

On Combining Linear-Based Strategies For Tabled Evaluation of Logic Programs

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Tabling in Logic Programming

- Tabling is an implementation technique that overcomes some of the limitations of SLD resolution.
 - ◆ **Positive Infinite Cycles** (insufficient expressiveness)
 - ◆ **Negative Infinite Cycles** (inconsistence)
 - ◆ **Redundant Computations** (inefficiency)
- Implementations of tabling are currently available in systems like XSB Prolog, Yap Prolog, B-Prolog, ALS-Prolog, Mercury and more recently Ciao Prolog.

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- Implementations of tabling are currently available in systems like XSB Prolog, Yap Prolog, B-Prolog, ALS-Prolog, Mercury and more recently Ciao Prolog.
- In these implementations, we can distinguish two main categories of tabling mechanisms:
 - ◆ **Suspension-Based Tabling**: can be seen as a sequence of sub-computations that can be suspended and later resumed, when necessary, to compute fix-points (XSB Prolog, Yap Prolog, Mercury and Ciao Prolog).
 - ◆ **Linear Tabling**: can be seen as a single execution tree where tabled subgoals use iterative computations, without requiring suspension and resumption, to compute fix-points (B-Prolog, ALS Prolog and Yap Prolog).

Linear Tabling

- The two most well-known linear tabling strategies are:
 - ◆ **DRE (Dynamic Reordering of Execution)**: repeated calls, **the followers**, execute from the backtracking point of the former call. A follower is then repeatedly re-executed, until all the available answers and clauses have been exhausted, that is, until a fix-point is reached (B-Prolog and Yap Prolog).
 - ◆ **DRA (Dynamic Reordering of Alternatives)**: tables not only the answers to tabled subgoals, but also the alternatives leading to repeated calls, the **looping alternatives**. It then uses the looping alternatives to repeatedly recompute them until reaching a fix-point (ALS Prolog and Yap Prolog).

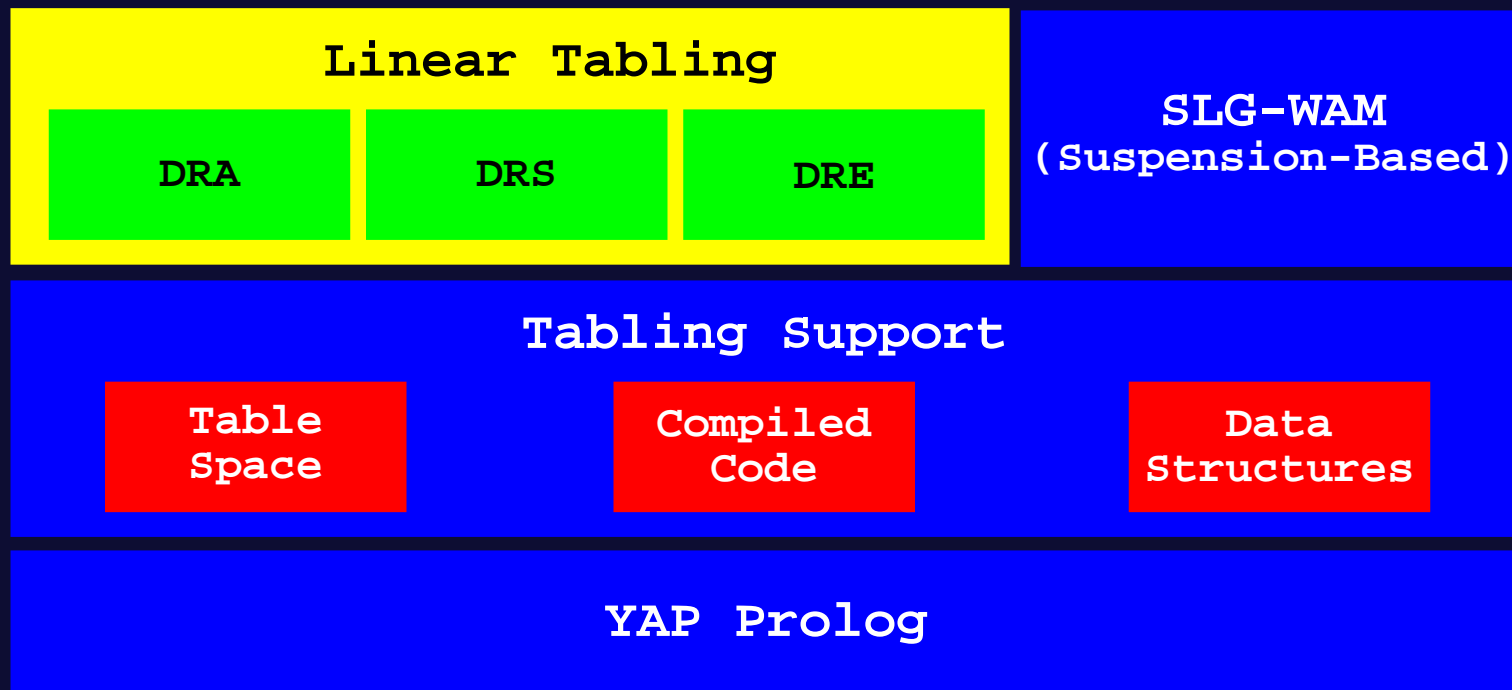
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 - ◆ **DRA (Dynamic Reordering of Alternatives)**: tables not only the answers to tabled subgoals, but also the alternatives leading to repeated calls, the **looping alternatives**. It then uses the looping alternatives to repeatedly recompute them until reaching a fix-point (ALS Prolog and Yap Prolog).

- In this work, we also propose a new linear tabling strategy:
 - ◆ **DRS (Dynamic Reordering of Solutions)**: it can be seen as a variant of the DRA strategy, but applied to the consumption of solutions. The key idea is to memorize the solutions leading to consumer calls, the **looping solutions**, and use them as the DRA strategy uses the looping alternatives (Yap Prolog).

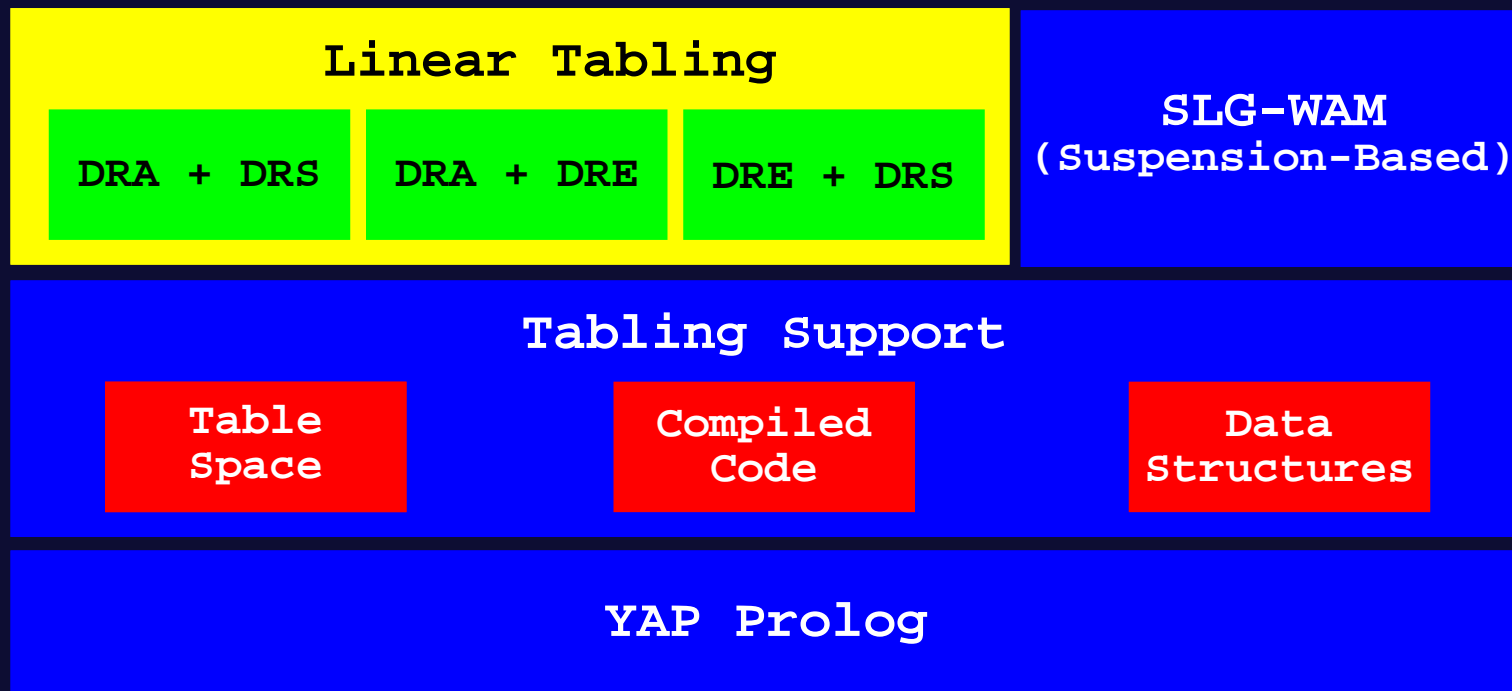
Our Goal

- Implement a framework on top of the **Yap Prolog system**, that supports the **combination of the three strategies**.
- Analyze the **advantages and weaknesses** of each strategy, when used **solely or combined** with the others.



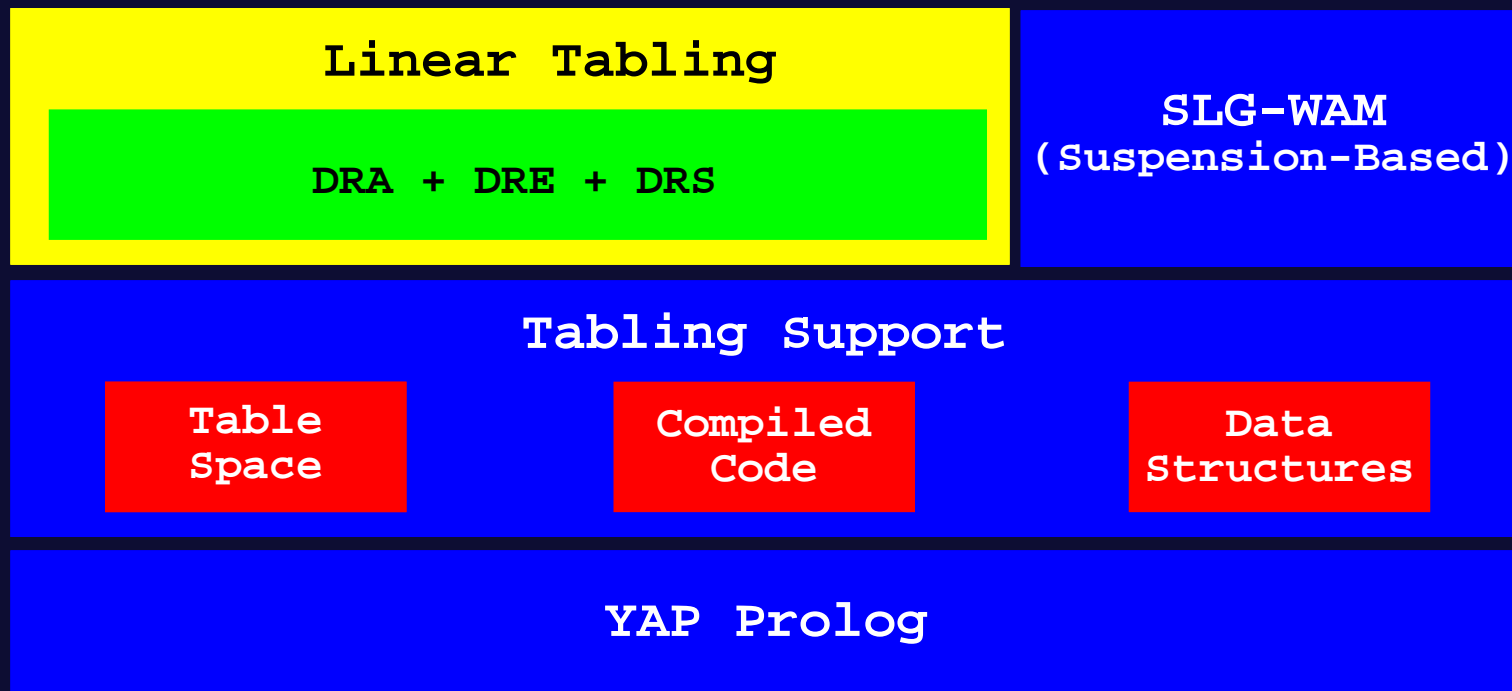
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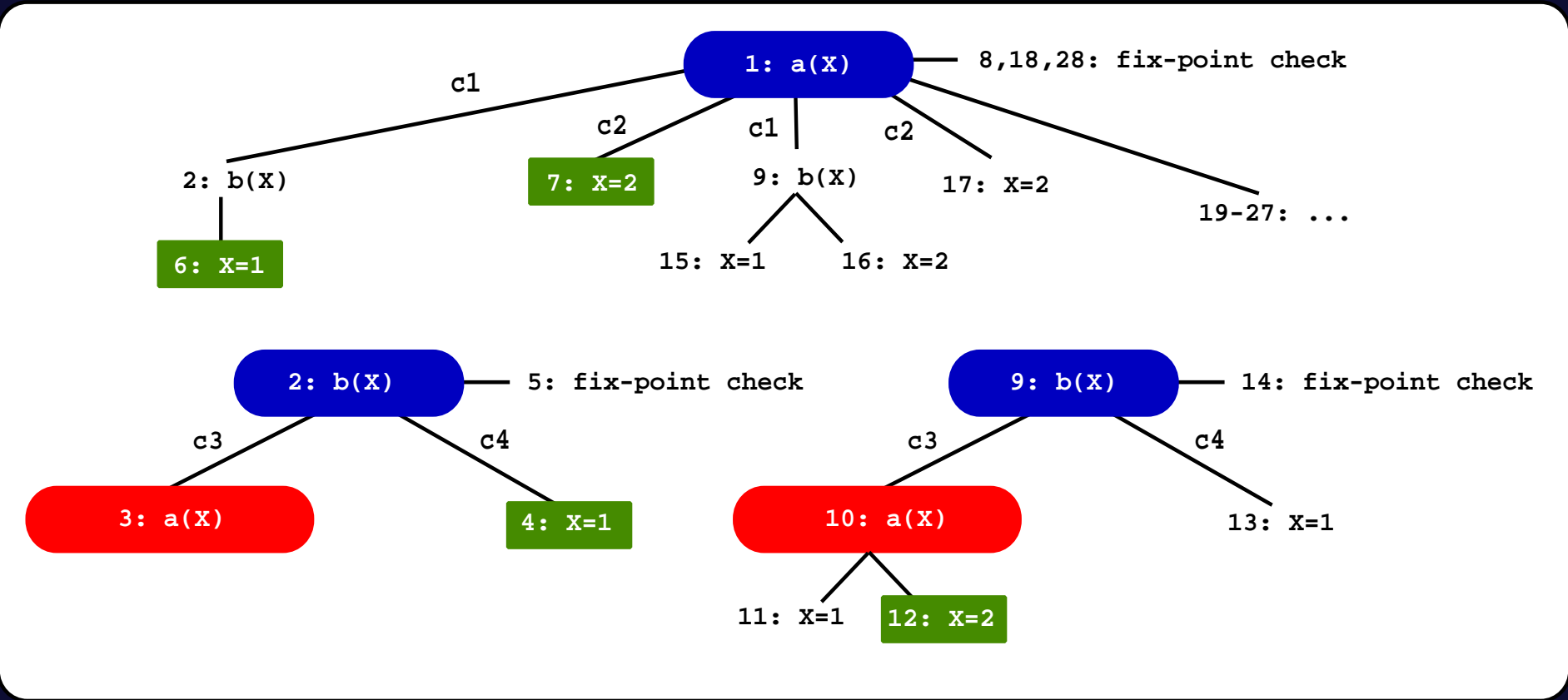
Evaluation Example I - Standard Linear Tabling

```

:- table a/1, b/1.

a(X):- b(X).      (c1)
a(2).             (c2)
b(X):- a(X).      (c3)
b(1).             (c4)
    
```

Call	Solutions
1: a(X)	6: X=1 7: X=2
2: b(X)	4: X=1 12: X=2



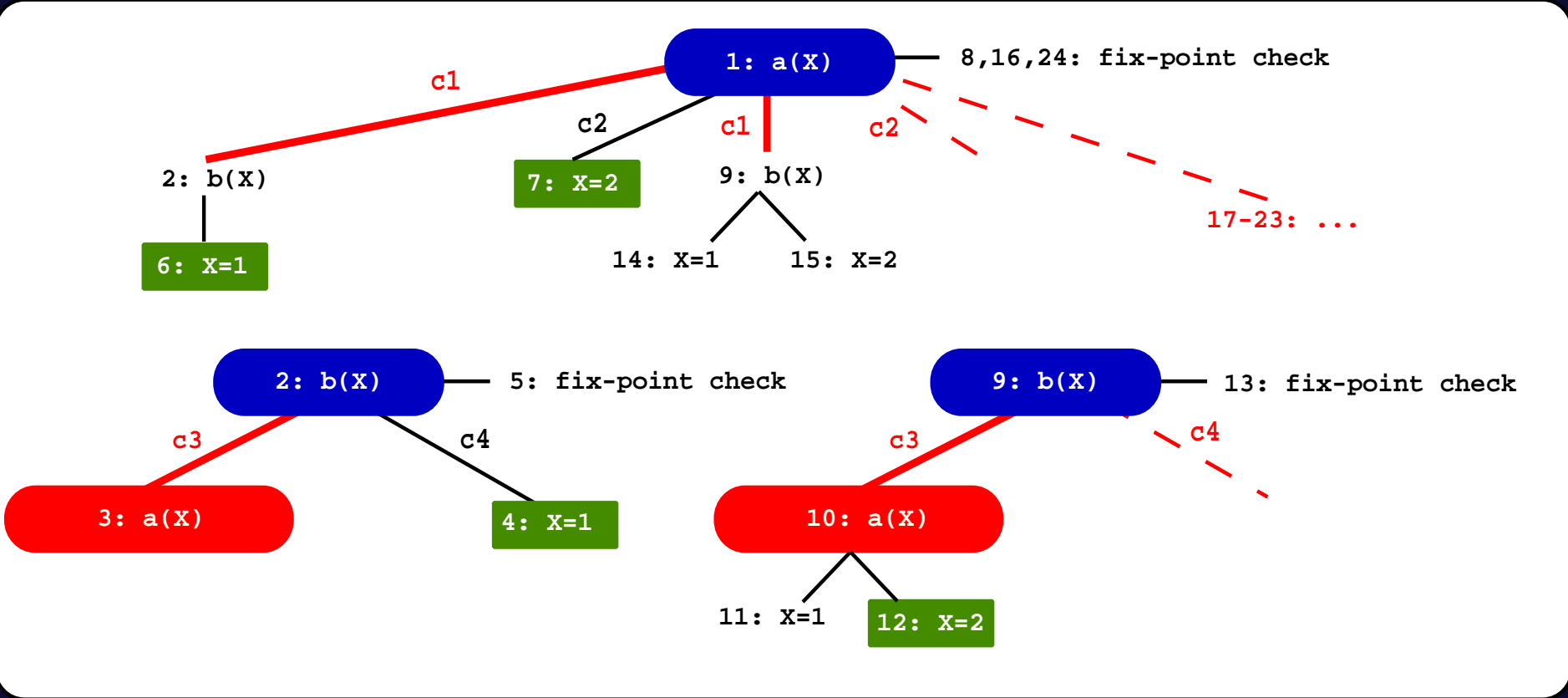
Evaluation Example I - DRA

```

:- table a/1, b/1.

a(X):- b(X).      (c1)
a(2).             (c2)
b(X):- a(X).      (c3)
b(1).             (c4)
    
```

Call	Solutions	Looping Alternatives
1: a(X)	6: X=1 7: X=2	3: c1
2: b(X)	4: X=1 12: X=2	3: c3



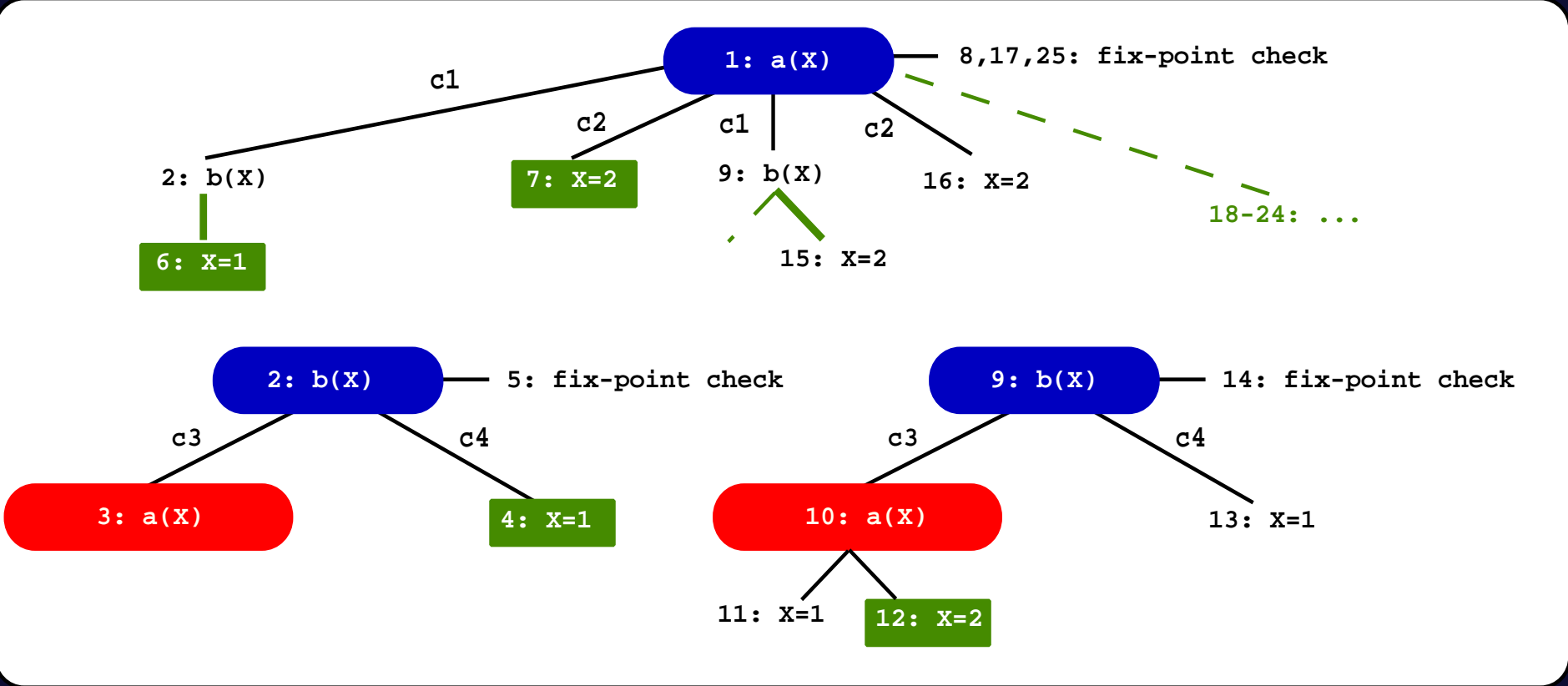
Evaluation Example I - DRS

```

:- table a/1, b/1.

a(X):- b(X).      (c1)
a(2).            (c2)
b(X):- a(X).      (c3)
b(1).            (c4)
    
```

Call	Solutions	Looping Solutions
1: a(X)	6: X=1 7: X=2	
2: b(X)	4: X=1 12: X=2	

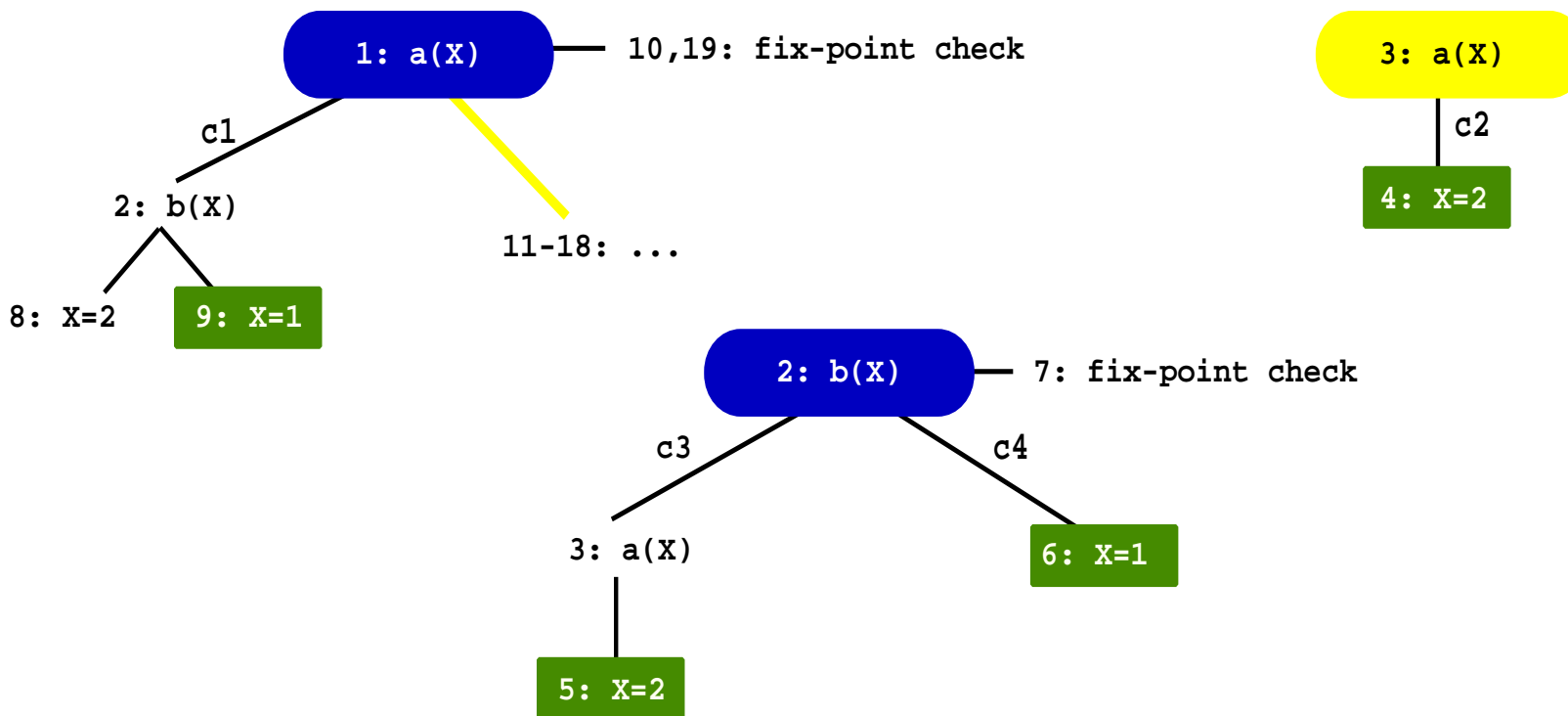


Evaluation Example I - DRE

```
:- table a/1, b/1.
```

```
a(X):- b(X).      (c1)
a(2).             (c2)
b(X):- a(X).      (c3)
b(1).             (c4)
```

Call	Solutions
1: a(X)	4: X=2 9: X=1
2: b(X)	5: X=2 6: X=1

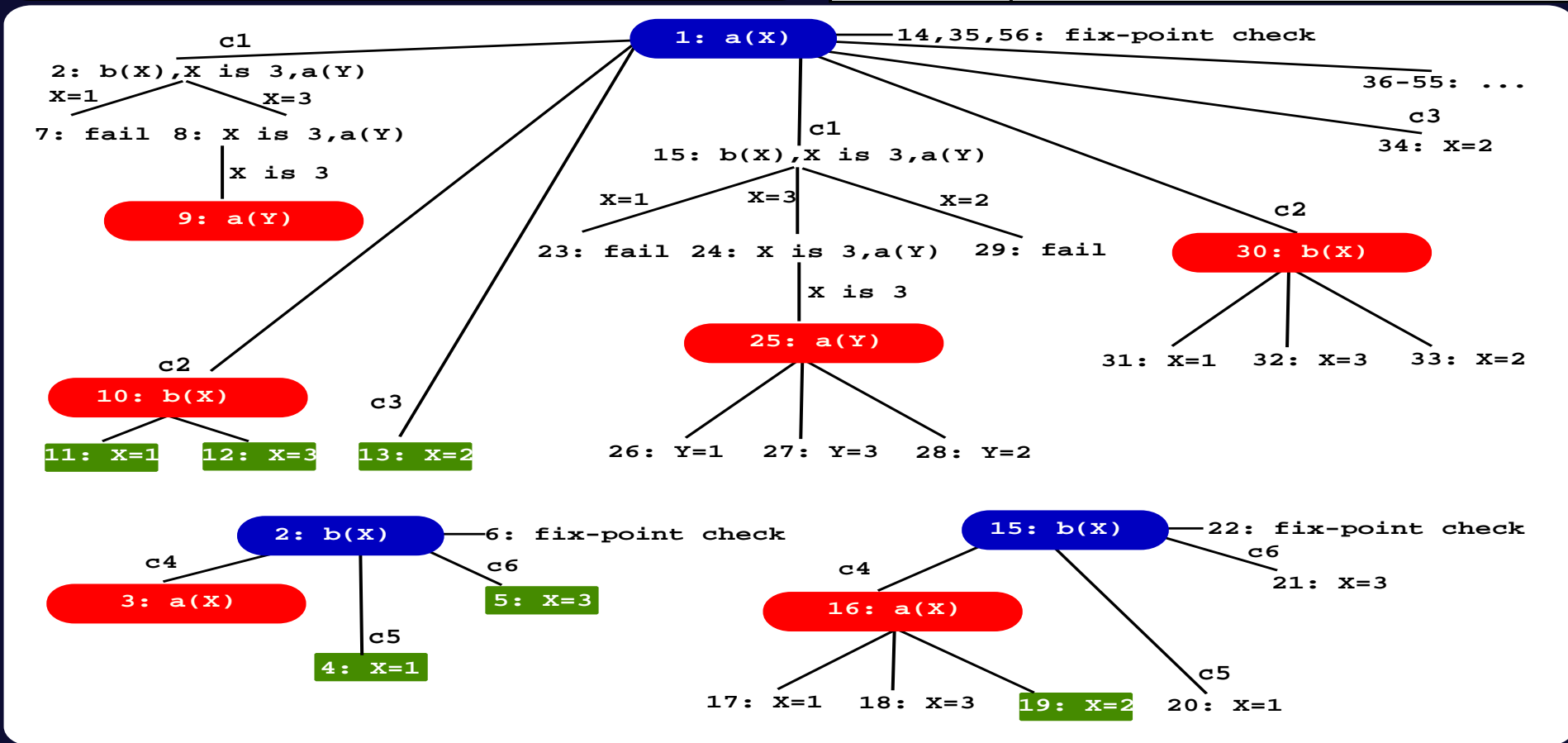


Evaluation Example II - Standard Linear Tabling

```
:-table a/1,b/1.
a(X):-b(X),X is 3,a(Y).
a(X):-b(X).
a(2).
b(X):-a(X).
b(1).
b(3).
```

- (c1)
- (c2)
- (c3)
- (c4)
- (c5)
- (c6)

Call	Solutions
1: a(X)	11: X=1 12: X=3 13: X=2
2: b(X)	4: X=1 5: X=3 19: X=2

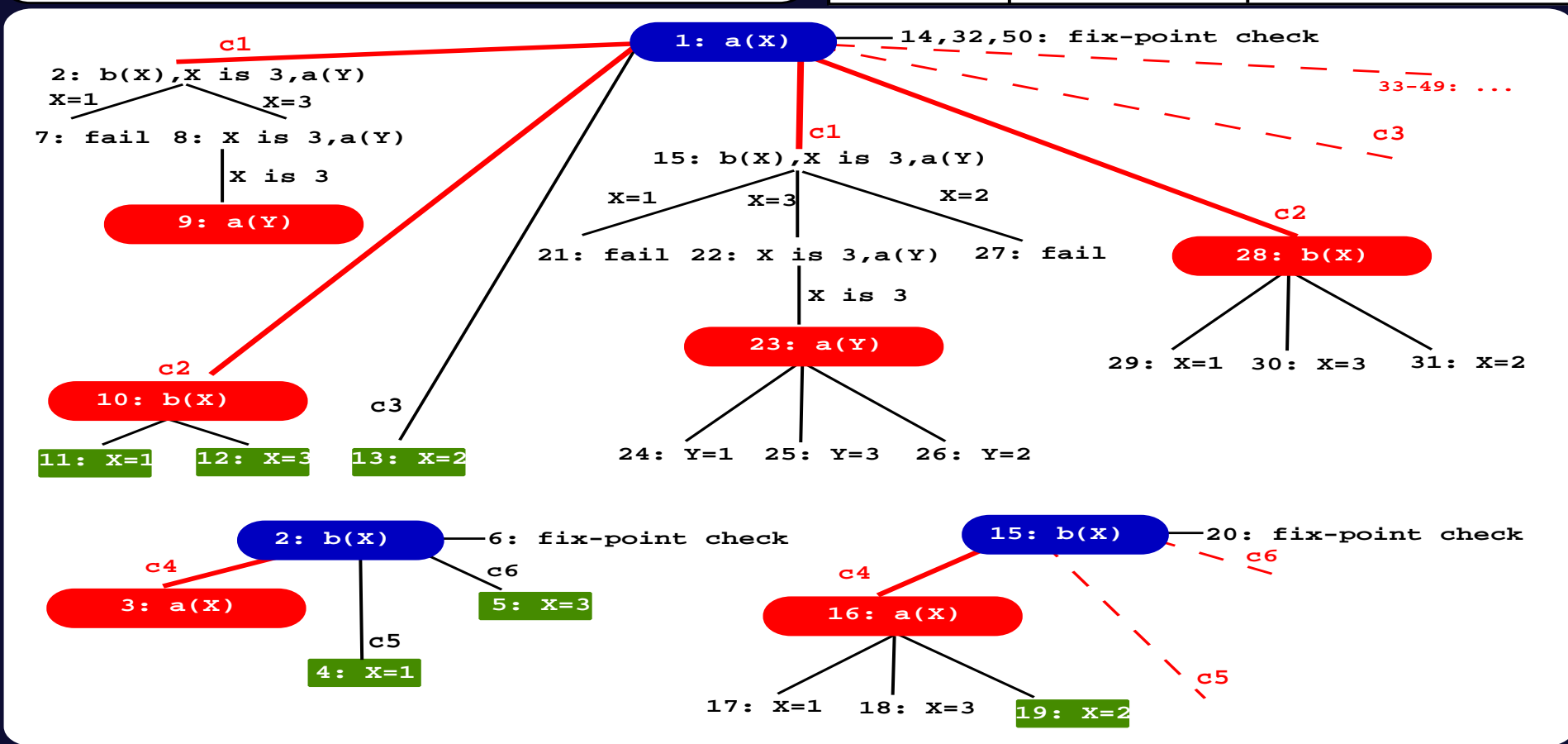


Evaluation Example II - DRA

```
:-table a/1,b/1.
a(X):-b(X),X is 3,a(Y).
a(X):-b(X).
a(2).
b(X):-a(X).
b(1).
b(3).
```

- (c1)
- (c2)
- (c3)
- (c4)
- (c5)
- (c6)

Call	Solutions	Loop Alt
1: a(X)	11: X=1 12: X=3 13: X=2	3: c1 10: c2
2: b(X)	4: X=1 5: X=3 19: X=2	3: c4



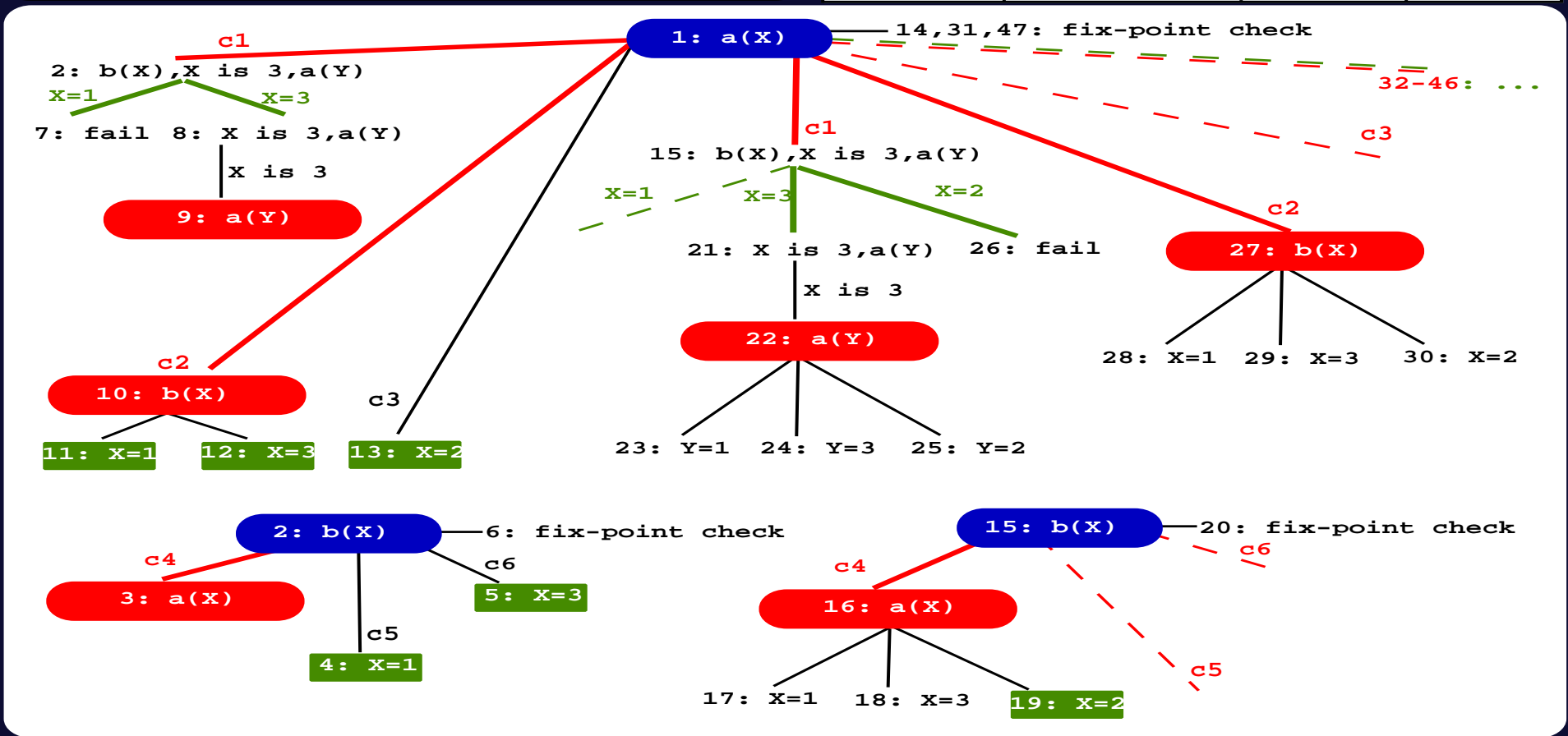
Evaluation Example II - DRA + DRS

```

:-table a/1,b/1.
a(X):-b(X),X is 3,a(Y).
a(X):-b(X).
a(2).
b(X):-a(X).
b(1).
b(3).
    
```

- (c1)
- (c2)
- (c3)
- (c4)
- (c5)
- (c6)

Call	Solutions	Loop Alt	Loop Sol
1: a(X)	11: X=1 12: X=3 13: X=2	3: c1 10: c2	
2: b(X)	4: X=1 5: X=3 19: X=2	3: c4	9: X=3

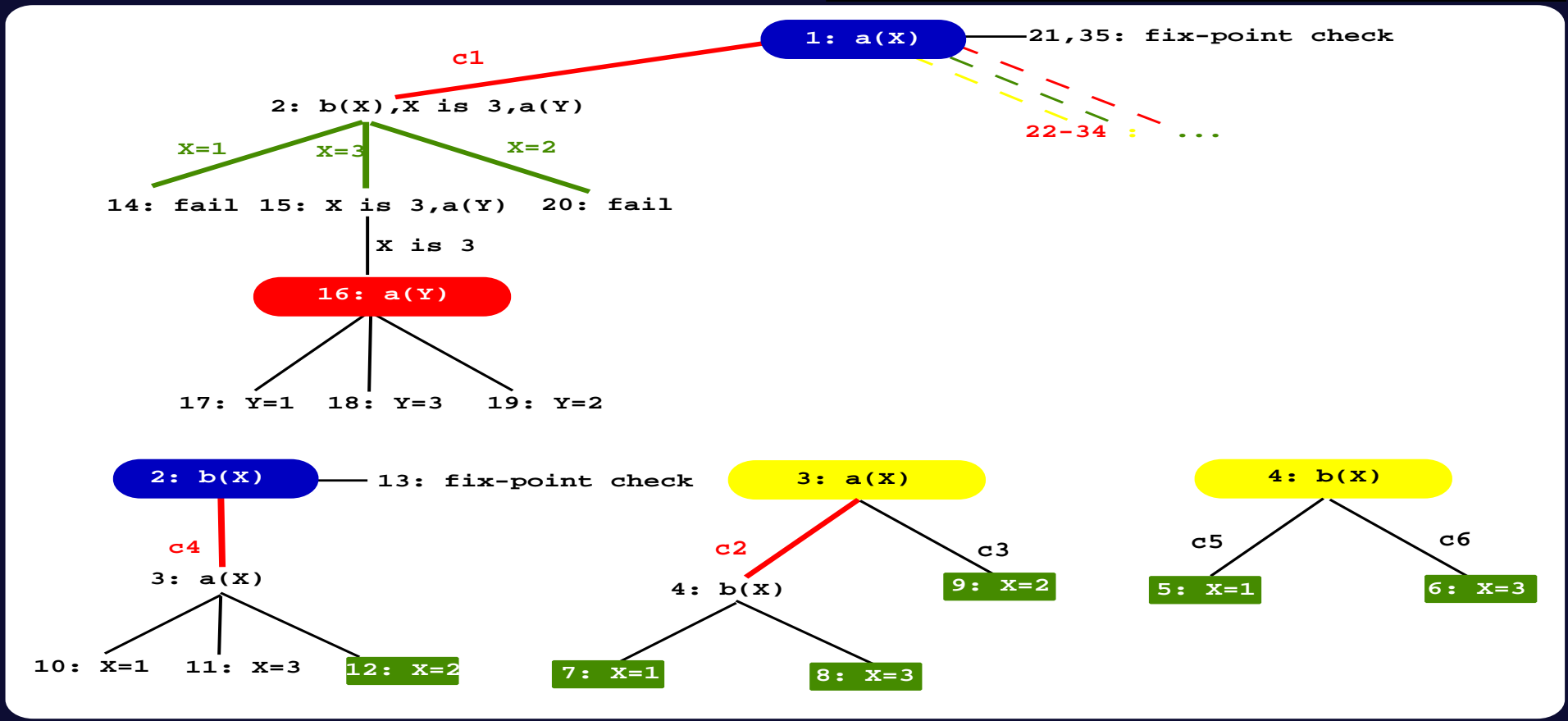


Evaluation Example II - DRA + DRS + DRE

```
:-table a/1,b/1.
a(X):-b(X),X is 3,a(Y).
a(X):-b(X).
a(2).
b(X):-a(X).
b(1).
b(3).
```

- (c1)
- (c2)
- (c3)
- (c4)
- (c5)
- (c6)

Call	Solutions	Loop Alt	Loop Sol
1: a(X)	7: X=1 8: X=3 9: X=2	3: c1 4: c2	
2: b(X)	5: X=1 6: X=3 12: X=2	3: c4	16: X=3

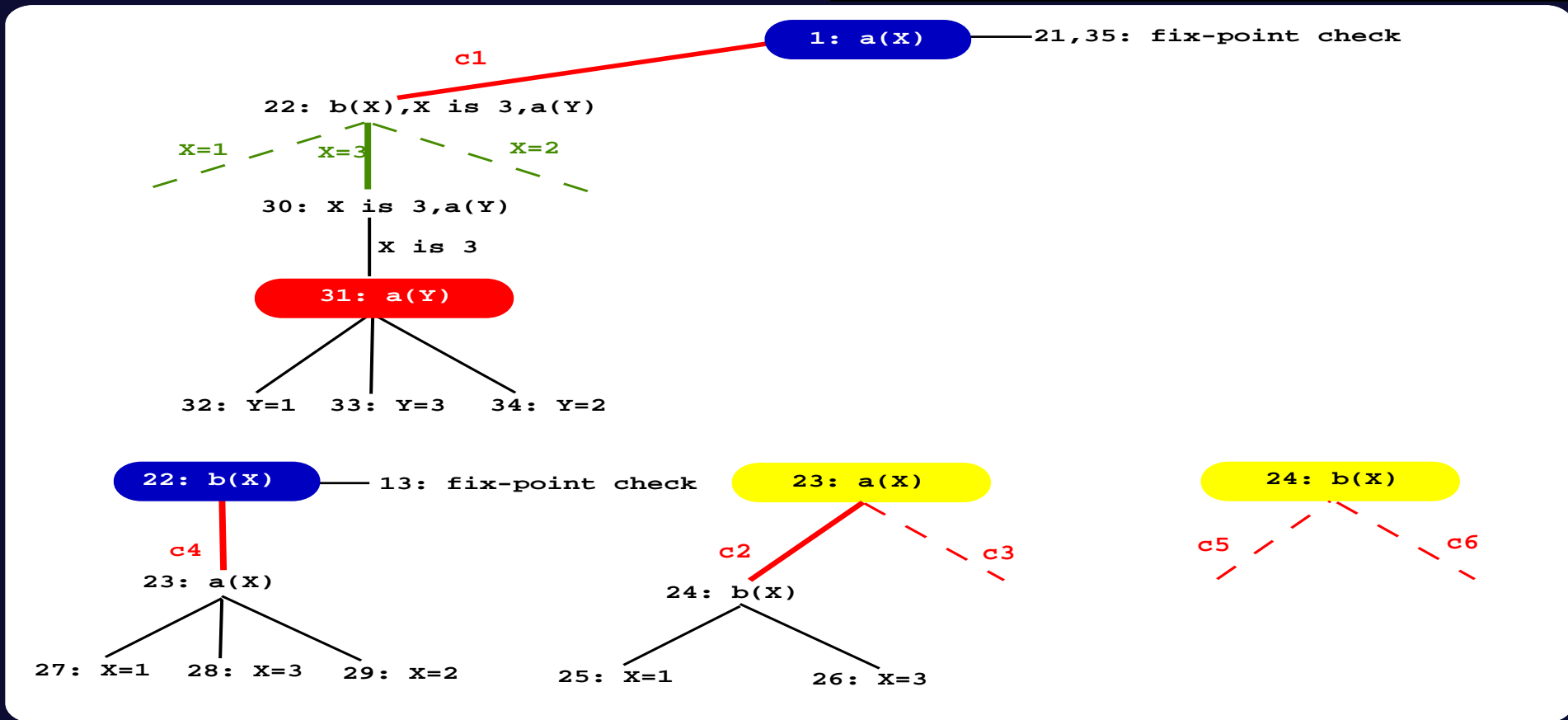


Evaluation Example II - DRA + DRS + DRE

```
:-table a/1,b/1.
a(X):-b(X),X is 3,a(Y).
a(X):-b(X).
a(2).
b(X):-a(X).
b(1).
b(3).
```

- (c1)
- (c2)
- (c3)
- (c4)
- (c5)
- (c6)

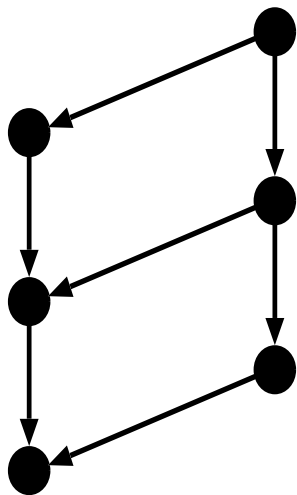
Call	Solutions	Loop Alt	Loop Sol
1: a(X)	7: X=1 8: X=3 9: X=2	3: c1 4: c2	
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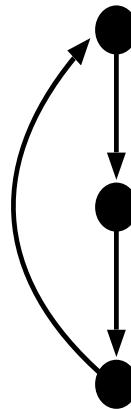
Path Problem - Configuration

```
path_first(X,Z) :- edge(X,Y) , path_first(Y,Z).
path_first(X,Z) :- edge(X,Z).
```

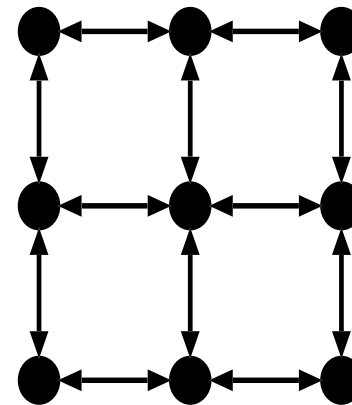
```
path_last(X,Z) :- edge(X,Z).
path_last(X,Z) :- edge(X,Y) , path_last(Y,Z).
```



Pyramid
(depth 3)



Cycle
(depth 3)



Grid
(depth 3)

Experimental Results

Strategy	Pyramid			Cycle			Grid		
	1000	2000	3000	1000	2000	3000	20	30	40
Recursive Clause First									
Standard	664	2,669	6,040	377	1,522	3,400	386	2,714	10,689
DRE	1.02	1.01	1.02	1.00	1.01	1.01	1.02	1.00	1.00
DRA	1.55	1.51	1.51	1.22	1.23	1.21	1.14	1.09	1.10
DRS	1.01	1.00	1.01	1.21	1.23	1.22	1.23	1.27	1.31
DRE+DRA	1.52	1.51	1.50	1.24	1.23	1.20	1.15	1.10	1.06
DRE+DRS	1.01	1.01	1.00	1.22	1.23	1.22	1.22	1.23	1.23
DRA+DRS	1.54	1.52	1.51	1.56	1.57	1.52	1.42	1.42	1.43
All	1.56	1.53	1.50	1.55	1.57	1.52	1.38	1.39	1.37
Recursive Clause Last									
Standard	673	2,775	6,216	382	1,542	3,487	365	2,602	10,403
DRE	0.99	1.01	1.01	1.01	1.01	1.01	1.02	1.03	1.03
DRA	1.47	1.49	1.47	1.24	1.22	1.22	1.15	1.13	1.11
DRS	0.99	0.99	1.01	1.20	1.21	1.23	1.21	1.27	1.30
DRE+DRA	1.49	1.34	1.43	1.24	1.22	1.22	1.14	1.12	1.10
DRE+DRS	1.00	0.99	1.01	1.23	1.22	1.23	1.22	1.27	1.30
DRA+DRS	1.47	1.47	1.46	1.55	1.54	1.53	1.42	1.43	1.43
All	1.49	1.48	1.09	1.48	1.56	1.55	1.42	1.44	1.45

Statistics For The Edge Grid 40

```
path_first(X,Z) :- sld1 , edge(X,Y) , path_first(Y,Z) , sld2.
path_first(X,Z) :- sld3 , edge(X,Z) , sld4.
```

```
path_last(X,Z) :- ...
path_last(X,Z) :- ...
```

Strategy	#SLD Computations			
	sld1/0	sld2/0	sld3/0	sld4/0
Recursive Clause First				
Standard	35,202	200,974,309	35,201	149,757
DRE	1.05	1.04	1.05	1.04
DRA	1.00	1.05	21.99	12.00
DRS	1.00	1.29	1.00	1.00
DRE+DRA	1.05	1.10	1.07	1.11
DRE+DRS	1.05	1.33	1.05	1.04
DRA+DRS	1.00	1.38	21.99	12.00
All	1.05	1.43	1.07	1.11

Statistics For The Edge Grid 40

```

path_first(X,Z) :- ...
path_first(X,Z) :- ...

path_last(X,Z) :- sld3 , edge(X,Z) , sld4.
path_last(X,Z) :- sld1 , edge(X,Y) , path_last(Y,Z) , sld2.

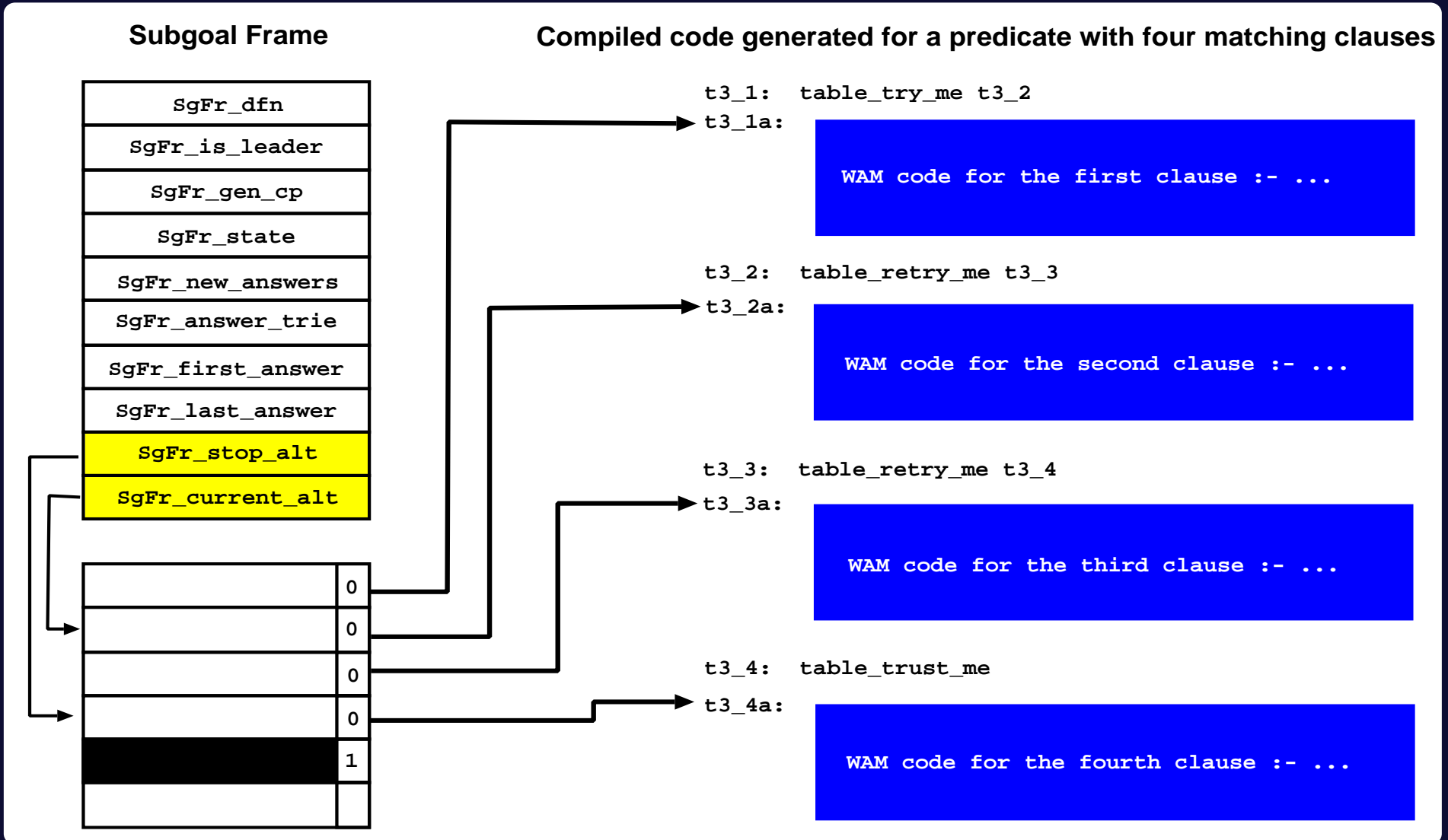
```

Strategy	#SLD Computations			
	sld1/0	sld2/0	sld3/0	sld4/0
Recursive Clause Last				
Standard	48,602	352,277,129	48,602	205,920
DRE	1.00	1.00	1.00	1.00
DRA	1.00	1.05	20.99	11.50
DRS	1.00	1.29	1.00	1.00
DRE+DRA	1.00	1.05	20.99	11.50
DRE+DRS	1.00	1.29	1.00	1.00
DRA+DRS	1.00	1.38	20.99	11.50
All	1.00	1.38	20.99	11.50

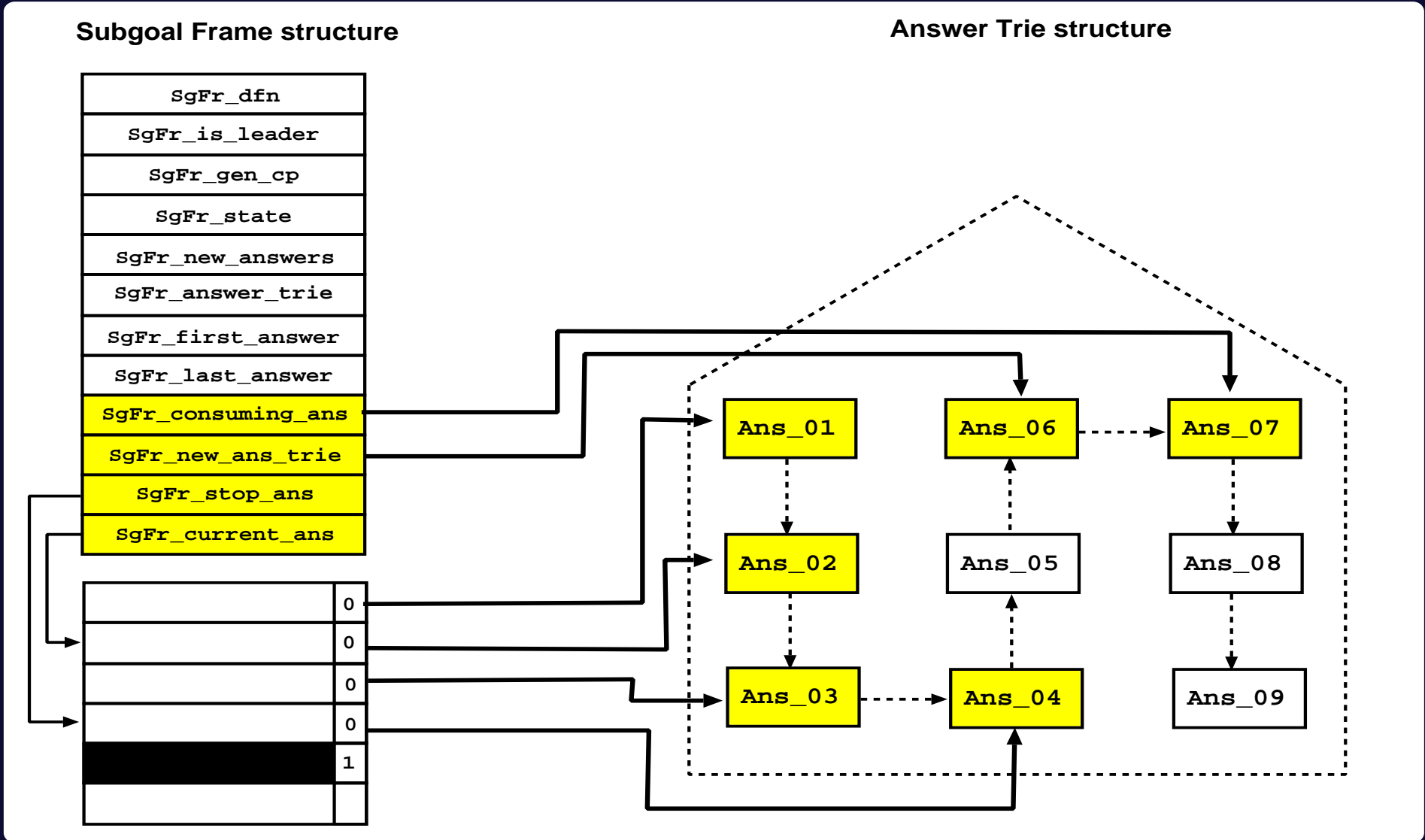
Conclusions and Further Work

- We have presented a new framework that integrates all possible combinations of the already existent linear tabling strategies **DRA** and **DRE** and the new strategy **DRS**.
- Our experiments for **DRS** strategy showed that the strategy of avoiding the consumption of non-looping solutions in re-evaluation rounds can be quite effective for programs that can benefit from it, with insignificant costs for the other programs.
- Further work will include study a possible source-code analysis tool that would determine which linear tabling strategy should be used for a particular program before it's evaluation.

Implementation Details - DRA



Implementation Details - DRS



Implementation Details - DRE

