

Computer Vision – TP1

Image Formation

Miguel Coimbra, Francesco Renna

Outline

- ‘Computer Vision’?
- The Human Visual System
- Image Capturing Systems

Topic: Computer Vision?

- 'Computer Vision'?
- The Human Visual System
- Image Capturing Systems

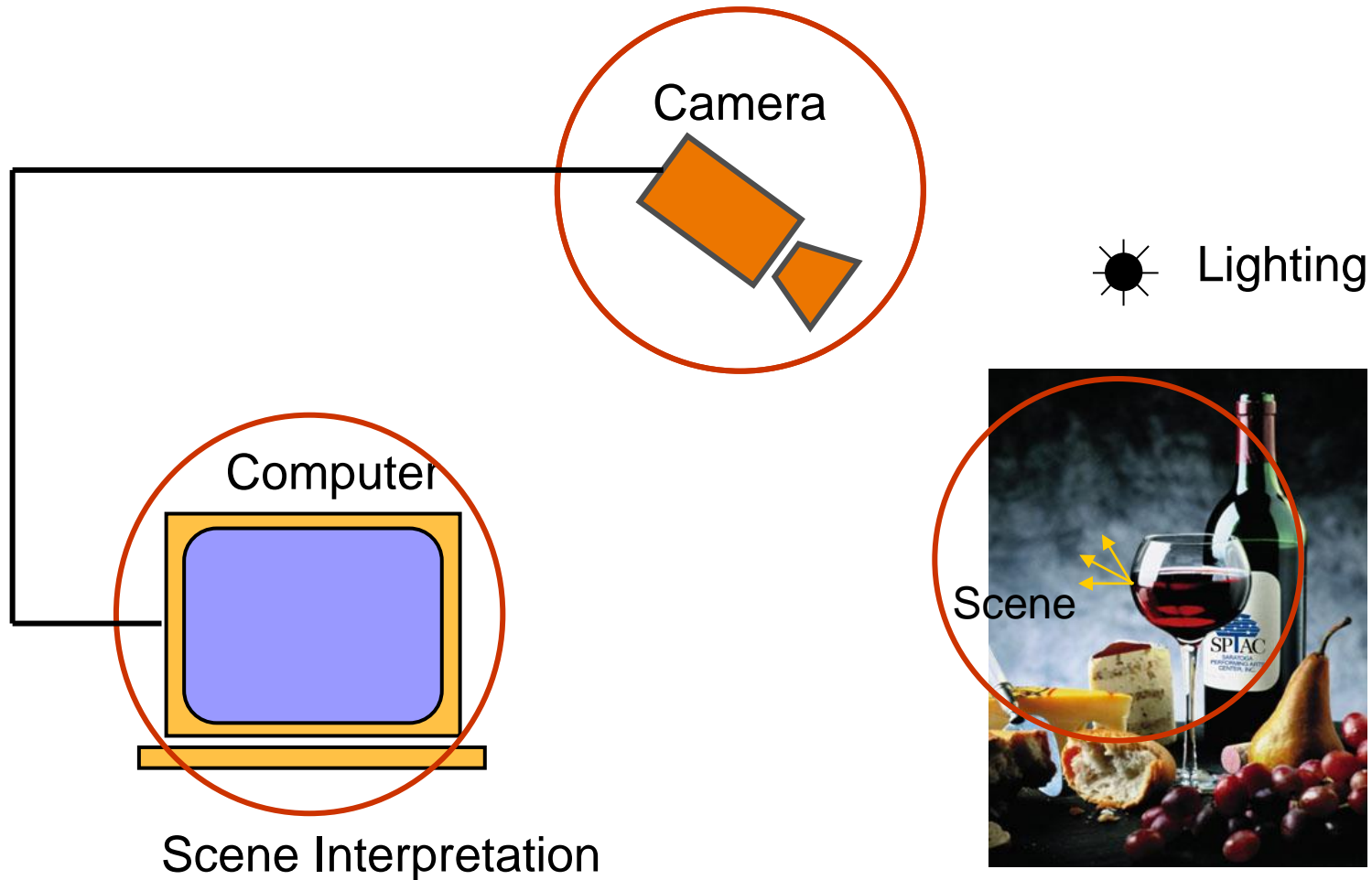
Computer Vision

“The goal of **Computer Vision** is to make useful decisions about real physical objects and scenes based on sensed images”,

Shapiro and Stockman, “Computer Vision”, 2001



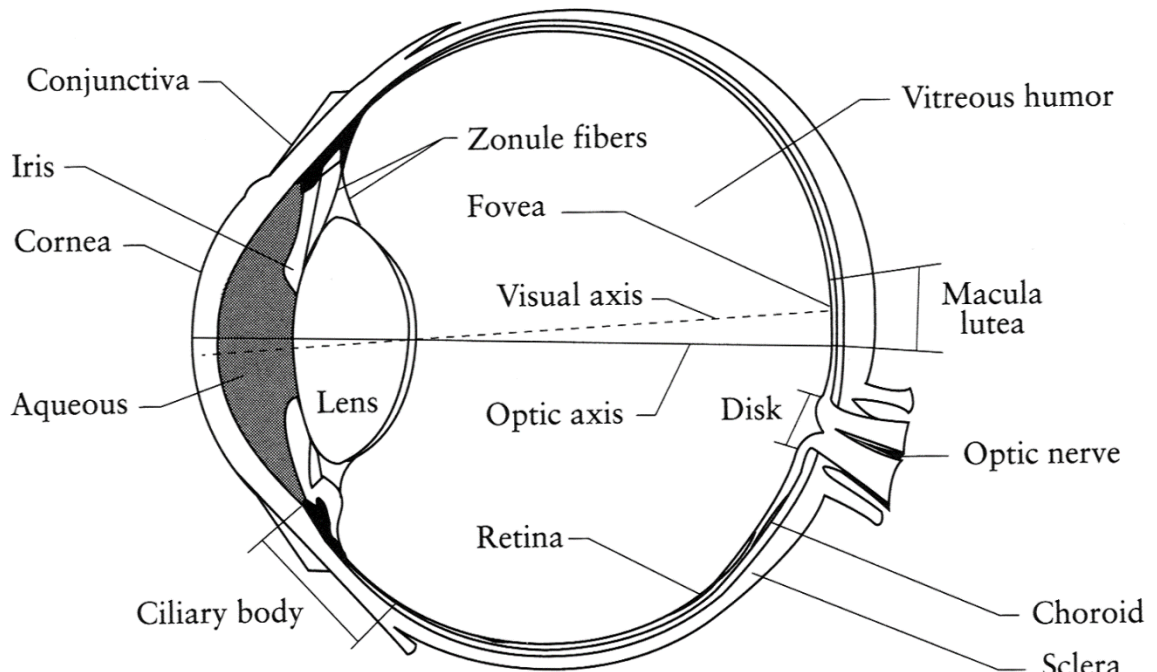
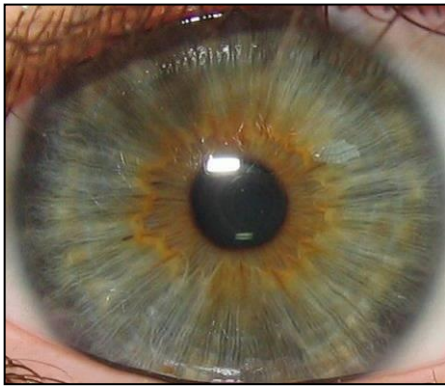
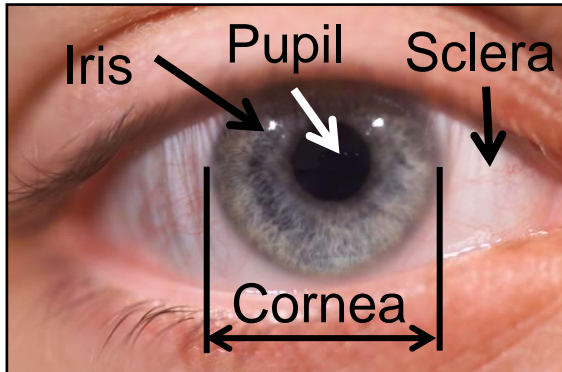
Components of a Computer Vision System



Topic: The Human Visual System

- 'Computer Vision'?
- **The Human Visual System**
- Image Capturing Systems

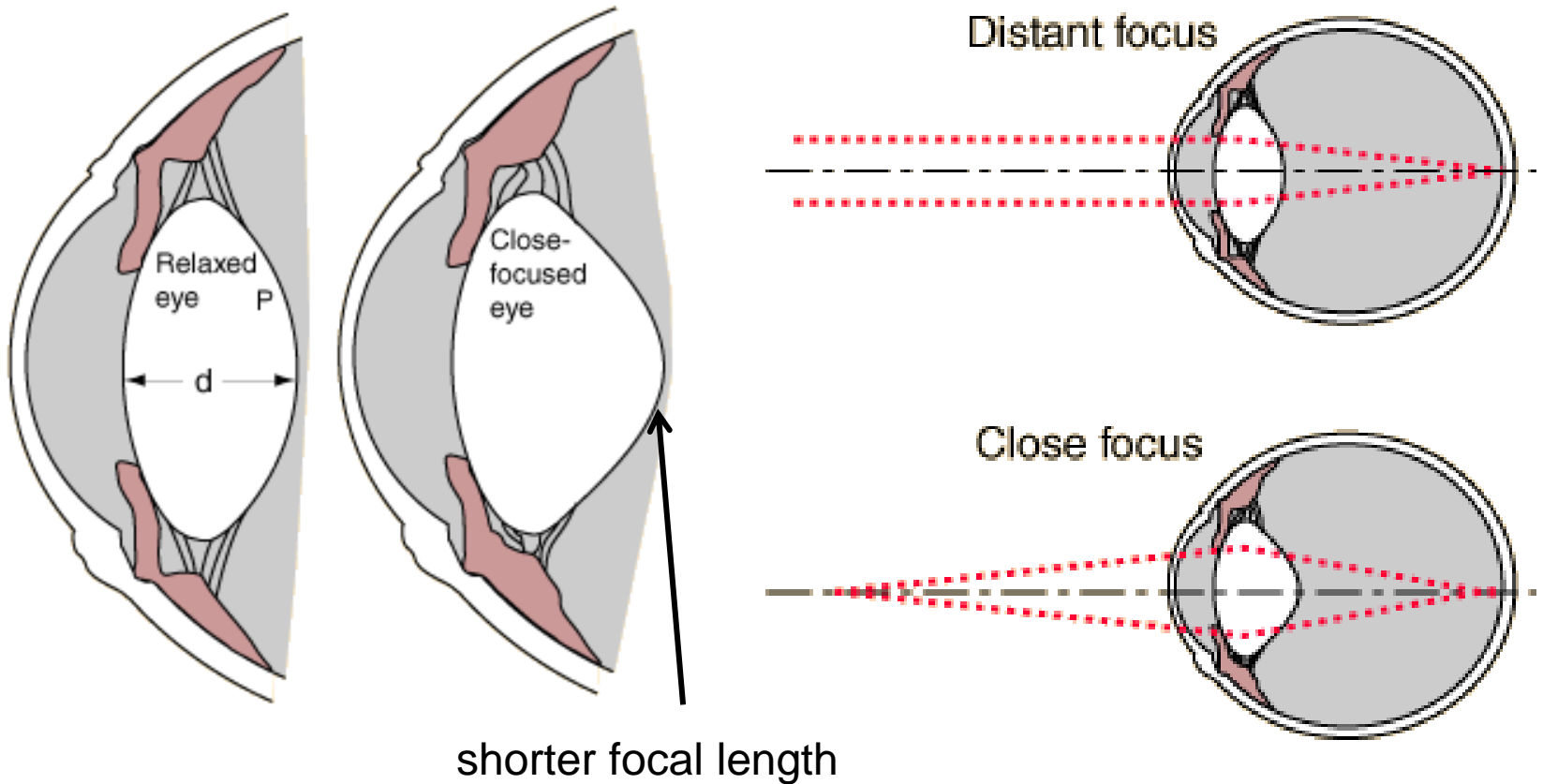
Our Eyes



Iris is the diaphragm that changes the aperture (pupil)

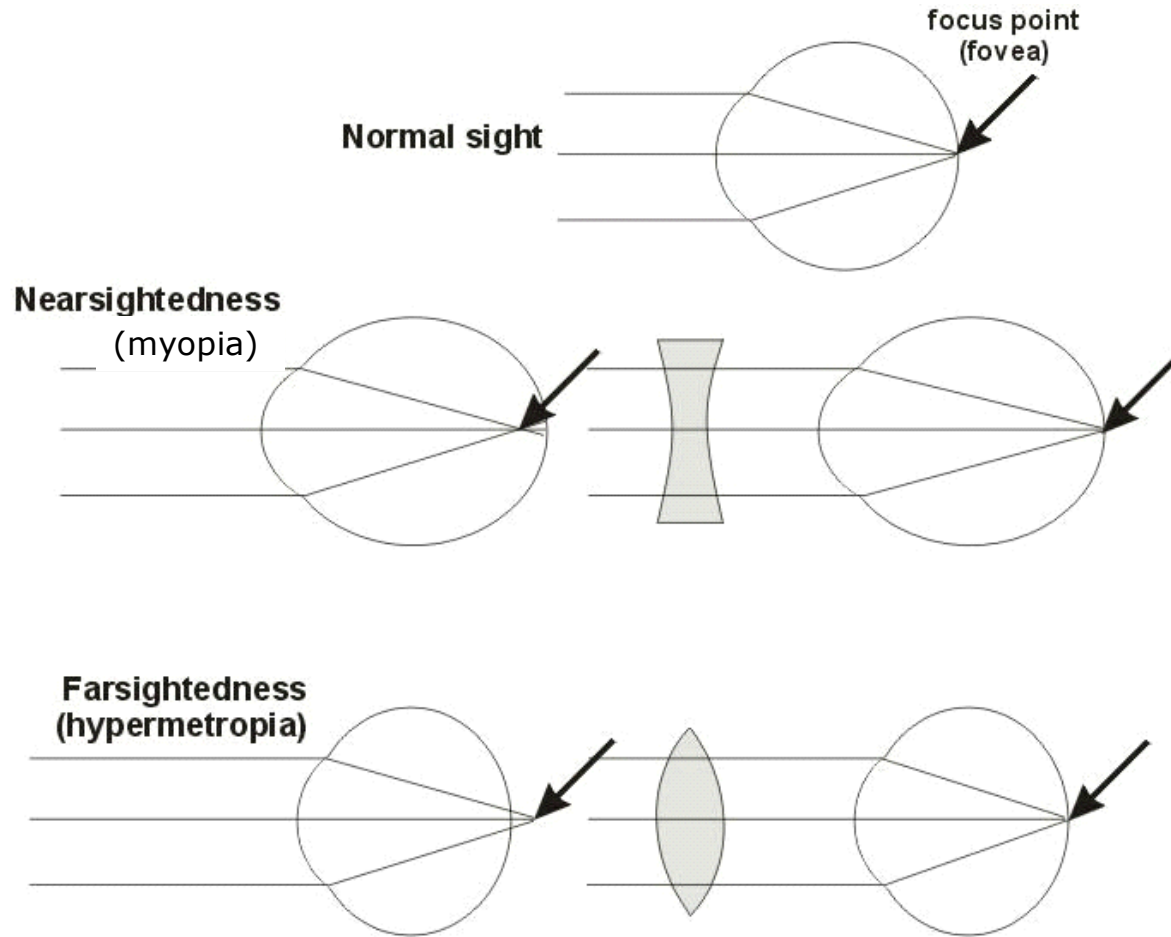
Retina is the sensor where the fovea has the highest resolution

Focusing



Changes the focal length of the lens

Myopia and Hyperopia



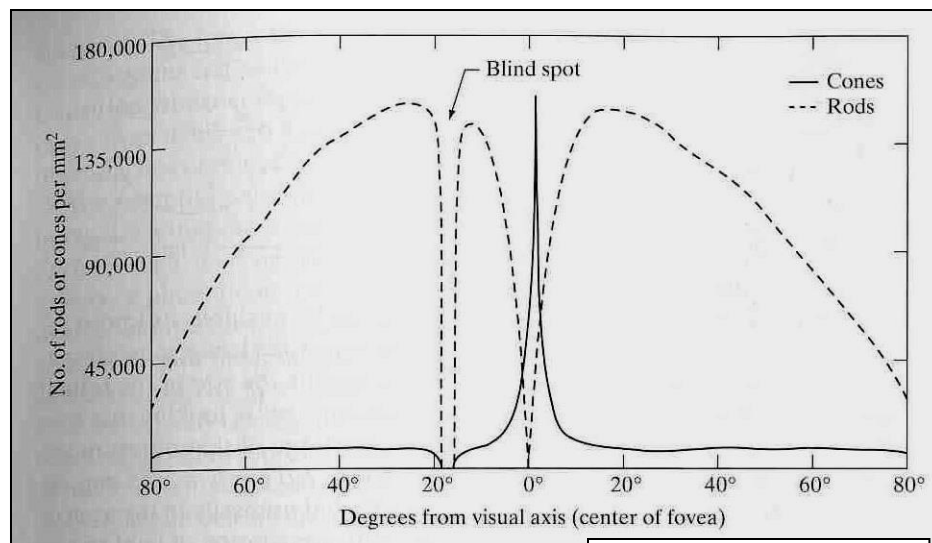
Blind Spot in the Eye



Close your right eye and look directly at the “+”

Colour

- **Our retina has:**
 - **Cones** – Measure the frequency of light (colour)
 - 6 to 7 millions
 - High-definition
 - Need high luminosity
 - **Rods** – Measure the intensity of light (luminance)
 - 75 to 150 millions
 - Low-definition
 - Function with low luminosity



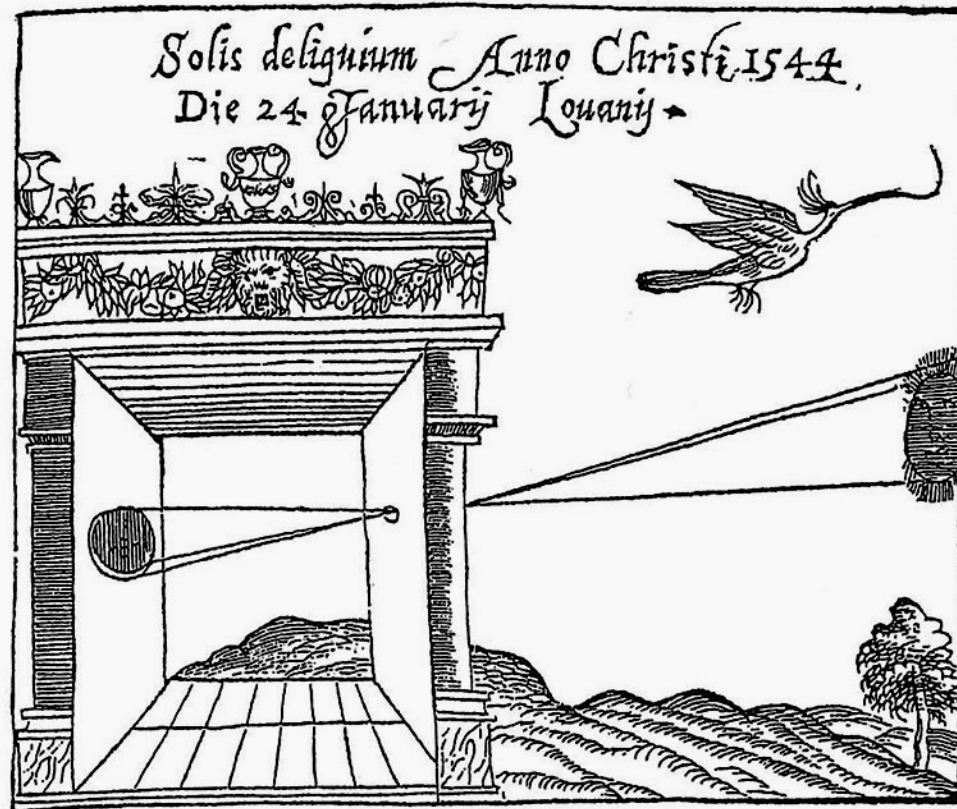
Gonzalez & Woods

We only see colour in the centre of our retina!

Topic: Image Capturing Systems

- 'Computer Vision'?
- The Human Visual System
- **Image Capturing Systems**

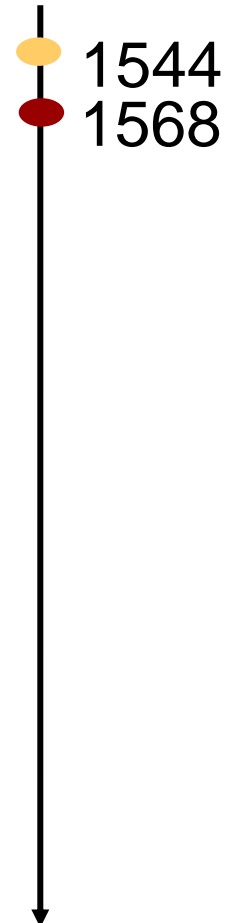
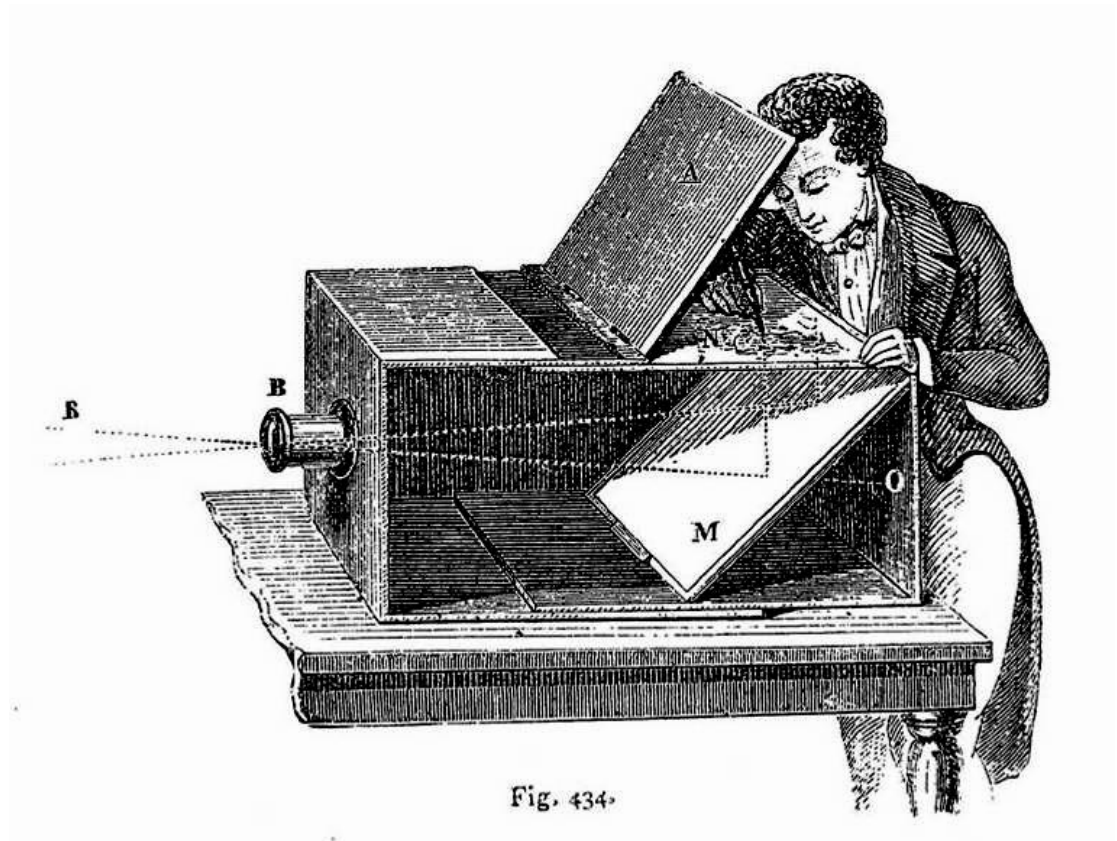
A Brief History of Images



1544

Camera Obscura, Gemma Frisius, 1544

A Brief History of Images

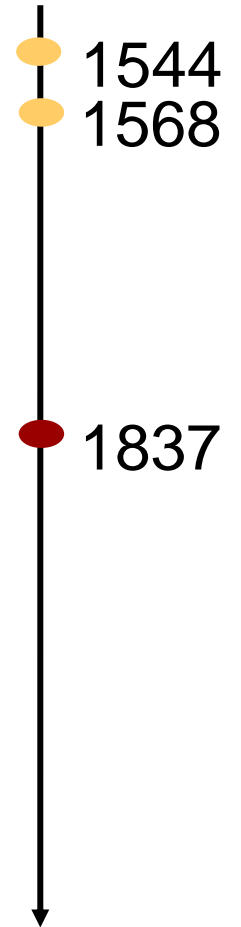


Lens Based Camera Obscura, 1568

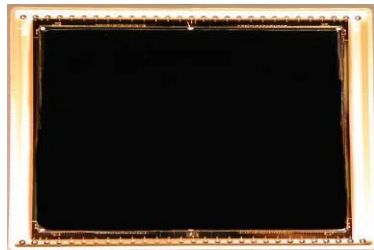
A Brief History of Images



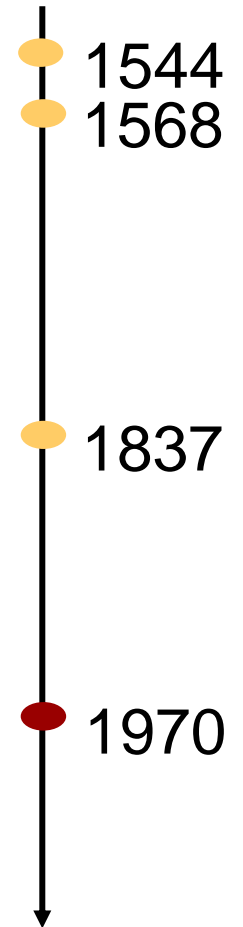
Still Life, Louis Jaques Mande Daguerre, 1837



A Brief History of Images



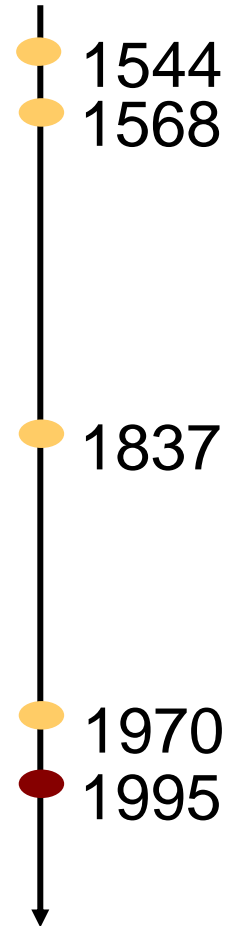
Silicon Image Detector, 1970



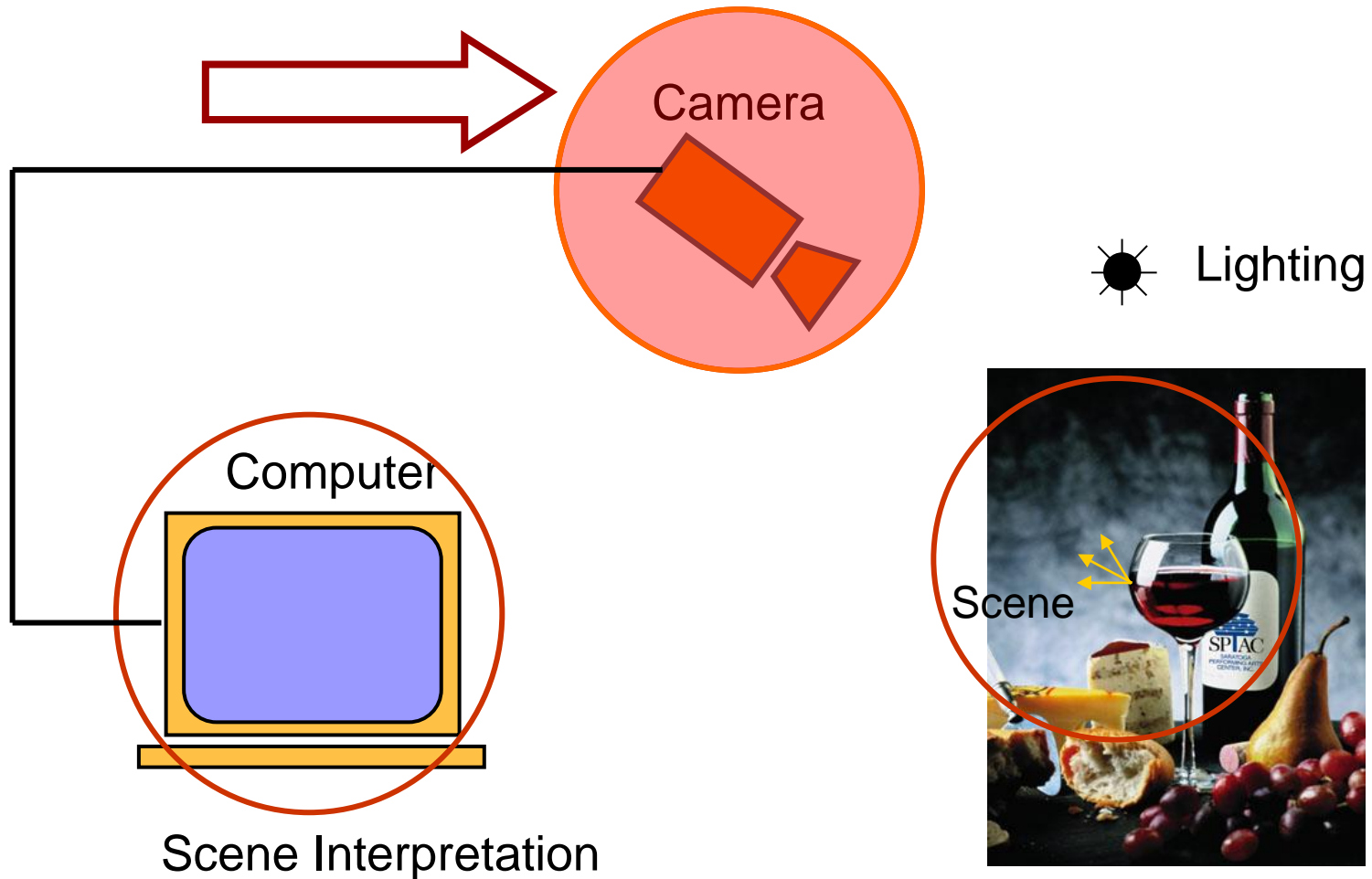
A Brief History of Images



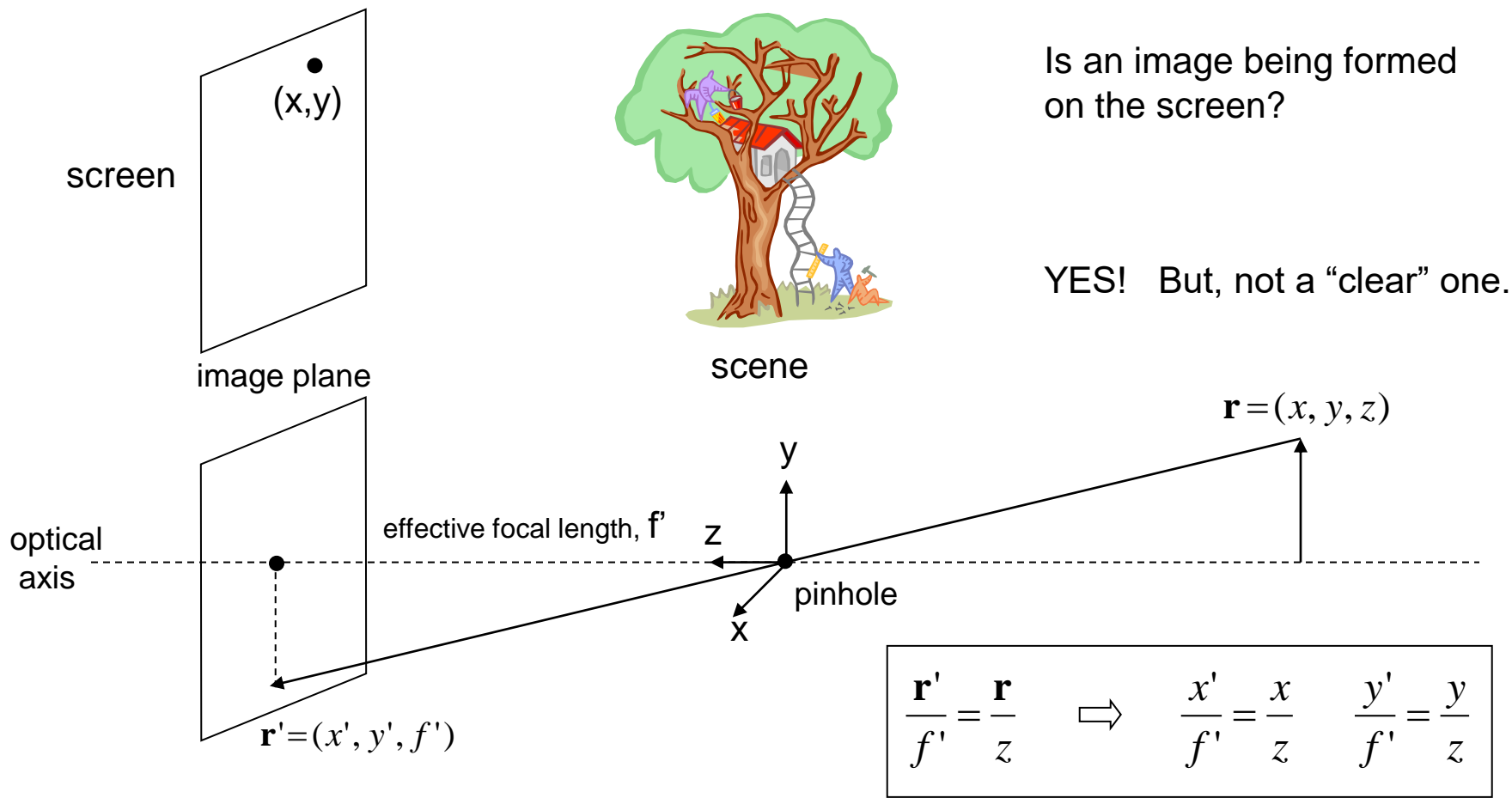
Digital Cameras



Components of a Computer Vision System

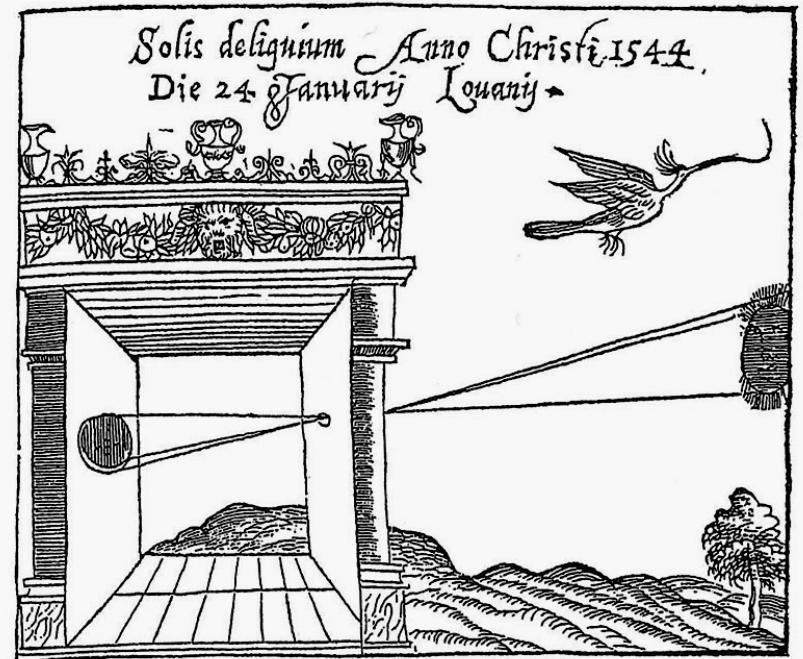


Pinhole and the Perspective Projection



Pinhole Camera

- Basically a pinhole camera is a box, with a tiny hole at one end and film or photographic paper at the other.
- Mathematically: out of all the light rays in the world, choose the set of light rays passing through a point and projecting onto a plane.



Pinhole Photography



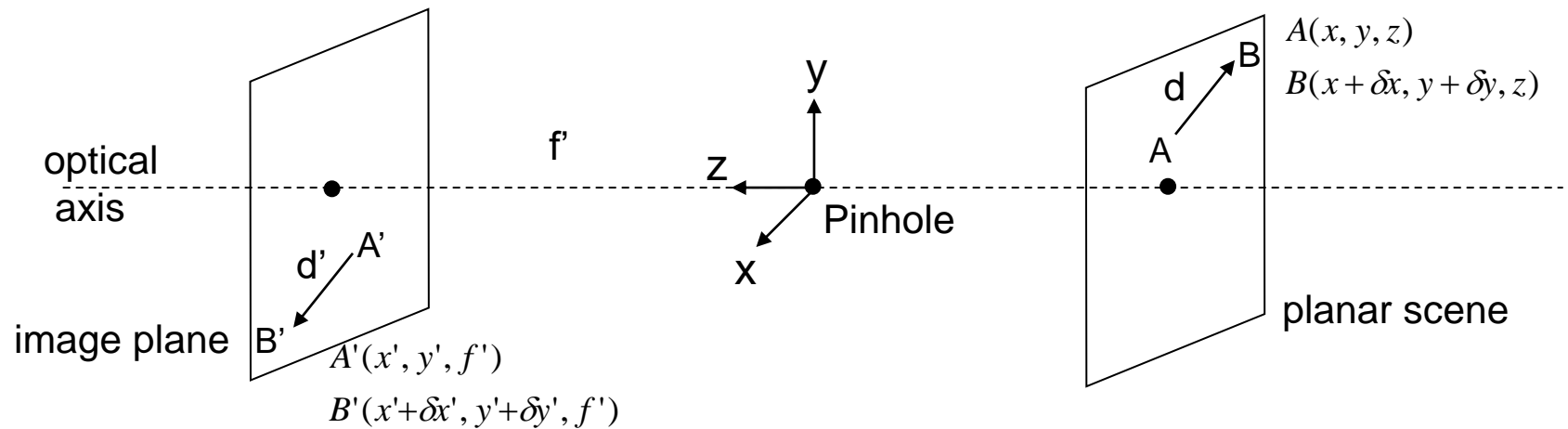
©Charlotte Murray Untitled, 4" x 5" pinhole photograph, 1992



Image Size inversely proportional to Distance

Reading: <http://www.pinholeresource.com/>

Magnification



From perspective projection:

$$\frac{x'}{f'} = \frac{x}{z} \quad \frac{y'}{f'} = \frac{y}{z}$$



Magnification:

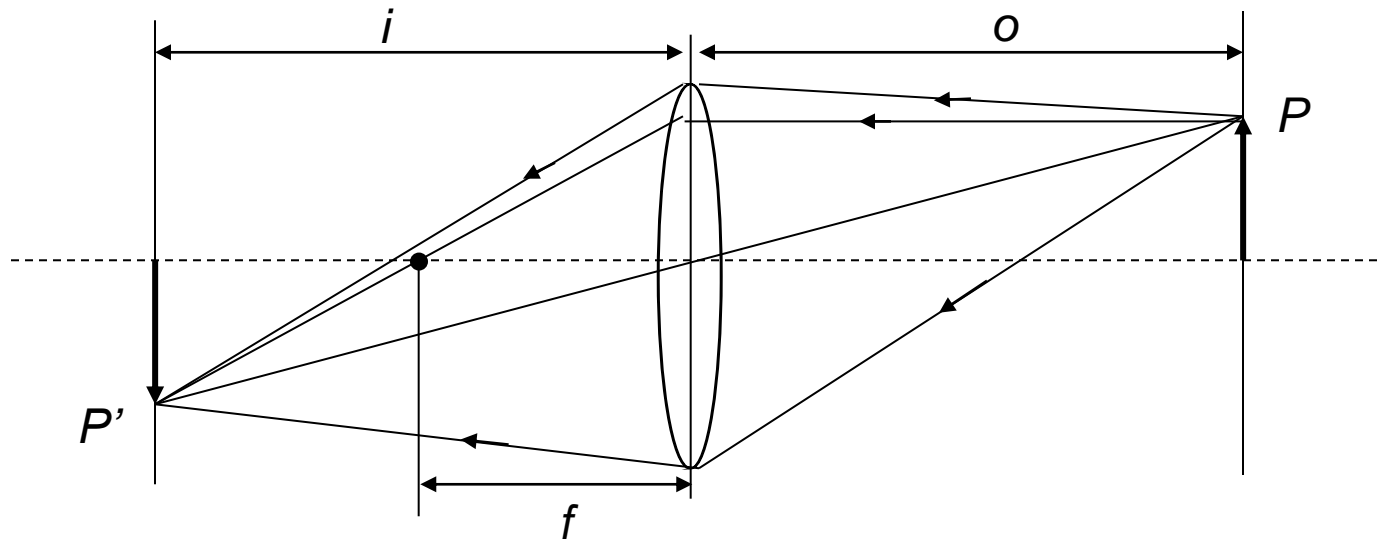
$$m = \frac{d'}{d} = \frac{\sqrt{(\Delta x')^2 + (\Delta y')^2}}{\sqrt{(\Delta x)^2 + (\Delta y)^2}} = \frac{f'}{z}$$

$$\frac{x' + \Delta x'}{f'} = \frac{x + \Delta x}{z} \quad \frac{y' + \Delta y'}{f'} = \frac{y + \Delta y}{z}$$

$$\frac{Area_{image}}{Area_{scene}} = m^2$$

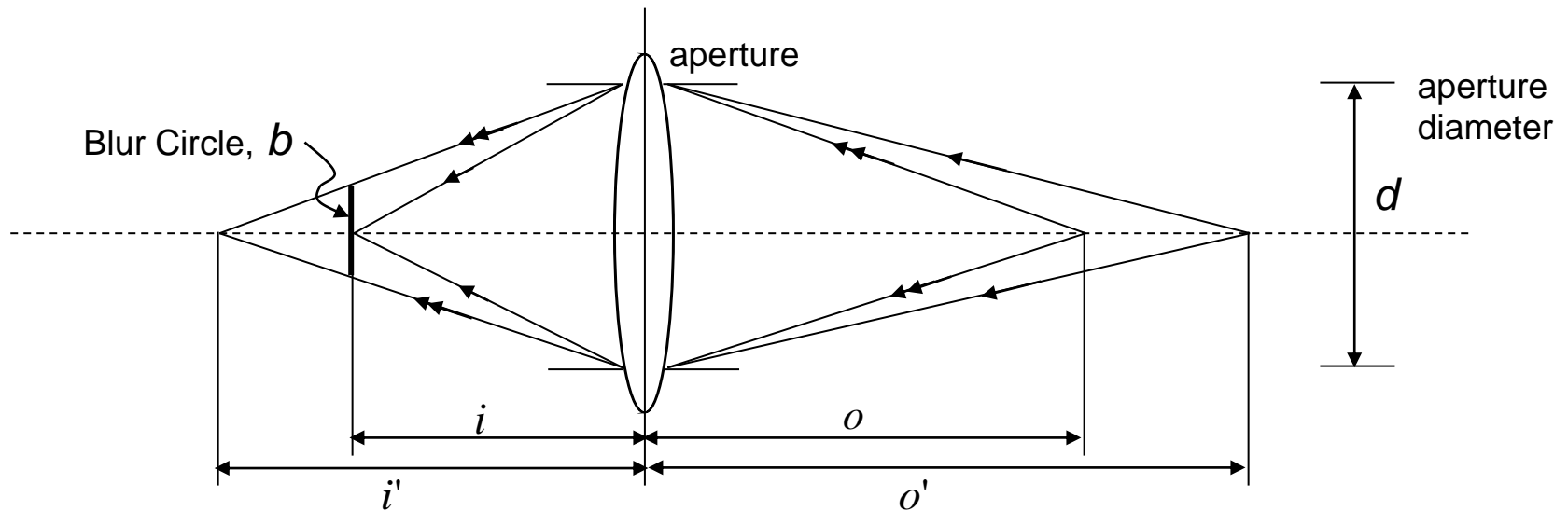
Image Formation using Lenses

- Lenses are used to avoid problems with pinholes.
- Ideal Lens: Same projection as pinhole but gathers more light!



- Gaussian Thin Lens Formula: $\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$
- f is the focal length of the lens – determines the lens's ability to refract light

Focus and Defocus



- Gaussian Law:

$$\frac{1}{i} + \frac{1}{o} = \frac{1}{f}$$



$$(i' - i) = \frac{f}{(o' - f)} \frac{f}{(o - f)} (o - o')$$

$$\frac{1}{i'} + \frac{1}{o'} = \frac{1}{f}$$

- In theory, only one scene plane is in focus

Depth of Field

- Range of object distances over which image is sufficiently well focused
- Range for which *blur circle* is less than the resolution of the sensor



http://images.dpchallenge.com/images_portfolio/27920/print_preview/116336.jpg

Image Sensors

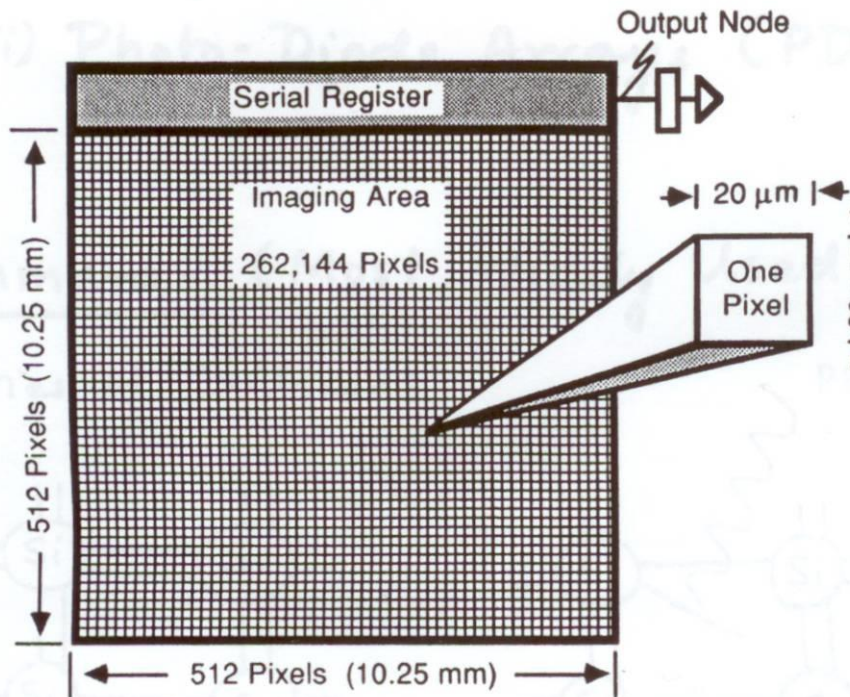


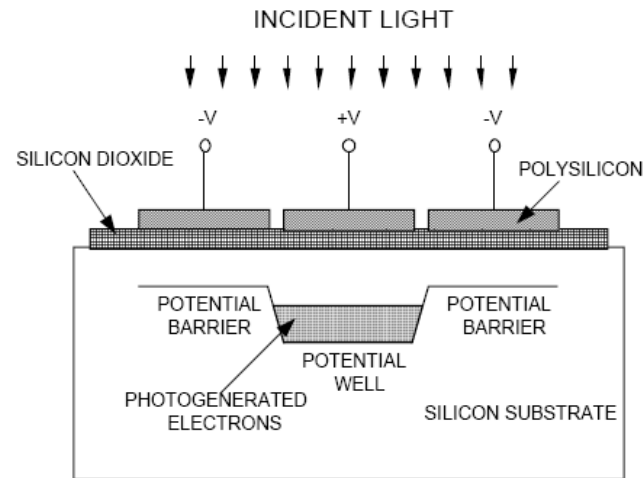
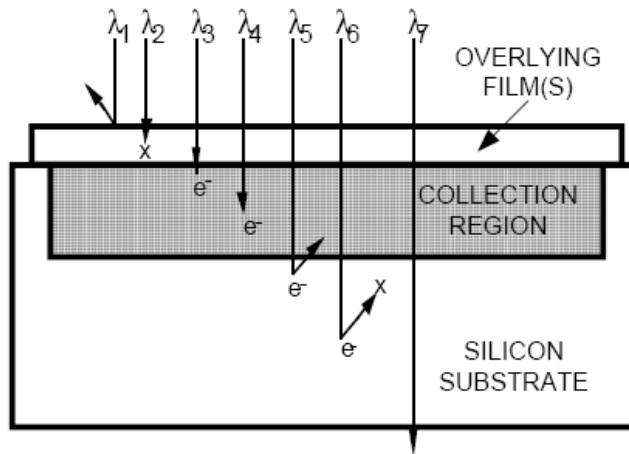
FIG. 4. Typical 512 × 512 CCD.

Considerations

- Speed
- Resolution
- Signal / Noise Ratio
- Cost

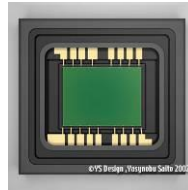
Image Sensors

- Convert light into an electric charge



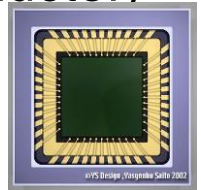
CCD (charge coupled device)

- Higher dynamic range
- High uniformity
- Lower noise



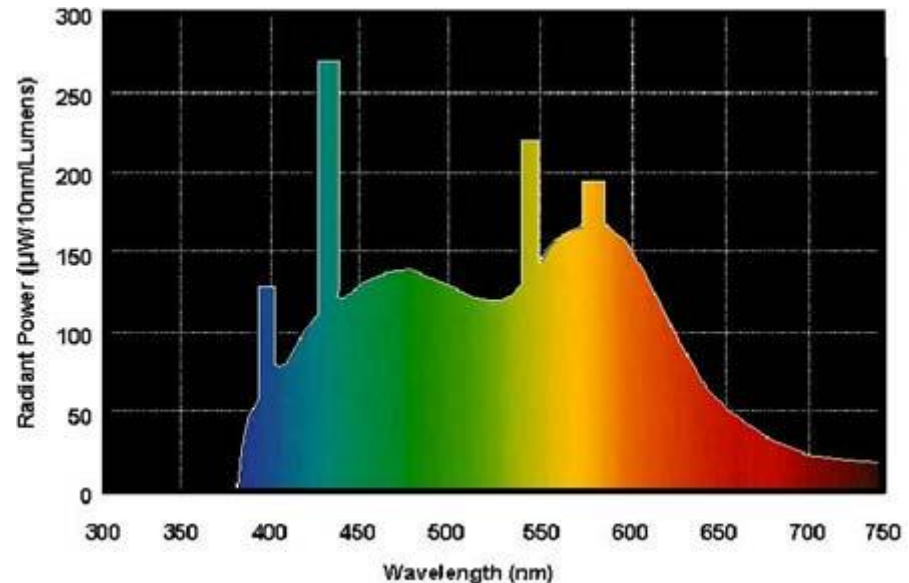
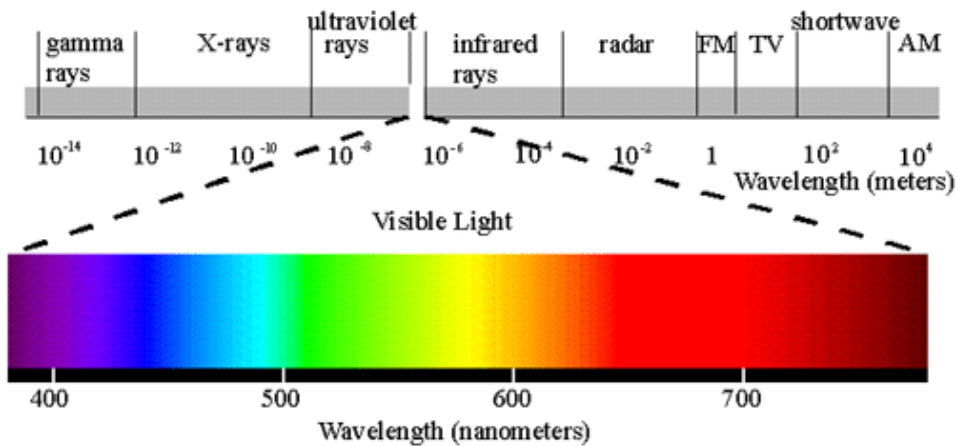
CMOS (complementary metal
Oxide semiconductor)

- Lower voltage
- Higher speed
- Lower system complexity



Sensing Brightness

Incoming light has a **spectral distribution** $p(\lambda)$

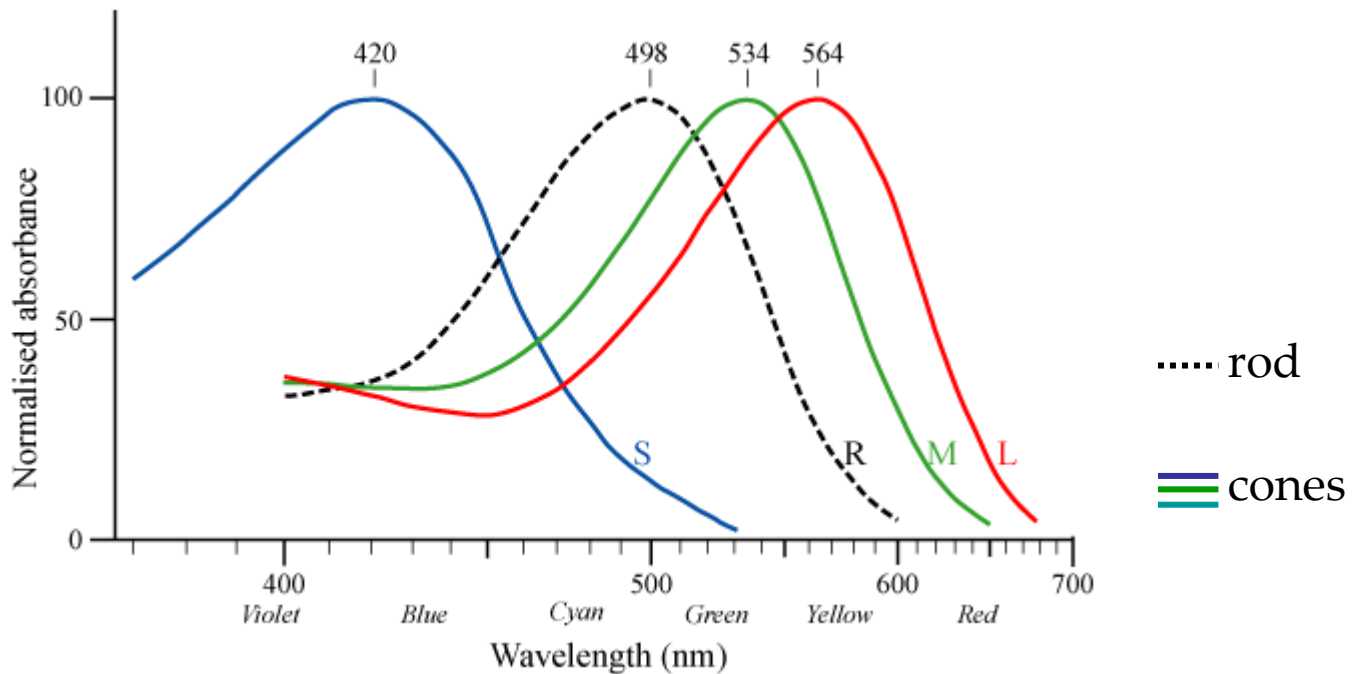


So the pixel intensity becomes

$$I = k \int_{-\infty}^{\infty} q(\lambda)p(\lambda)d\lambda$$

How do we sense colour?

- Do we have infinite number of filters?

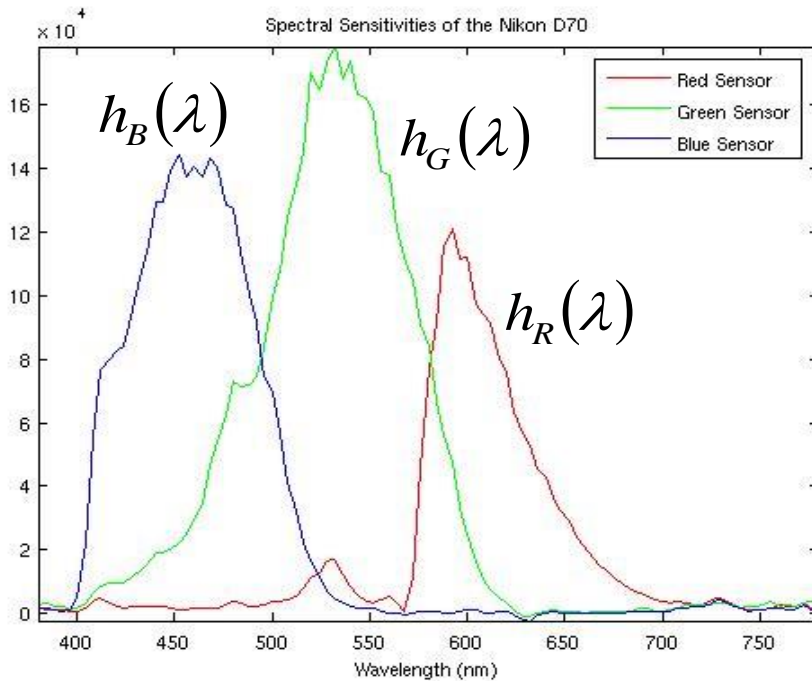


Three filters of different spectral responses

Sensing Colour

- **Tristimulus (trichromatic) values** (I_R, I_G, I_B)

Camera's spectral response functions: $h_R(\lambda), h_G(\lambda), h_B(\lambda)$

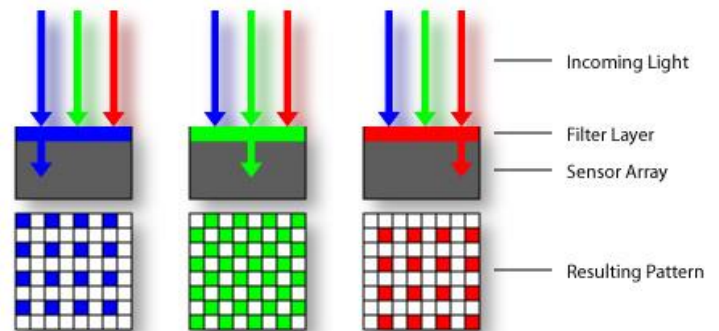
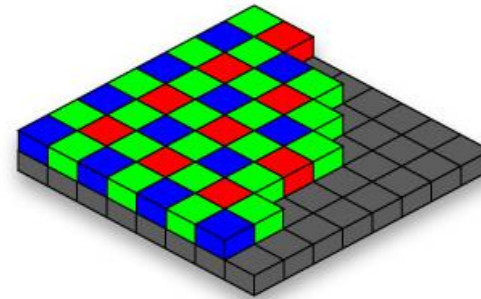
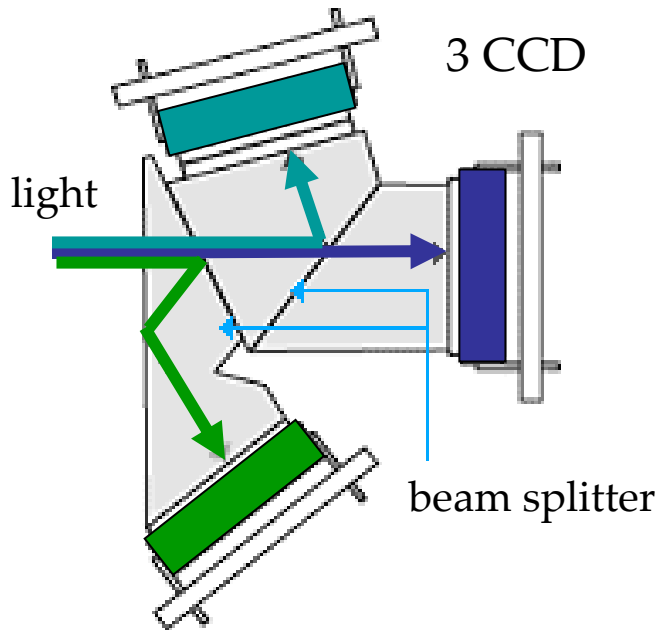


$$I_R = k \int_{-\infty}^{\infty} h_R(\lambda) p(\lambda) d\lambda$$

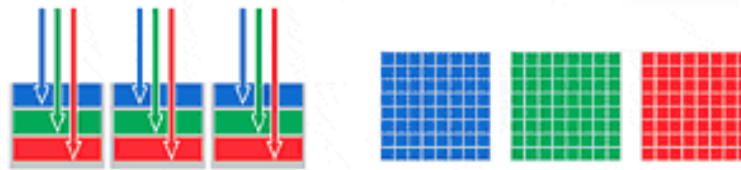
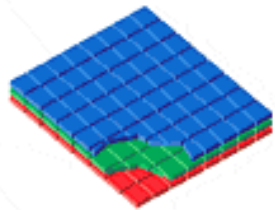
$$I_G = k \int_{-\infty}^{\infty} h_G(\lambda) p(\lambda) d\lambda$$

$$I_B = k \int_{-\infty}^{\infty} h_B(\lambda) p(\lambda) d\lambda$$

Sensing Colour



Bayer pattern



Foveon X3™

Resources

- Szeliski, “Computer Vision: Algorithms and Applications”, Springer, 2011
 - Chapter 1 – “Introduction”
 - Chapter 2 – “Image Formation”