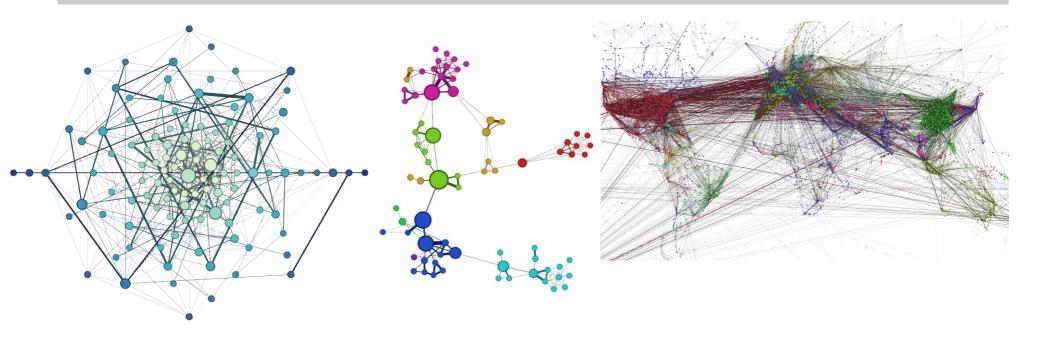
An Introduction To Network Science





Motivation and the "small world" phenomenon

Planet Earth

7,6 Billion Humans

+114

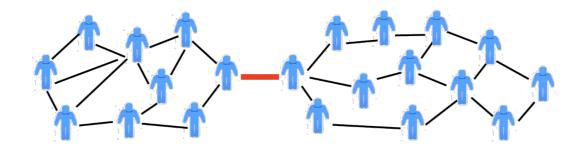
How many "degrees" of separation?

......



1929 Frigyes Karinthy

"If you choose a person out of the 1.5 billions of our planet, I bet that using no more than *five* individuals, one of them my acquaintance, I could contact the person you chose, using only the list of acquaintances of each one"





1969 Stanley Milgram

- People chosen at random on a US State
- Request to send a letter to a given final person in another state :
 - If you know the final person, send directly to him
 - If not, send to someone you think it is more likely to know him

An Experimental Study of the Small World Problem*

JEFFREY TRAVERS

Harvard University

AND

STANLEY MILGRAM

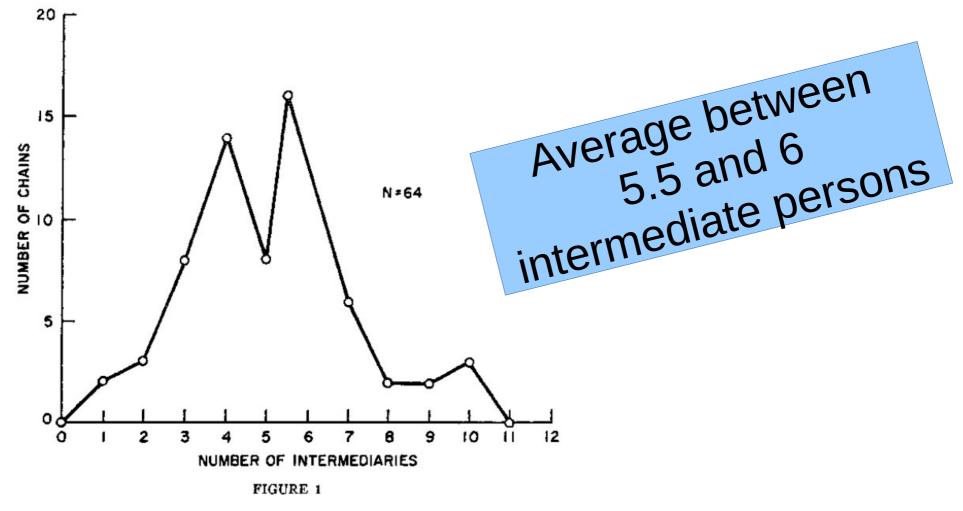
The City University of New York

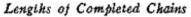
Arbitrarily selected individuals (N=296) in Nebraska and Boston are asked to generate acquaintance chains to a target person in Massachusetts, employing "the small world method" (Milgram, 1967). Sixty-four chains reach the target person. Within this group the mean number of intermediaries between starters and targets is 5.2. Boston starting chains reach the target person with fewer intermediaries than those starting in Nebraska; subpopulations in the Nebraska group do not differ among themselves. The funneling of chains through sociometric "stars" is noted, with 48 per cent of the chains passing through three persons before reaching the target. Applications of the method to studies of large scale social structure are discussed.





1969 Stanley Milgram







"Small World" Project

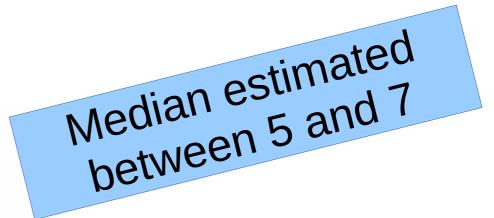
More than 20.000 chains of emails to 18 persons of 13 countries

An Experimental Study of Search in Global Social Networks

2003

Peter Sheridan Dodds,¹ Roby Muhamad,² Duncan J. Watts^{1,2*}

We report on a global social-search experiment in which more than 60,000 e-mail users attempted to reach one of 18 target persons in 13 countries by forwarding messages to acquaintances. We find that successful social search is conducted primarily through intermediate to weak strength ties, does not require highly connected "hubs" to succeed, and, in contrast to unsuccessful social search, disproportionately relies on professional relationships. By accounting for the attrition of message chains, we estimate that social searches can reach their targets in a median of five to seven steps, depending on the separation of source and target, although small variations in chain lengths and participation rates generate large differences in target reachability. We conclude that although global social networks are, in principle, searchable, actual success depends sensitively on individual incentives.



B 150

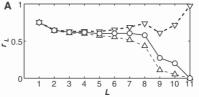
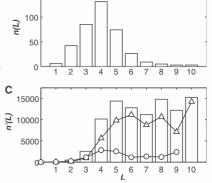


Fig. 1. Distributions of message chain lengths. (A) Average per-step attrition rates (circles) and 95% confidence interval (triangles). (B) Histogram representing the number of chains that are completed in *L* steps (<L> = 4.01). (C) "Ideal" histogram of chain lengths recovered from (B) by accounting for message attrition (A). Bars represent the ideal histogram recovered with average values of *r* [circles in

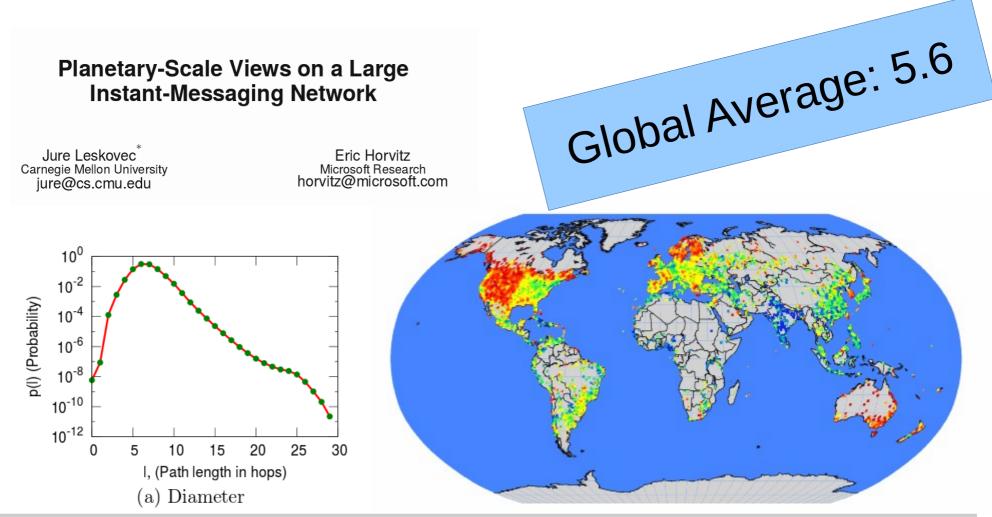


(A)] for the histogram in (B); lines represent a decomposition of the complete data into chains that start in the same country as the target (circles) and those that start in a different country (triangles).



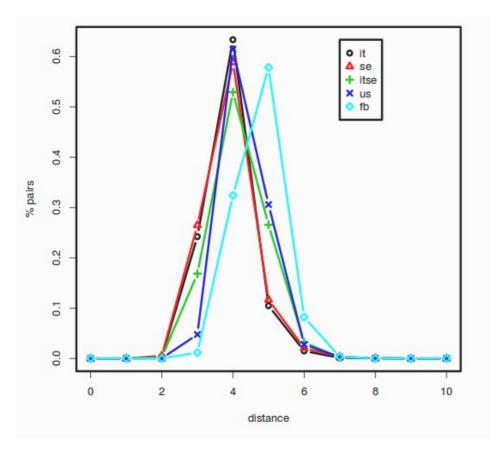
2008 Microsoft Messenger

30 billion conversations between 240 million persons





• 69 billions of friendships between 721 millions of persons





Computer Science > Social and Information Networks

Four Degrees of Separation

Lars Backstrom, Paolo Boldi, Marco Rosa, Johan Ugander, Sebastiano Vigna

(Submitted on 19 Nov 2011 (v1), last revised 5 Jan 2012 (this version, v3))

Frigyes Karinthy, in his 1929 short story "L\'aancszemek" ("Chains") suggested that any two persons are distanc individuals, one of whom is a personal acquaintance, he could contact the selected individual [...]". It is not comp graph theory, but the "six degrees of separation" phrase stuck after John Guare's 1990 eponymous play. Followi one", where "distance" is the usual path length-the number of arcs in the path.) Stanley Milgram in his famous e average number of intermediaries on the path of the postcards lay between 4.4 and 5.7, depending on the sam; We report the results of the first world-scale social-network graph-distance computations, using the entire Facet corresponding to 3.74 intermediaries or "degrees of separation", showing that the world is even smaller than we interesting geographic subgraphs, looking also at their evolution over time.

The networks we are able to explore are almost two orders of magnitude larger than those analysed in the previvery accurate.



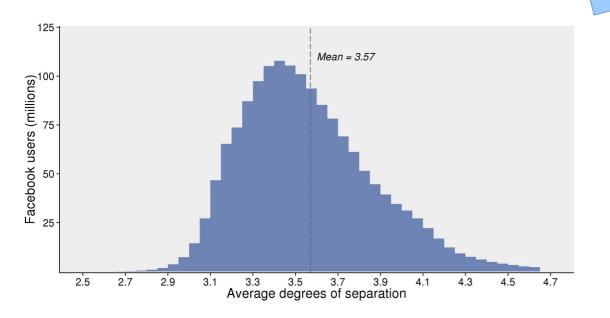
1.59 billions of persons

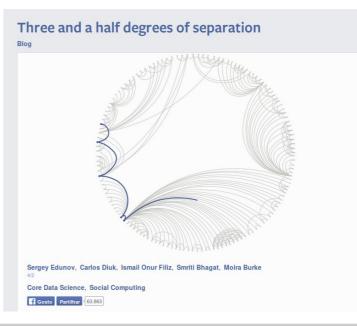
My degrees of separation

Pedro Rib

Pedro Ribeiro's average degrees of separation from everyone is 3.43.



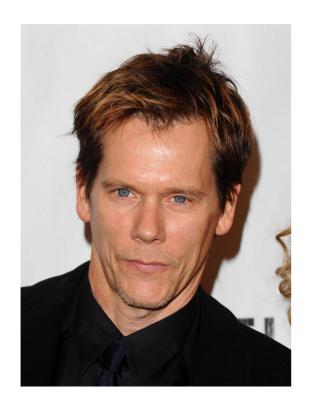


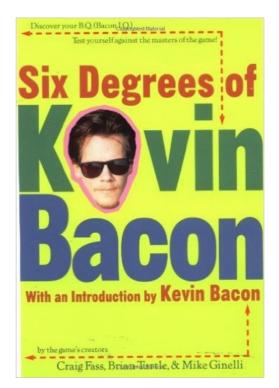


How to explain this?

- Imagine that a person has, on average, 100 friends The power of exponentiation
 - 0 intermediates: 100
 - 1 intermediate: $100^2 = 10.000$
 - -2 intermediates: $100^3 = 1.000.000$
 - -3 intermediates: $100^4 = 100.000.000$
 - -4 intermediates: $100^{5} = 10.000.000.000$
 - -5 intermediates: $100^{6} = 1.000.000.000.000$
- In practice, not all friends are new, but still there is a very fast growth

- The six degrees of Kevin Bacon
 - How many connections to link Kevin Bacon to any other actor, director, producer...
 - "Game" initiated in 1994







Joaquim de Almeida



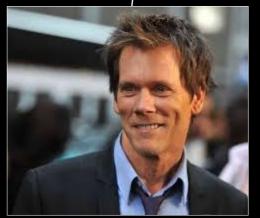


Bret Cullen



Joaquim de Almeida (Bacon Number: 2)





Kevin Bacon



Joaquim de Almeida (Bacon Number: 2)







Nicolau Breyner



Nicolau Breyner (Bacon Number: 3)





Marilyn Monroe



Charlie Chaplin



Marilyn Monroe (Bacon Number: 2)





Charlie Chaplin (Bacon Number: 2)



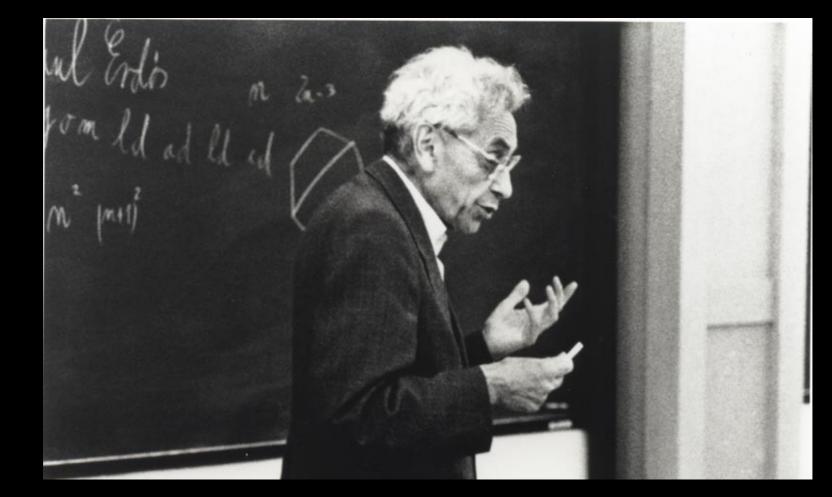
More examples of "Small World" The six degrees of Kevin Bacon https://oracleofbacon.org/ (average number: 3.009) **Kevin Bacon Number** # of persons



"People would start to come up to me in the subway and literally go..."



"Zero! Zero! Zero! Zero!"

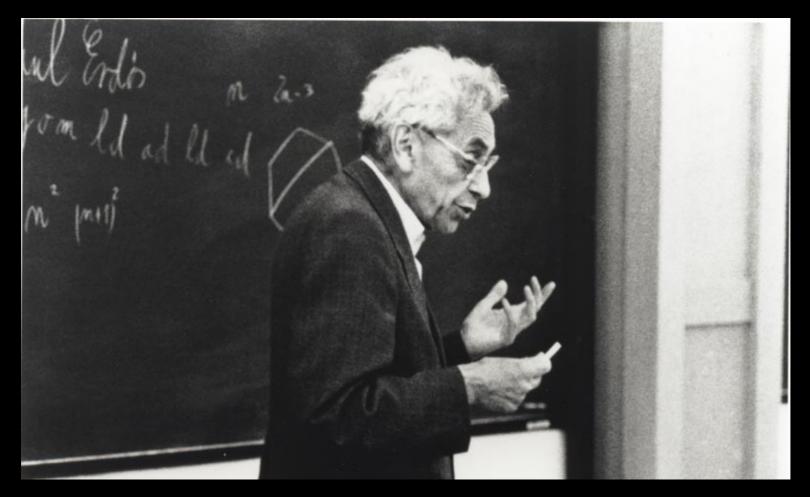


Paul Erdös

Erdös Number

- Erdös number:
 - Scientific articles and very prolific
 mathematician
 http://wwwp.oakland.edu/enp/

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ATHEMATICA	LINEI ALREVIEWS			
Search MSC	Collaboration Dista	Current Jou	rnals Current Publications	
	Number = 4			
Pedro R	libeiro	coauthored with	Srinivasan Parthasarathy ¹	MR3385657
	an Parthasarathy ¹	coauthored with	Yusu Wang	MR3685725
	·	coauthored with coauthored with	Yusu Wang Boris Aronov	MR3685725 MR2347131



Paul Erdös



Emergence of Network Science

Complexity

"I think the next century will be the century of complexity"

Stephen Hawking (Jan, 2000)

The Real World is Complex

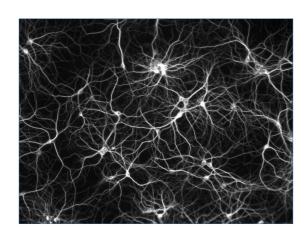
World Population: 7.6 billions



The Real World is Complex

World Population: 7.6 billions



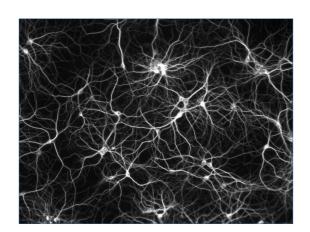


Human Brain Neurons: 100 billions

The Real World is Complex

World Population: 7.6 billions





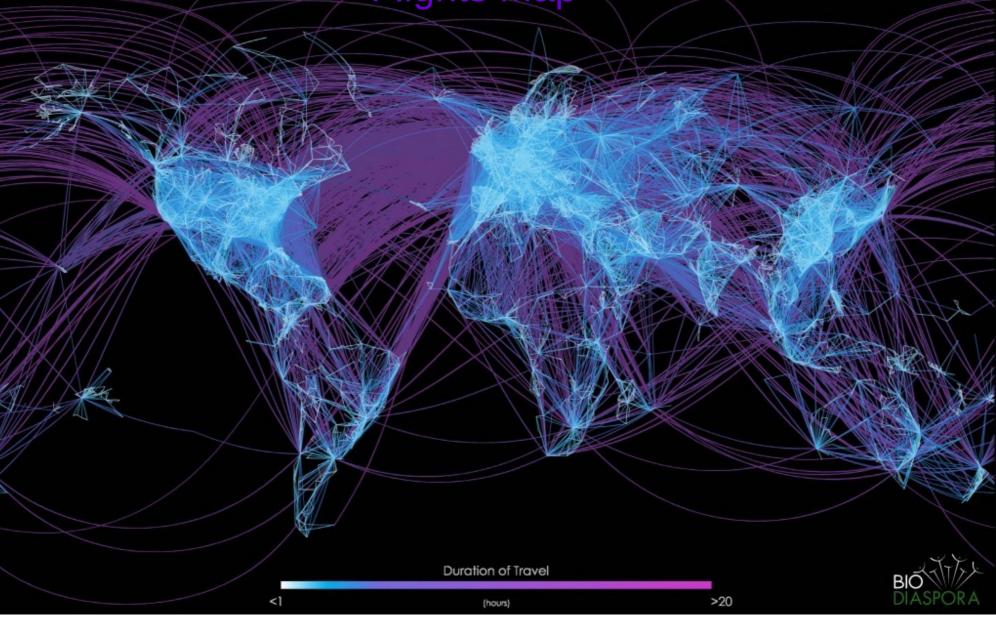
Human Brain Neurons: 100 billions

Internet Devices: 8 billions



Complex Systems → Complex Networks





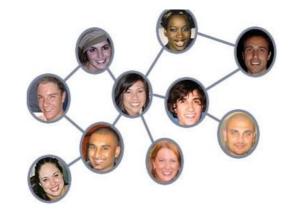
Pedro Ribeiro - An Introduction to Network Science

Complex Networks are Ubiquitous

Social

Complex Networks are Ubiquitous

Social



Facebook

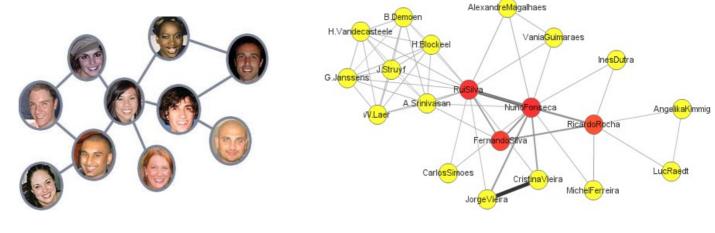
Complex Networks are Ubiquitous

AlexandreMagalhaes Vuluer Rusilva Ru

Facebook

Social

Co-authorship

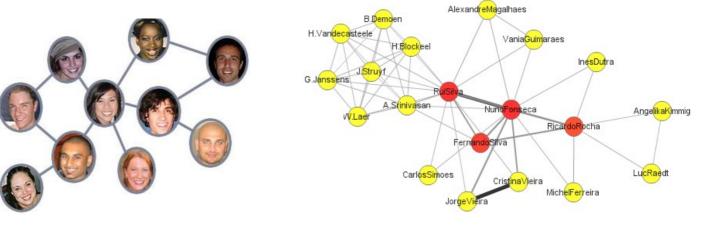


Facebook

Co-authorship

Biological

Social



Facebook

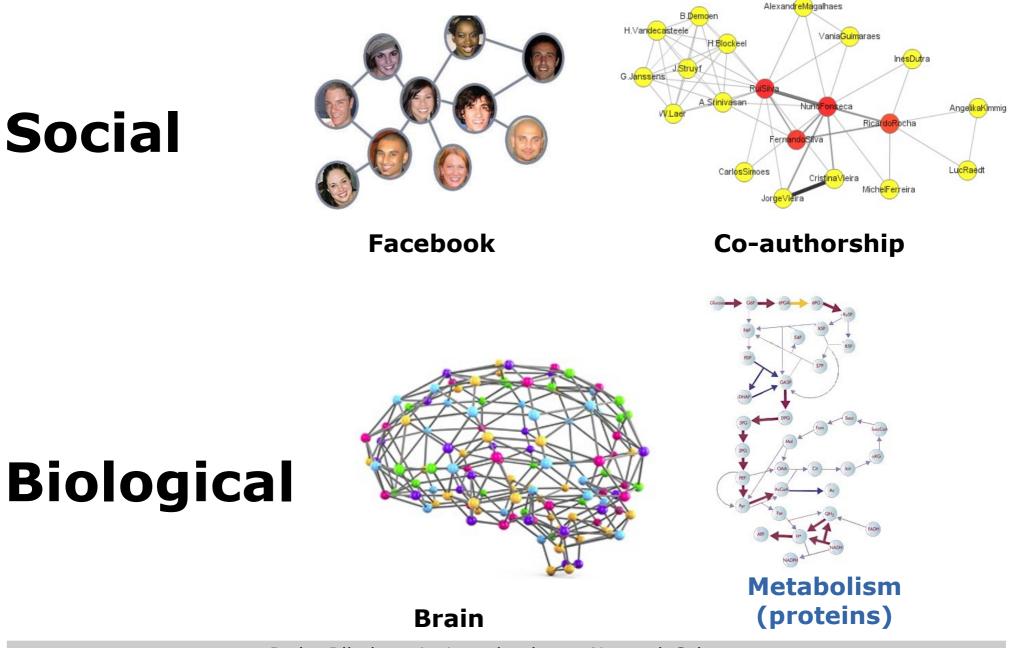
Co-authorship

Biological

Social

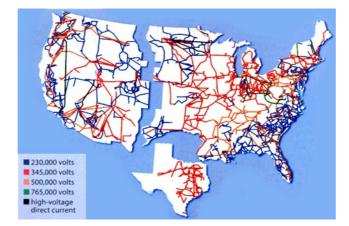


Brain



Spatial

Spatial



Power

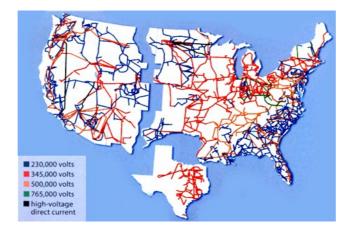
Spatial



Power



Spatial

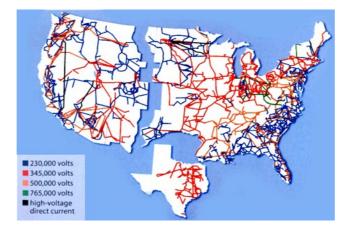


Power



Software

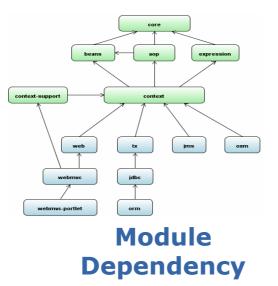
Spatial



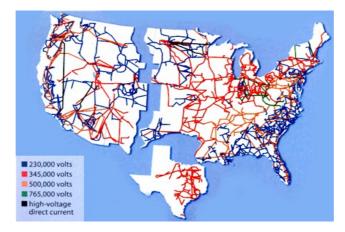






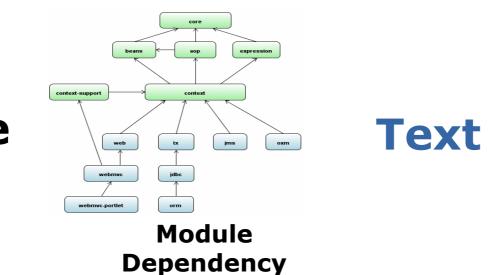


Spatial



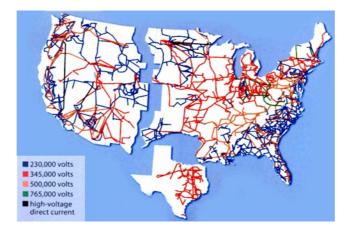






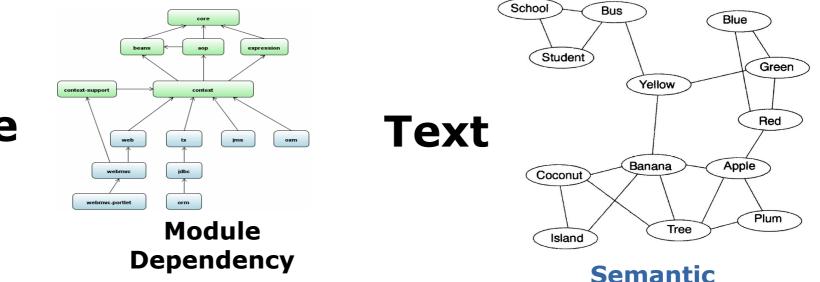


Spatial

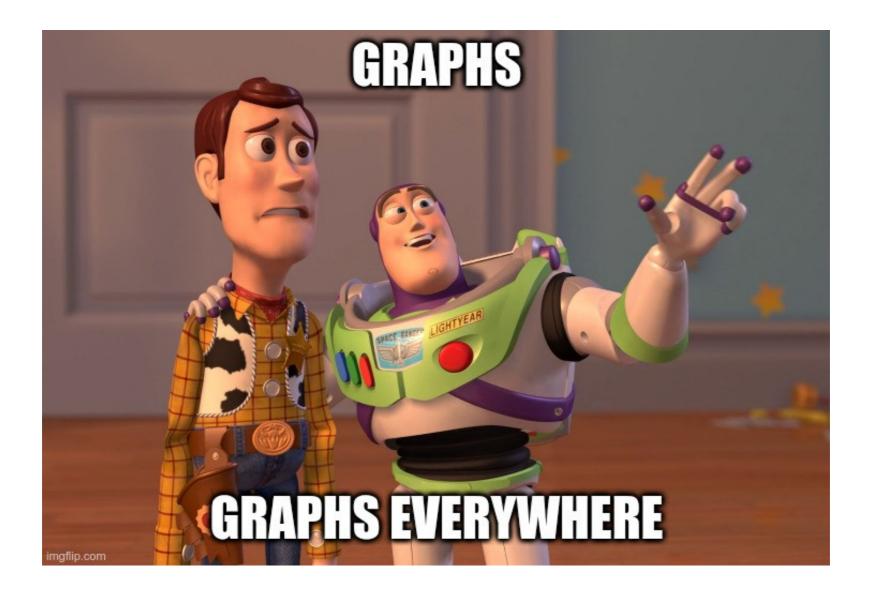


Power





Software



Network Science

Behind many complex systems there is a **network** that defines the **interactions** between the components

In order to understand the systems... we need to understand the **networks**!

Network Science

- Network Science has been emerging on this century as a new discipline:
 - Origins on graph theory and social network research

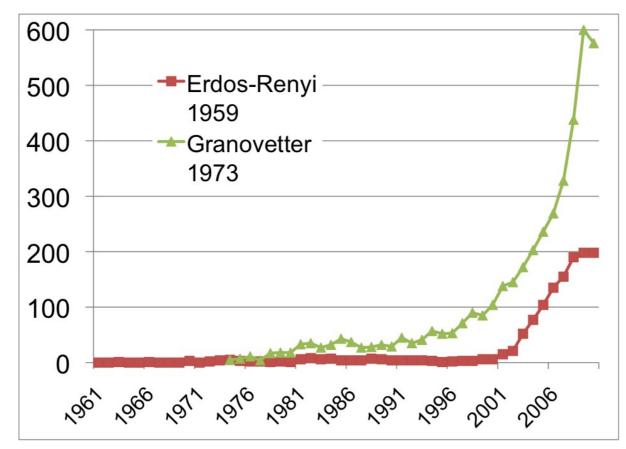


Image: Adapted from (Barabasi, 2015)

• Two main contributing factors:

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1) The emergence of **network maps**

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- Movie actor network: 1998
- World Wide Web: 1999
- Citation Network: 1998
- Metabolic Network: 2000
- PPI Network: 2001

• Two main contributing factors:

1) The emergence of network maps

- Movie actor network: 1998
- World Wide Web: 1999
- Citation Network: 1998
- Metabolic Network: 2000
- PPI Network: 2001

• **436 nodes** – 2003 (email exchange, Adamic-Adar, SocNets)

- **43,553 nodes –** 2006 (email exchange, Kossinets-Watts, Science)
- **4.4 million nodes** 2005 (friendships, Liben-Nowell, PNAS)
- 800 million nodes 2011 (Facebook, Backstrom et al.)

Size matters!

• Two main contributing factors:

2) Universality of network characteristics

Image: Adapted from (Newman, 2005)

• Two main contributing factors:

2) Universality of network characteristics

 The architecture and topology of networks from different domains exhibit more similarities that what one would expect

• Two main contributing factors:

2) Universality of network characteristics

• The architecture and topology of networks from different domains exhibit more similarities that what one would

10^4 (a)	10 ⁶ (b)	10 ⁴ (c)	Many real world networks are power law	
102				exponent α (in/out degree)
10 ⁰ + · · · · · · · · · · · · · · · · · ·		10 ⁰ +	film actors	2.3
10^0 10^2 10^4	10^0 10^2 10^4	10^0 10^2 10^4	ר telephone call graph	2.1
word frequency	citations	web hits	email networks	1.5/2.0
(d)	(e)	10 ⁴ -E.g. power laws	sexual contacts	3.2
100-	10 ⁶	1.3	WWW	2.3/2.7
		103-	internet	2.5
$10 - \frac{1}{10^6}$	10^{0} 10^{0} 10^{2} 10^{4} 10^{6} telephone calls received	10^2 2 3 4 5 6 $7earthquake magnitude$	peer-to-peer	2.1
			metabolic network	2.2
			protein interactions	2.4

Image: Adapted from (Newman, 2005)

Image: Adapted from Leskovec, 2015

Impact of Network Science: Economic



Google

facebook.

Impact of Network Science: Scientific





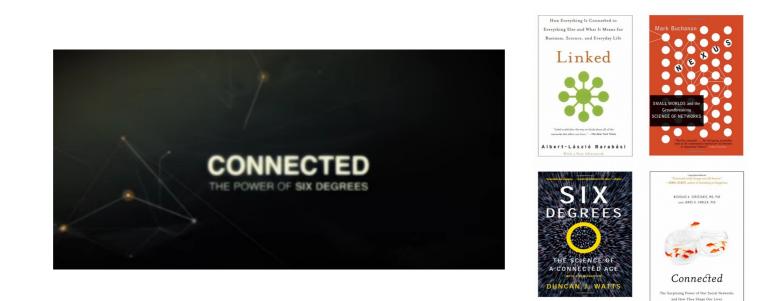
Impact of Network Science: Societal



PREMIER REFERENCE SOURCE

Network Science for Military Coalition Operations Information Exchange and Interaction





Reasoning about Networks

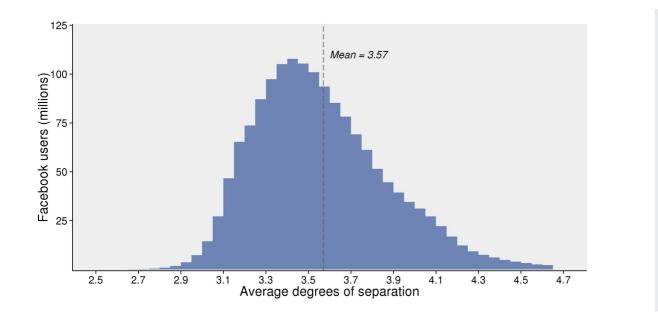
- What do we hope to achieve from studying networks?
 - Patterns and statistical properties of network data
 - Design principles and models
 - Algorithms and predictive models to answer questions and make predictions

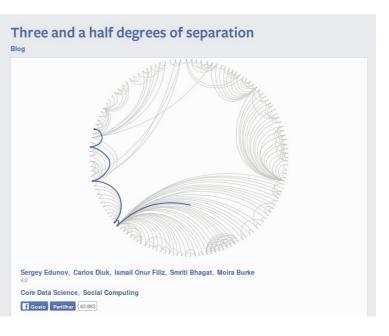
Mining and Learning with Graphs

- How do we mine networks?
 - Empirically: Study network data to find organizational principles
 - How do we measure and quantify networks?
 - Mathematical models: Graph theory and statistical models
 - Models allow us to understand behaviors and distinguish surprising from expected phenomena
 - Algorithms for analyzing graphs
 - Hard computational challenges

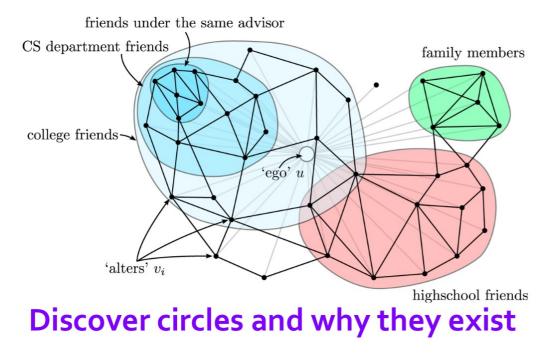
• Some possible tasks:

- Some possible tasks:
 - General Patterns
 - Ex: "scale-free", "small-world"

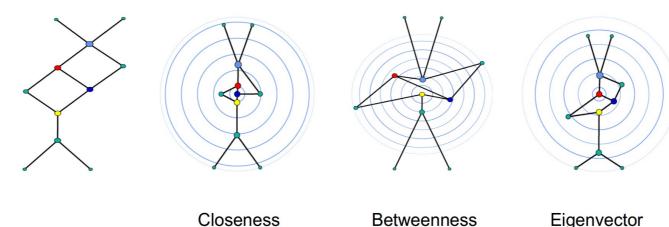




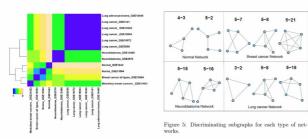
- Some possible tasks:
 - General Patterns
 - Ex: "scale-free", "small-world"
 - Community Detection
 - What groups of nodes are "related"?



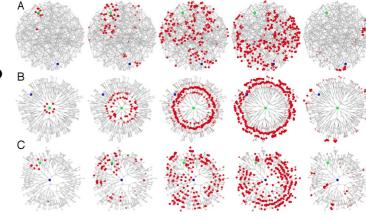
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 - Information Propagation
 - Epidemics? Robustness?

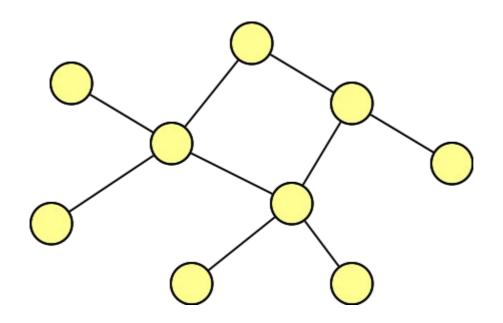


- Some possible tasks:
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 - Ex: "scale-free", "small-world"
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 - What groups of nodes are "related"?
 - Node Classification
 - Importance and function of a
 - Network Comparison
 - What is the type of the netwo
 - Information Propagation
 - Epidemics? Robustness?
 - Link prediction
 - Future connections? Errors in graph constructions?



Brief Introduction to Graph Theory and Network Vocabulary

Terminology



- **Objects:** nodes, vertices **V**
- Interactions: links, edges E
- System: network, graph G(V,E)

Networks or Graphs?

- Network often refers to real systems
 - Web, Social network, Metabolic network
 - Language: Network, node, link
- Graph is a mathematical representation of a network
 - Web graph, Social graph (a Facebook term)
 - Language: Graph, vertex, edge

We will try to make this distinction whenever it is appropriate, but in most cases we will use the two terms interchangeably

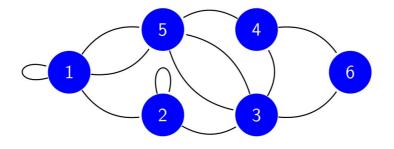
Choosing the Network

- If you connect individuals that work with each other, you will explore a professional network
- If you connect those that are friend, you will be exploring a friendship network
- If you connect scientific papers that cite each other, you will be studying the citation network
- Another example: if you connect all papers with the same word in the title, what will you be exploring?
- There might be several possible representations

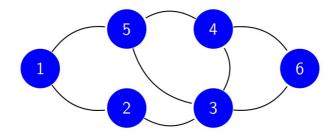
The choice of the network representation of a given fomain determines our ability to use it successfully

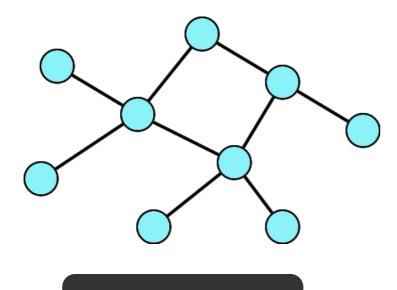
Simple and multi-graphs

- In general, graphs may have self-loops and multi-edges
 - A graph with either is called a **multi-graph**



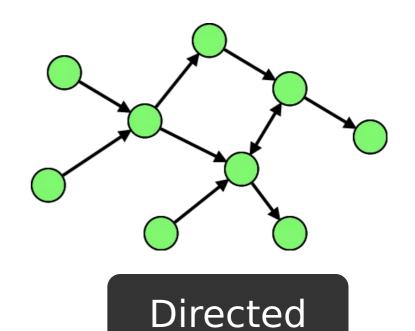
 We will mostly work with simple graphs, with no self-loops or multi-edges







- co-authorship networks
- actor networks
- facebook friendships



- www hyperlinks
- phone calls
- roads network

Edge Attributes

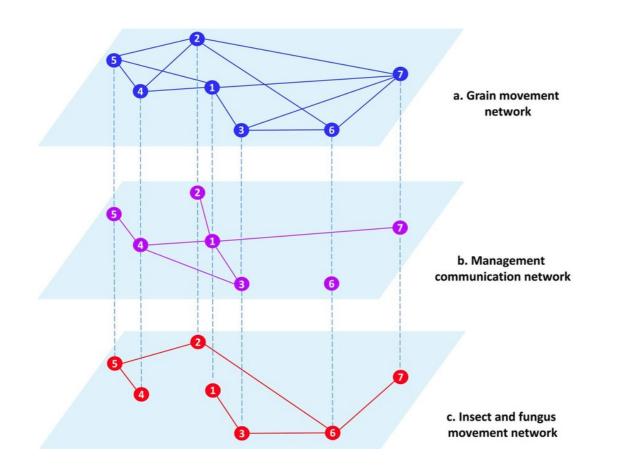
- Examples:
 - Weight (duration call, distance road, ...)
 - Ranking (best friend, second best friend, ...)
 - Type (friend, relative, co-worker, ...)
 [colored edges]
 - We can have a set of **multiple** attributes

Node Attributes

- Examples:
 - **Type** (nationality, sex, age, ...) [colored nodes]
 - We can have a set of **multiple** attributes

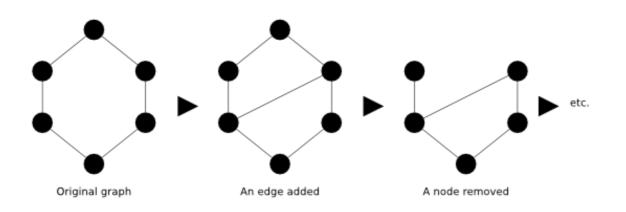
Multiplex Networks

• Different layers (types) of connections



Temporal Networks

Evolution over time

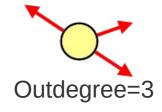


Node Properties

• From immediate connections

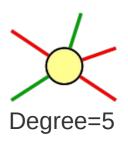
- Outdegree

how many directed edges originate at node





how many directed edges are incident on a node Indegree=2



- **Degree** (in or out)

number of outgoing and incoming edges

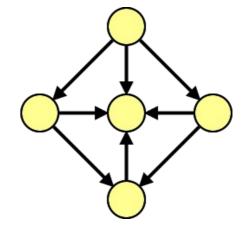
Node Properties

Degree related metrics:

- Degree sequence

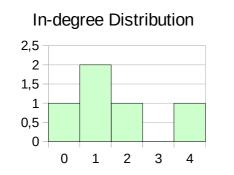
an ordered list of the (in,out) degree of each node

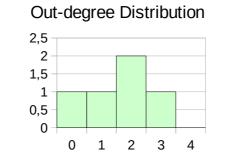
- In-degree sequence: [4, 2, 1, 1, 0]
- Out-degree sequence: [3, 2, 2, 1, 0]
- Degree sequence: [4, 3, 3, 3, 3]



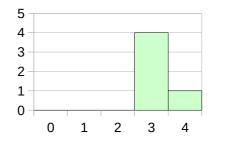
- Degree Distribution

a frequency count of the occurrences of each degree [usually plotted as probability \rightarrow normalization]





Degree Distribution



Sparsity of Networks

Real Networks are usually very Sparse!

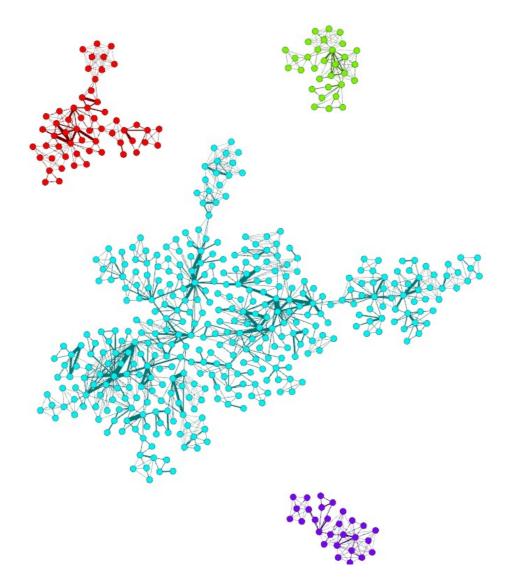
Network	Dir/Undir	Nodes	Edges	Avg. Degree
Internet	Undirected	192,244	609,066	6.33
WWW	Directed	325,729	1,479,134	4.60
Power Grid	Undirected	4,941	6,594	2.67
Mobile Phone Calls	Directed	36,595	91,826	2.51
Email	Directed	57,194	103,731	1.81
Science Collaboration	Undirected	23,133	93,439	8.08
Actor Network	Undirected	702,388	29,397,908	83.71
Citation Network	Directed	449,673	4,689,479	10.43
E. Coli Metabolism	Directed	1,039	5,082	5.58
Protein Interactions	Undirected	2,018	2,930	2.90

 A graph where every pair of nodes is connected is called a complete graph (or a clique)

Table: Adapted from (Barabasi, 2015)

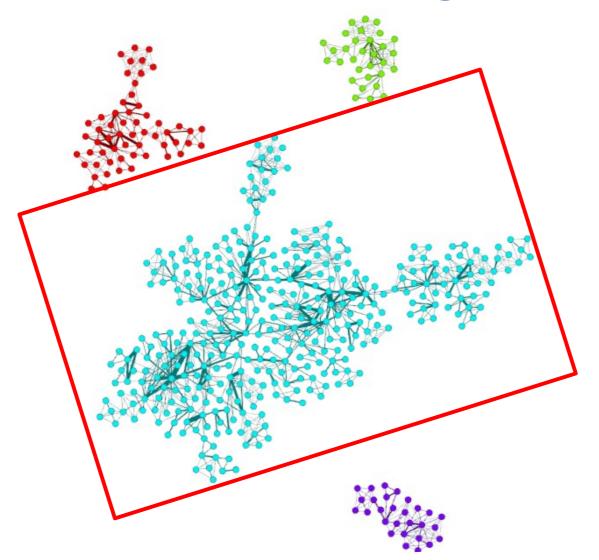
Connectivity

Not everything is connected



Connectivity

 If the largest component has a large fraction of the nodes we call it the giant component



Bipartite

 A bipartite graph is a graph whose nodes can be divided into two disjoint sets U and V such that every edge connects a node in U to one in V.

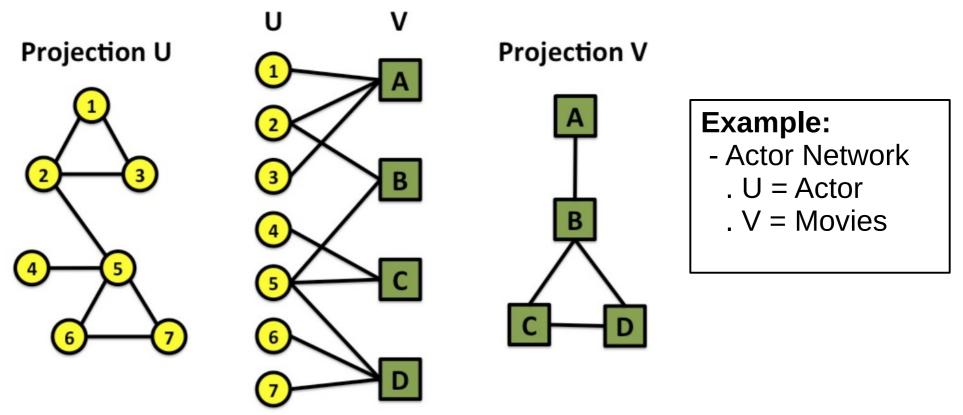
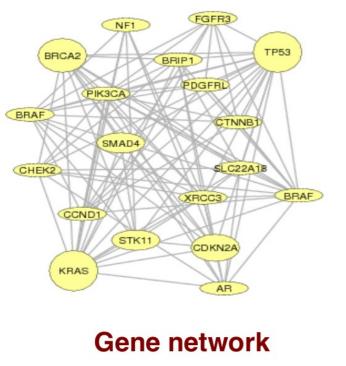
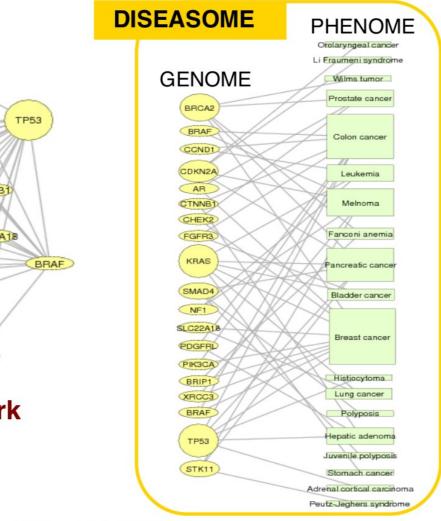
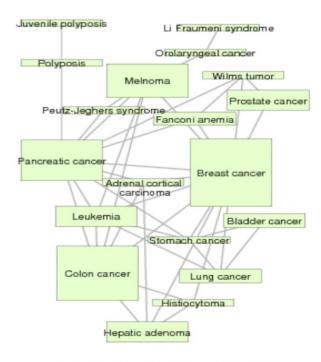


Image: Adapted from Leskovec, 2015

Bipartite Network Projections







Disease network

Goh, Cusick, Valle, Childs, Vidal & Barabási, PNAS (2007)

Bipartite - Human Disease Network

