

Concurrent Programming - Exercises 5

Weak bisimilarity and observable congruence

1. Let

$$\begin{aligned} Buffer &:= put?.get?.Buffer \\ BufferL &:= put?.pass!.BufferL \\ BufferR &:= pass?.get?.BufferR \end{aligned}$$

Show $(BufferL|BufferR)\setminus\{pass!,pass?\} \approx (Buffer|Buffer)$.

2. Given the weak bisimilarity \approx

$$\approx = \bigcup_{R \text{ weak bisimulation}} R$$

Show that

- (a) \approx is an equivalence.
- (b) \approx is the largest weak bisimulation.
- (c) The weak bisimilarity is coarsest than the strong bisimilarity, i.e., $\sim \subseteq \approx$.

3. Let

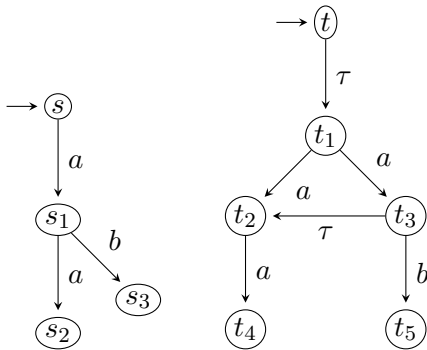
$$\begin{aligned} CMB &:= coin?.coffee!.CMB + coin?.CMB \\ CS &:= pub!.coin!.coffee?.CS \\ UniBad &:= (CMB|CS)\setminus\{coin,coffee\} \end{aligned}$$

Is true that $Spec \approx Unibad$ where $Spec := pub!.Spec$?

4. Show that for any $P, Q \in CCS$ and $\alpha \in Act$ the following equivalences hold:

$$\begin{aligned} \alpha.\tau.P &\approx \alpha.P \\ P + \tau.P &\approx \tau.P \\ \alpha.(P + \tau.Q) &\approx \alpha.(P + \tau.Q) + \alpha.Q \end{aligned}$$

5. Consider the following LTS and show that $s \not\approx t$ using a weak bisimulation game.



6. Consider the following protocol $Protocol := acc?.del!.Protocol$ that corresponds to a communication channel . Given the implementation

$$\begin{aligned}
 Send &:= acc?.Sending \\
 Sending &:= send!.Wait \\
 Wait &:= ack?.Send + error?.Sending \\
 Rec &:= trans?.Del \\
 Del &:= del!.Ack \\
 Ack &:= ack!.Rec \\
 Med &:= send?.Med1 \\
 Med1 &:= \tau.Err + trans!.Med \\
 Err &:= error!.Med
 \end{aligned}$$

show that $(Send|Med|Rec) \setminus \{send, error, trans, ack\} \approx Protocol$. Check with Pseuco.Com.

7. Show that $a.0 + 0 \not\approx a.0 + \tau.0$ and conclude that \approx is not a congruence in CCS .
8. Let \simeq be the observable congruence
- $\tau.a \not\approx a$
 - $P|\tau.Q \not\approx \tau.(P|Q)$

9. Consider the following algorithms $MUTEX$ for mutual exclusivity. For each one:
- (a) Write it in CCS . Use $enter_i$ and $exit_i$ for $i = 1, 2$ to indicate the critical region.
 - (b) Text with pseuco.com using random traces
 - (c) Implement also in CAAL.
 - (d) Consider also

$$MutexSpec := enter1.exit1.MutexSpec + enter2.exit2.MutexSpec$$

Is true that $MUTEX \approx MutexSpec$?

- i) Peterson algorithm.

For process $P_i, j, i = 1, 2$ and $i \neq j$.

```

while true do
  noncritical actions
   $b_i \leftarrow \text{true};$ 
   $k \leftarrow j;$ 
  while  $b_j \wedge k = j$  do
    skip;
  critical actions
   $b_i \leftarrow \text{false}$ 

```

- ii) Hyman algorithm. Variables b_i are Boolean and k is an integer. For processes $P_i, j, i = 1, 2$ and $i \neq j$.

```

while true do

```

noncritical actions

```
bi ← true;  
while k ≠ i do  
  while bj do  
    skip;  
  k ← i;  
critical actions;  
bi ← false;
```

iii) Pnueli algorithm.

Variables y_i are Boolean and start in *false* being local. The variable s is shared and has value 0 or 1 starting in 1. For process P_i and $i = 0, 1$:

```
while true do  
  noncritical actions  
  yi ← true;  
  s ← i;  
  while ¬(y1-i = 0 ∨ (s ≠ i)) do  
    skip;  
critical actions;  
  yi ← false;
```