# Computer Vision – TP1 Image Formation

Miguel Tavares Coimbra



### Outline

- 'Computer Vision'?
- The Human Visual System
- Image Capturing Systems

# Topic: Computer Vision?

- 'Computer Vision'?
- The Human Visual System
- Image Capturing Systems

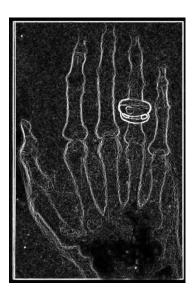
### Computer Vision

"The goal of Computer Vision is to make useful decisions about real physical objects and scenes based on sensed images",

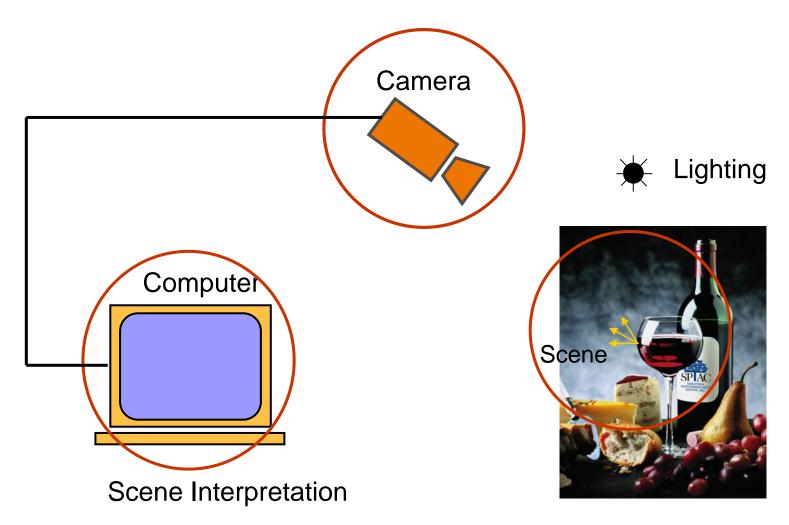
Shapiro and Stockman, "Computer Vision", 2001







### Components of a Computer Vision System

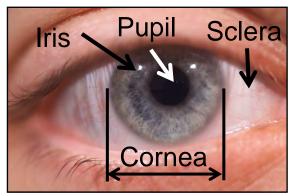




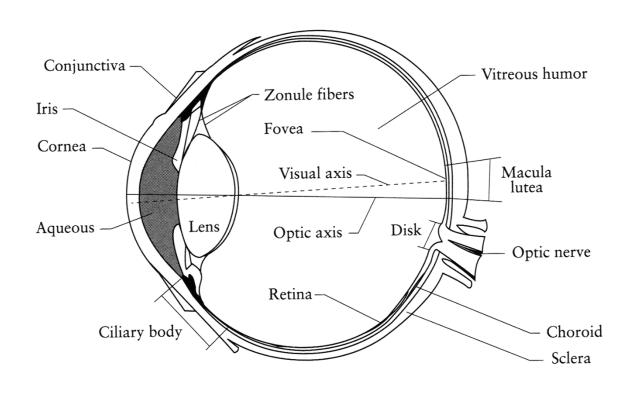
### Topic: The Human Visual System

- 'Computer Vision'?
- The Human Visual System
- Image Capturing Systems

### Our Eyes

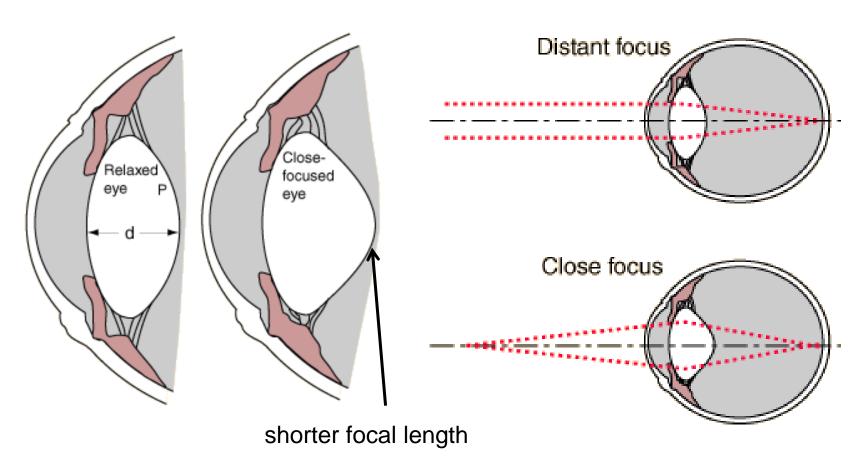






Iris is the diaphragm that changes the aperture (pupil) Retina is the sensor where the fovea has the highest resolution

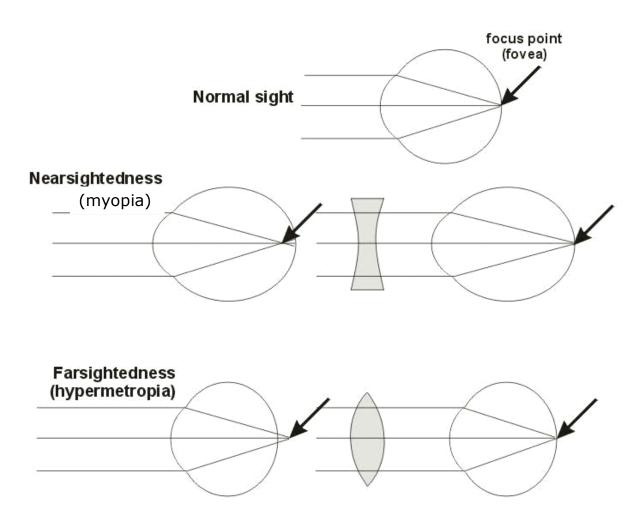
# Focusing



Changes the focal length of the lens



# Myopia and Hyperopia



### Blind Spot in the Eye

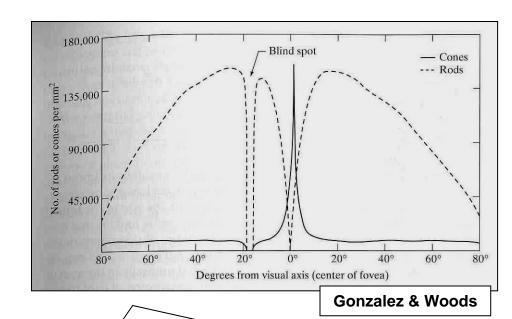


Close your right eye and look directly at the "+"

### Colour

### Our retina has:

- Cones Measure the frequency of light (colour)
  - 6 to 7 millions
  - High-definition
  - Need high luminosity
- Rods Measure the intensity of light (luminance)
  - 75 to 150 millions
  - Low-definition
  - Function with low luminosity

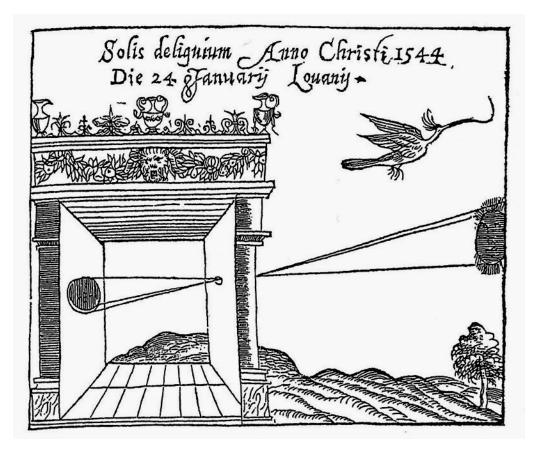


We only see colour in the centre of our retina!



### Topic: Image Capturing Systems

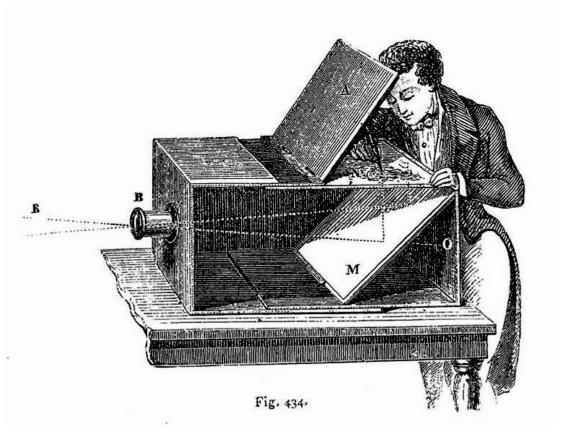
- 'Computer Vision'?
- The Human Visual System
- Image Capturing Systems







1544



1544 1568

Lens Based Camera Obscura, 1568



Still Life, Louis Jaques Mande Daguerre, 1837

1544 1568

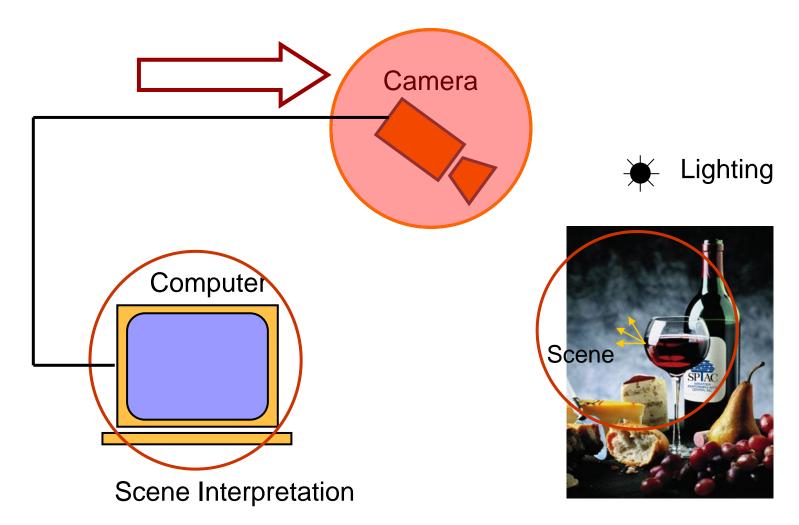
1837





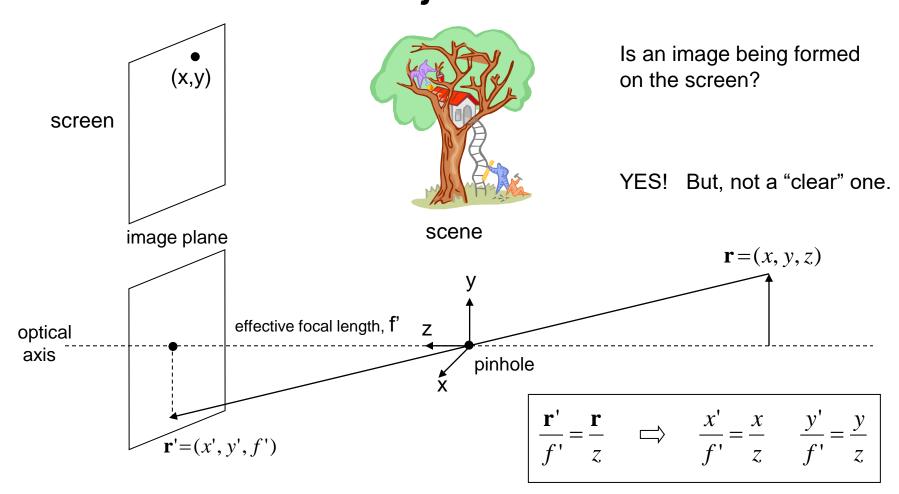


### Components of a Computer Vision System



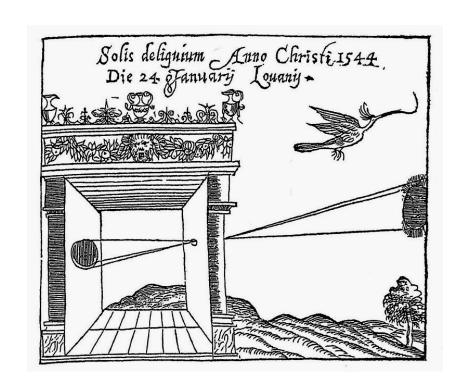


# Pinhole and the Perspective Projection



### Pinhole Camera

- Basically a pinhole camera is a box, with a tiny hole at one end and film or photographic paper at the other.
- Mathematically: out of all the light rays in the world, choose the set of light rays passing through a point and projecting onto a plane.



### Pinhole Photography



©Charlotte Murray Untitled, 4" x 5" pinhole photograph, 1992

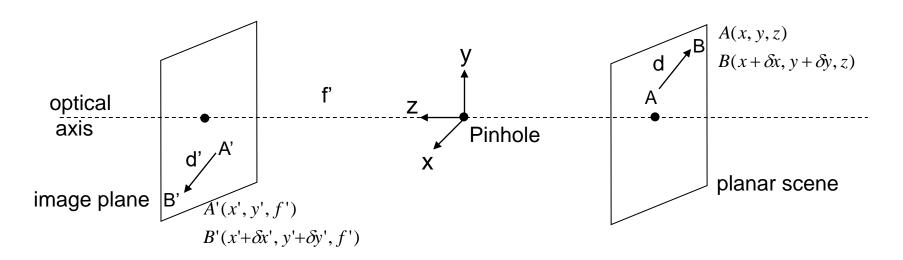


Image Size inversely proportional to Distance

Reading: http://www.pinholeresource.com/



## Magnification



#### From perspective projection:

$$\frac{x'}{f'} = \frac{x}{z} \qquad \frac{y'}{f'} = \frac{y}{z}$$



$$\frac{x' + \delta x'}{f'} = \frac{x + \delta x}{z}$$

$$\frac{x'+\delta x'}{f'} = \frac{x+\delta x}{z} \qquad \frac{y'+\delta y'}{f'} = \frac{y+\delta y}{z}$$

### Magnification:

$$m = \frac{d'}{d} = \frac{\sqrt{(\delta x')^2 + (\delta y')^2}}{\sqrt{(\delta x)^2 + (\delta y)^2}} = \frac{f'}{z}$$

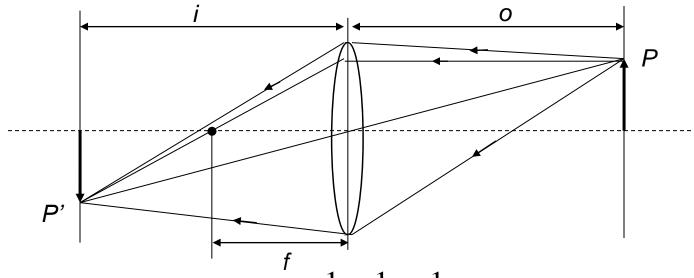
$$\frac{Area_{image}}{Area_{scene}} = m^2$$





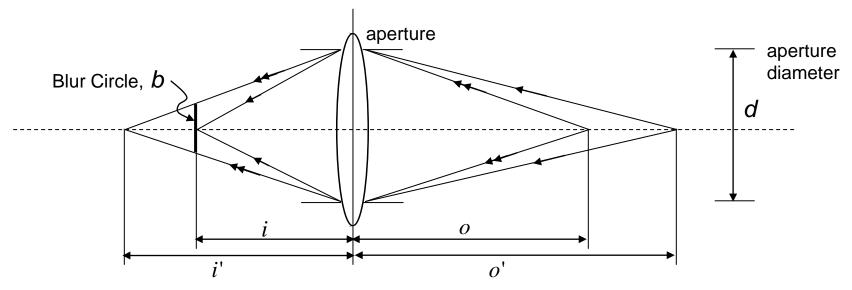
# Image Formation using Lenses

- Lenses are used to avoid problems with pinholes.
- Ideal Lens: Same projection as pinhole but gathers more light!



- Gaussian Thin Lens Formula:  $\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$
- *f* is the focal length of the lens determines the lens's ability to refract light

### Focus and Defocus



Gaussian Law:

$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$$
$$\frac{1}{i'} + \frac{1}{o'} = \frac{1}{f}$$

$$\qquad \qquad \Box \\$$

$$(i'-i) = \frac{f}{(o'-f)} \frac{f}{(o-f)} (o-o')$$

• In theory, only one scene plane is in focus

### Depth of Field

- Range of object distances over which image is <u>sufficiently well</u> focused
- Range for which blur circle is less than the resolution of the sensor



http://images.dpchallenge.com/images\_portfolio/27920/print\_preview/116336.jpg

### Image Sensors

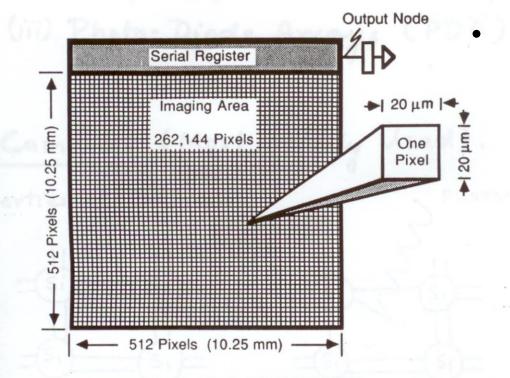


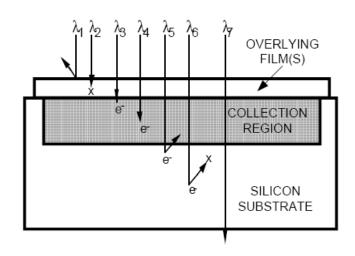
Fig. 4. Typical  $512 \times 512$  CCD.

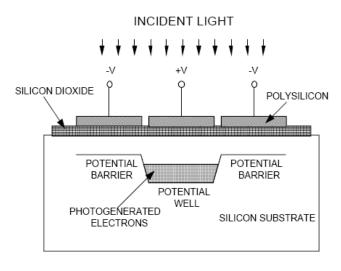
### Considerations

- Speed
- Resolution
- Signal / Noise Ratio
- Cost

### Image Sensors

Convert light into an electric charge





CCD (charge coupled device)

Higher dynamic range High uniformity Lower noise



CMOS (complementary metal

Oxide semiconductor)

Lower voltage

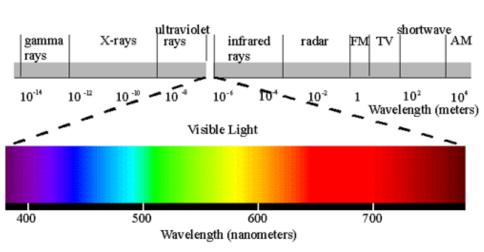
Higher speed

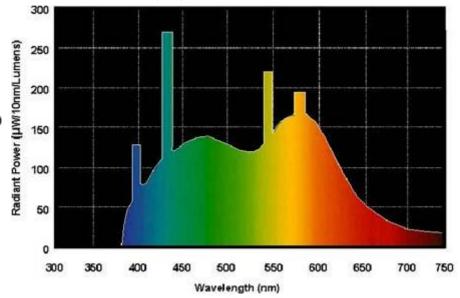
Lower system complexity



# Sensing Brightness

Incoming light has a spectral distribution  $p(\lambda)$ 





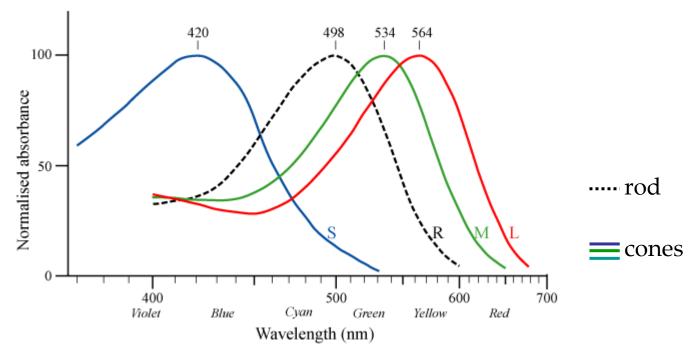
So the pixel intensity becomes

$$I = k \int_{-\infty}^{\infty} q(\lambda) p(\lambda) d\lambda$$



### How do we sense colour?

Do we have infinite number of filters?



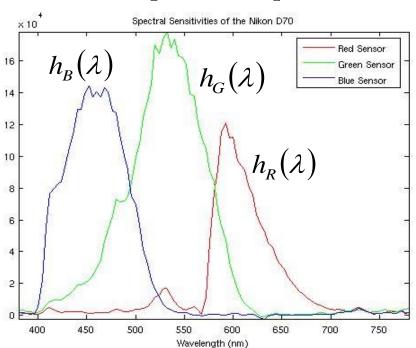
Three filters of different spectral responses



# Sensing Colour

• Tristimulus (trichromatic) values  $(I_R, I_G, I_B)$ 

Camera's spectral response functions:  $h_R(\lambda), h_G(\lambda), h_B(\lambda)$ 

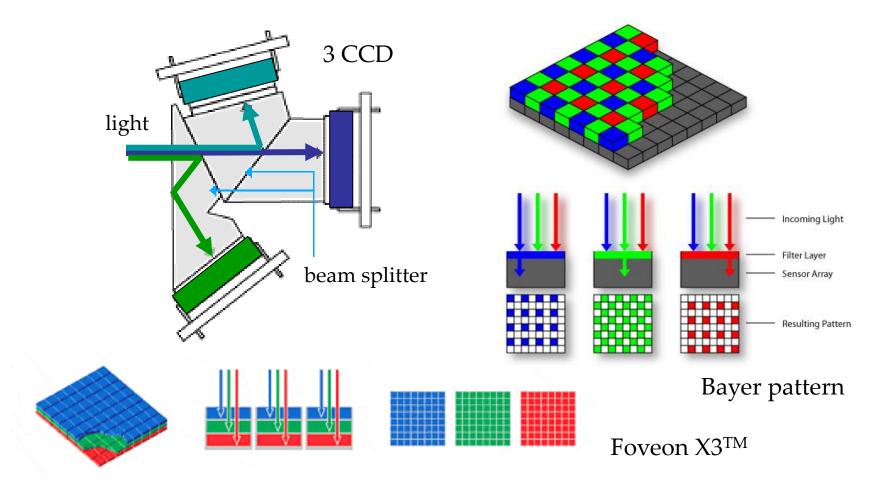


$$I_{R} = k \int_{-\infty}^{\infty} h_{R}(\lambda) p(\lambda) d\lambda$$

$$I_G = k \int_{-\infty}^{\infty} h_G(\lambda) p(\lambda) d\lambda$$

$$I_{B} = k \int_{-\infty}^{\infty} h_{B}(\lambda) p(\lambda) d\lambda$$

# Sensing Colour





### Resources

- Szeliski, "Computer Vision: Algorithms and Applications", Springer, 2011
  - Chapter 1 "Introduction"
  - Chapter 2 "Image Formation"