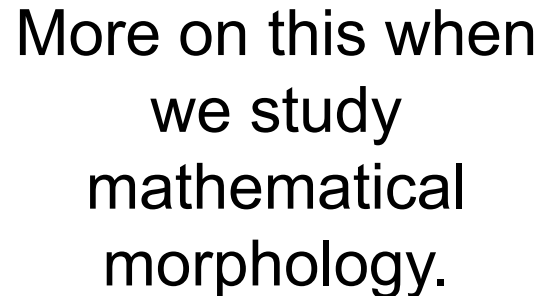
Image
Addition

a b
c d
e f

FIGURE 3.30 (a) Image of Galaxy Pair NGC 3314. (b) Image corrupted by additive Gaussian noise with zero mean and a standard deviation of 64 gray levels. (c)–(f) Results of averaging $K = 8, 16, 64,$ and 128 noisy images. (Original image courtesy of NASA.)

Logic Operations

- Binary Images
- We can use Boolean Logic
- Operations:
 - AND
 - OR
 - NOT



More on this when
we study
mathematical
morphology.

Topic: Example: Background Subtraction

- Dynamic Range Manipulation
- Neighborhoods and Connectivity
- Image Arithmetic
- **Example: Background Subtraction**

Example: Background Subtraction

- Image arithmetic is simple and powerful.

Is there a
person
here?
Where?



Background Subtraction

- Remember: We can only see numbers!

Is there a
person
here?
Where?

0	3	2	5	4	7	6	9	8
3	0	1	2	3	4	5	6	7
2	1	0	3	2	5	4	7	6
1	2	3	0	1	2	3	4	5
4	3	2	1	0	3	2	5	4
7	4	5	2	3	0	1	2	3
6	5	4	3	2	1	0	3	2
9	6	7	4	5	2	3	0	1
8	7	6	5	4	3	2	1	0

Background Subtraction

- What if I know this?



Background Subtraction

- Subtract!
- Limitations?



Background Subtraction

- **Objective:**
 - Separate the foreground objects from a static background.
- **Large variety of methods:**
 - Mean & Threshold [CD04]
 - Normalized Block Correlation [Mats00]
 - Temporal Derivative [Hari98]
 - Single Gaussian [Wren97]
 - Mixture of Gaussians [Grim98]

Segmentation!!
More on this
later.

Resources

- R. Gonzalez, and R. Woods – Chapter 2
- R. Gonzalez, and R. Woods – Chapter 4
- K. Toyama, J. Krumm, B. Brumitt, and B. Meyers, “Wallflower: Principles and practice of background maintenance”, in Proc. of IEEE ICCV, Corfu, Greece, 1999.