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# **FAdo Documentation**

***Release 1.3.5.1***

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**Aug 01, 2019**



# CONTENTS

<b>1</b>	<b>What is FAdo?</b>	<b>3</b>
1.1	Regular Languages . . . . .	3
1.2	Finite Languages . . . . .	3
1.3	Transducers . . . . .	4
1.4	Codes . . . . .	4
<b>2</b>	<b>Module: Finite Automata (fa)</b>	<b>5</b>
2.1	Class FA (abstract class for Finite Automata) . . . . .	5
2.2	Class OFA (one-way finite automata class) . . . . .	12
2.3	Class DFA (Deterministic Finite Automata) . . . . .	16
2.4	Class NFA (Nondeterministic Finite Automata) . . . . .	30
2.5	Class NFAr (Nondeterministic Finite Automata w/ reverse transition f.) . . . . .	39
2.6	Class GFA (Generalized Finite Automata) . . . . .	41
2.7	Class SSemiGroup (Syntactic SemiGroup) . . . . .	43
2.8	Class EnumL (Language Enumeration) . . . . .	44
2.9	Functions . . . . .	44
<b>3</b>	<b>Module: Common Definitions (common)</b>	<b>47</b>
3.1	Class Word . . . . .	47
<b>4</b>	<b>Module: FAdo IO Functions (fio)</b>	<b>49</b>
4.1	Functions . . . . .	49
<b>5</b>	<b>Module: Regular Expressions (reex)</b>	<b>51</b>
5.1	Class RegularExpression . . . . .	51
5.2	Class regexp (regular expression) . . . . .	51
5.3	Class specialConstant . . . . .	56
5.4	Class epsilon . . . . .	58
5.5	Class emptyset . . . . .	58
5.6	Class sigmaP . . . . .	59
5.7	Class sigmaS . . . . .	60
5.8	Class connective . . . . .	61
5.9	Class star . . . . .	62
5.10	Class concat . . . . .	64
5.11	Class disj . . . . .	65
5.12	Class power . . . . .	66
5.13	Class option . . . . .	68
5.14	Class conj (intersection) . . . . .	70
5.15	Class shuffle . . . . .	70
5.16	Class atom . . . . .	71

5.17	Class position . . . . .	75
5.18	Class ParseReg . . . . .	76
5.19	Class sconnective (special connective) . . . . .	76
5.20	Class sconcat . . . . .	77
5.21	Class sstar . . . . .	78
5.22	Class sdisj . . . . .	79
5.23	Class sconj . . . . .	80
5.24	Class snot . . . . .	81
5.25	Functions . . . . .	83
<b>6</b>	<b>Module: Transducers (transducers)</b>	<b>85</b>
6.1	Class Transducer . . . . .	85
6.2	Class SFT (Standard Form Transducers) . . . . .	85
6.3	Functions . . . . .	91
<b>7</b>	<b>Module: Finite Languages (f1)</b>	<b>93</b>
7.1	Class FL (Finite Language) . . . . .	93
7.2	Class DFCA (Deterministic Finite Cover Automata) . . . . .	95
7.3	Class AFA (Acyclic Finite Automata) . . . . .	95
7.4	Class ADFA (Acyclic Deterministic Finite Automata) . . . . .	96
7.5	Class ANFA (Acyclic Non-deterministic Finite Automata) . . . . .	99
7.6	Class RndWGen (Random Word Generator) . . . . .	100
7.7	Functions . . . . .	100
<b>8</b>	<b>Module: graphs (graph creation and manipulation)</b>	<b>103</b>
<b>9</b>	<b>Module: Context Free Grammars Manipulation (cfg)</b>	<b>107</b>
9.1	Class CFGGrammar (Context Free Grammar) . . . . .	107
9.2	Class CNF . . . . .	107
9.3	Class cfgGenerator . . . . .	108
9.4	Class reStringRGenerator (Reg Exp Generator) . . . . .	108
9.5	Functions . . . . .	108
<b>10</b>	<b>Module: Random DFA Generator (rndfa)</b>	<b>111</b>
10.1	Class ICDFArgen (Generator container) . . . . .	111
10.2	Class ICDFArnd (Complete IC DFA random generator) . . . . .	111
10.3	Class ICDFArndIncomple (Incomplete IC DFA generator) . . . . .	112
<b>11</b>	<b>Module: Random ADFA Generator (rndadfa)</b>	<b>113</b>
11.1	Class ADFArnd (ADFA random generator) . . . . .	113
<b>12</b>	<b>Module: Combo Operations (comboperations)</b>	<b>117</b>
<b>13</b>	<b>Module: Codes (codes)</b>	<b>121</b>
13.1	Class CodeProperty . . . . .	121
13.2	Class TrajProp . . . . .	121
13.3	Class IPTProp . . . . .	122
13.4	Class IATProp . . . . .	124
13.5	Class PrefixProp . . . . .	124
13.6	Class ErrDetectProp . . . . .	125
13.7	Class ErrCorrectProp . . . . .	125
13.8	Functions . . . . .	126
<b>14</b>	<b>Module: Grail Compatibility (grail)</b>	<b>129</b>
14.1	Class ParserGrail . . . . .	129

14.2	Class Grail . . . . .	129
14.3	Functions . . . . .	130
<b>15</b>	<b>Module: Set Specification Transducers and Automata (sst)</b>	<b>131</b>
15.1	Class PSP . . . . .	131
<b>16</b>	<b>Small Tutorial</b>	<b>133</b>
<b>17</b>	<b>A small tutorial for FAdo</b>	<b>135</b>
<b>18</b>	<b>Indices and tables</b>	<b>141</b>
	<b>Python Module Index</b>	<b>143</b>
	<b>Index</b>	<b>145</b>



## **FAdo: Tools for Language Models Manipulation**

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The support of transducers and all its operations, as well of Set Specifications, is a joint work with *Stavros Konstantinidis* (St. Mary's University, Halifax, NS, Canada) (<http://cs.smu.ca/~stavros/>).

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*Page of the project:* <http://fado.dcc.fc.up.pt>.

*Version:* 1.3.5.1

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## WHAT IS FADO?

The **FAdo** system aims to provide an open source extensible high-performance software library for the symbolic manipulation of automata and other models of computation.

To allow high-level programming with complex data structures, easy prototyping of algorithms, and portability (to use in computer grid systems for example), are its main features. Our main motivation is the theoretical and experimental research, but we have also in mind the construction of a pedagogical tool for teaching automata theory and formal languages.

### 1.1 Regular Languages

It currently includes most standard operations for the manipulation of regular languages. Regular languages can be represented by regular expressions (regexp) or finite automata, among other formalisms. Finite automata may be deterministic (DFA), non-deterministic (NFA) or generalized (GFA). In **FAdo** these representations are implemented as Python classes.

Elementary regular languages operations as union, intersection, concatenation, complementation and reverse are implemented for each class. Also several combined operations are available for specific models.

Several conversions between these representations are implemented:

- NFA -> DFA: subset construction
- NFA -> RE: recursive method
- GFA -> RE: state elimination, with possible choice of state orderings
- RE -> NFA: Thompson method, Glushkov method, follow, Brzozowski, and partial derivatives.
- For DFAs several minimization algorithms are available: Moore, Hopcroft, and some incremental algorithms. Brzozowski minimization is available for NFAs.
- An algorithm for hyper-minimization of DFAs
- Language equivalence of two DFAs can be determined by reducing their correspondent minimal DFA to a canonical form, or by the Hopcroft and Karp algorithm.
- Enumeration of the first words of a language or all words of a given length (Cross Section)
- Some support for the transition semigroups of DFAs

### 1.2 Finite Languages

Special methods for finite languages are available:

- Construction of a ADFA (acyclic finite automata) from a set of words
- Minimization of ADFAs
- Several methods for ADFAs random generation
- Methods for deterministic cover finite automata (DCFA)

## 1.3 Transducers

Several methods for transducers in standard form (SFT) are available:

- Rational operations: union, inverse, reversal, composition, concatenation, star
- Test if a transducer is functional
- Input intersection and Output intersection operations

## 1.4 Codes

A *language property* is a set of languages. Given a property specified by a transducer, several language tests are possible.

- Satisfaction i.e. if a language satisfies the property
- Maximality i.e. the language satisfies the property and is maximal
- Properties implemented by transducers include: input preserving, input altering, trajectories, and fixed properties
- Computation of the edit distance of a regular language, using input altering transducers

## MODULE: FINITE AUTOMATA (FA)

### Finite automata manipulation.

Deterministic and non-deterministic automata manipulation, conversion and evaluation.

### 2.1 Class FA (abstract class for Finite Automata)

```
class fa.FA
    Bases: common.Drawable
    Base class for Finite Automata.

    States
        set of states.
        Type list

    Sigma
        alphabet set.
        Type set

    Initial
        the initial state index.
        Type int

    Final
        set of final states indexes.
        Type set

    delta
        the transition function.
        Type dict
```

---

**Note:** This is just an abstract class. **Not to be used directly!!**

---

**addFinal** (*stateindex*)

A new state is added to the already defined set of final states.

**Parameters** **stateindex** (*int*) – index of the new final state.

**addSigma** (*sym*)

Adds a new symbol to the alphabet.

**Parameters** **sym** (*str*) – symbol to be added

**Raises** `DFAepsilonRedefinition` – if sym is Epsilon

---

**Note:**

- There is no problem with duplicate symbols because Sigma is a Set.
  - No symbol Epsilon can be added.
- 

**addState** (*name=None*)

Adds a new state to an FA. If no name is given a new name is created.

**Parameters** **name** (Object, optional) – Name of the state to be added.

**Returns** Current number of states (the new state index).

**Return type** `int`

**Raises** `DuplicateName` – if a state with that name already exists

**conjunction** (*other*)

A simple literate invocation of `__and__`

**Parameters** **other** (`FA`) – right hand operand.

**Returns** Intersection of self and other.

**Return type** `FA`

New in version 0.9.6.

**countTransitions** ()

Evaluates the size of FA transitionwise

**Returns** the number of transitions

**Return type** `int`

Changed in version 1.0.

**delFinal** (*st*)

Deletes a state from the final states list

**Parameters** **st** (`int`) – state to be marked as not final.

**delFinals** ()

Deletes all the information about final states.

**deleteState** (*sti*)

Remove the given state and the transitions related with that state.

**Parameters** **sti** (`int`) – index of the state to be removed

**Raises** `DFAstateUnknown` – if state index does not exist

**disj** (*other*)

Another simple literate invocation of `__or__`

**Parameters** **other** (`FA`) – the other FA.

**Returns** Union of self and other.

**Return type** `FA`

New in version 0.9.6.

**disjunction** (*other*)

A simple literate invocation of `__or__`

**Parameters** **other** (*FA*) – the other FA

**Returns** Union of self and other.

**Return type** *FA*

**dotDrawState** (*sti, sep='\n', \_strict=False, \_maxLblSz=6*)

Draw a state in dot format

**Parameters**

- **sti** (*int*) – index of the state.
- **sep** (*str*, optional) – separator.
- **\_maxLblSz** (*int*, optional) – max size of labels before getting removed
- **\_strict** (*bool*, optional) – use limitations of label sizes

**Returns** string to be added to the dot file.

**Return type** *str*

**dotDrawTransition** (*st1, sym, st2, sep*)

Draw a transition in dot format

**Parameters**

- **st1** (*str*) – departing state
- **sym** (*str*) – label
- **st2** (*str*) – arriving state
- **sep** (*str*) – separator

**dotFormat** (*size='20, 20', direction='LR', sep='\n', strict=False, maxLblSz=6*)

A dot representation

**Parameters**

- **direction** (*str*) – direction of drawing
- **size** (*str*) – size of image
- **sep** (*str*) – line separator
- **maxLblSz** – max size of labels before getting removed
- **strict** – use limitations of label sizes

**Returns** the dot representation

**Return type** *str*

New in version 0.9.6.

Changed in version 1.2.1.

**eliminateDeadName** ()

Eliminates dead state name (`common.DeadName`) renaming the state

**Attention:** works inplace

New in version 1.2.

**equivalentP** (*other*)

Test equivalence between automata

**Parameters** **other** (*FA*) – the other automata

**Return type** *bool*

New in version 0.9.6.

**evalSymbol** ()

Evaluation of a single symbol

**finalP** (*state*)

Tests if a state is final

**Parameters** **state** (*int*) – state index.

**Returns** is the state final?

**Return type** *bool*

**finalsP** (*states*)

Tests if all the states in a set are final

**Parameters** **states** (*set*) – set of state indexes.

**Returns** are all the states final?

**Return type** *bool*

New in version 1.0.

**hasStateIndexP** (*st*)

Checks if a state index pertains to an FA

**Parameters** **st** (*int*) – index of the state.

**Return type** *bool*

**images** (*sti, c*)

The set of images of a state by a symbol

**Parameters**

- **sti** (*int*) – state
- **c** (*object*) – symbol

**Return type** *iterable*

**indexList** (*lstn*)

Converts a list of stateNames into a set of stateIndexes.

**Parameters** **lstn** (*list*) – list of names

**Returns** the list of state indexes

**Return type** *set*

**Raises** *DFAstateUnknown* – if a state name is unknown

**initialP** (*state*)

Tests if a state is initial

**Parameters** **state** – state index

**Returns** is the state initial?

**Return type** `bool`

**initialSet** ()

The set of initial states

**Returns** set of States.

**Return type** `set`

**inputs** (*i*)

Input labels coming out of state *i*

**Parameters** *i* (`int`) – state

**Returns** set of input labels

**Return type** set of str

New in version 1.0.

**noBlankNames** ()

Eliminates blank names

**Returns** self

**Return type** `FA`

**Attention:** in place transformation

**plus** ()

Plus of a FA (star without the adding of epsilon)

New in version 0.9.6.

**renameState** (*st*, *name*)

Rename a given state.

**Parameters**

- **st** (`int`) – state index.
- **name** (`object`) – name.

**Returns** self.

**Return type** `FA`

---

**Note:** Deals gracefully both with int and str names in the case of name collision.

---

**Attention:** the object is modified in place

**renameStates** (*nameList=None*)

Renames all states using a new list of names.

**Parameters** **nameList** (`list`) – list of new names.

**Returns** self.

**Return type** `FA`

**Raises** `DFAerror` – if provided list is too short.

---

**Note:** If no list of names is given, state indexes are used.

---

**Attention:** the object is modified in place

**reversal** ()

Returns a NFA that recognizes the reversal of the language

**Returns** NFA recognizing reversal language

**Return type** *NFA*

**same\_nullability** (*s1*, *s2*)

Tests if this two states have the same nullability

**Parameters**

- **s1** (*int*) – state index.
- **s2** (*int*) – state index.

**Returns** have the states the same nullability?

**Return type** *bool*

**setFinal** (*statelist*)

Sets the final states of the FA

**Ags:** *statelist* (*intlist/set*): a list (or set) of final states indexes.

**Caution:** Erases any previous definition of the final state set.

**setInitial** (*stateindex*)

Sets the initial state of a FA

**Parameters** **stateindex** (*int*) – index of the initial state.

**setSigma** (*symbolSet*)

Defines the alphabet for the FA.

**Parameters** **symbolSet** (*list/set*) – alphabet symbols

**stateAlphabet** (*sti*)

Active alphabet for this state

**Parameters** **sti** (*int*) – state

**Return type** *list*

**stateIndex** (*name*, *autoCreate=False*)

Index of given state name.

**Parameters**

- **name** (*object*) – name of the state.
- **autoCreate** (*bool*, optional) – flag to create state if not already done.

**Returns** state index

**Return type** *int*



**Raises** `DFAstateUnknown` – if the state name is unknown and `autoCreate==False`

---

**Note:** Replaces `stateName`

---



---

**Note:** If the state name is not known and flag is set creates it on the fly

---

New in version 1.0.

**stateName** (*\*\*kwargs*)

Index of given state name.

**Parameters**

- **name** (*object*) – name of the state
- **autoCreate** (*bool*, optional) – flag to create state if not already done

**Returns** state index

**Return type** `int`

**Raises** `DFAstateUnknown` – if the state name is unknown and `autoCreate==False`

Deprecated since version 1.0: Use: `stateIndex()` instead

**succintTransitions** ()

Colapsed transitions

**union** (*other*)

A simple literate invocation of `__or__`

**Parameters** **other** (*FA*) – right hand operand.

**Returns** Union of self and other.

**Return type** *FA*

**words** (*stringo=True*)

Lexicographical word generator

**Parameters** **stringo** (*bool*, optional) – are words strings? Default is `True`.

**Yields** *Word* – the next word generated.

<p><b>Attention:</b> Does not generate the empty word</p>
---

New in version 0.9.8.

### 2.1.1 Class `SemiDFA` (Semi-Automata class)

**class** `fa.SemiDFA`

Bases: `common.Drawable`

Class of automata without initial or final states

**States**

list of states.

**Type** `list`

**delta**

transition function.

**Type** dict

**Sigma**

alphabet.

**Type** set

**dotDrawState** (*sti*, *sep*='\n')

Dot representation of a state

**Parameters**

- **sti** (*int*) – state index.
- **sep** (*str*, optional) – separator.

**Returns** line to add to the dot file.

**Return type** str

**static dotDrawTransition** (*st1*, *lbl1*, *st2*, *sep*='\n')

Draw a transition in dot format

**Parameters**

- **st1** (*str*) – departing state.
- **lbl1** (*str*) – label.
- **st2** (*str*) – arriving state.
- **sep** (*str*, optional) – separator.

**Returns** line to add to the dot file.

**Return type** str

**dotFormat** (*size*='20, 20', *direction*='LR', *sep*='\n')

Dot format of automata

**Parameters**

- **size** (*str*, optional) – image size.
- **direction** (*str*, optional) – direction of drawing.
- **sep** (*str*, optional) – separator.

**Returns** line to add to the dot file.

**Return type** str

## 2.2 Class OFA (one-way finite automata class)

**class** fa.OFA

Bases: *fa.FA*

Base class for one-way automata .. inheritance-diagram:: OFA

**SPRegExp** ()

Checks if FA is SP (Serial-PARallel), and if so returns the regular expression whose language is recognised by the FA

**Returns** equivalent regular expression

**Return type** *reex.regexp*

**Raises** **NotSP** – if the automaton is not Serial-Parallel

**See also:**

Moreira & Reis, Fundamenta Informatica, Series-Parallel automata and short regular expressions, n.91 3-4, pag 611-629. <http://www.dcc.fc.up.pt/~nam/publica/spa07.pdf>

---

**Note:** Automata must be Serial-Parallel

---

**acyclicP** (*strict=True*)

Checks if the FA is acyclic

**Parameters** **strict** (*bool*) – if not True loops are allowed

**Returns** True if the FA is acyclic

**Return type** *bool*

**addTransition** (*st1, sym, st2*)

Add transition :param int st1: departing state :param str sym: label :param int st2: arriving state

**allRegExps** ()

Evaluates the alphabetic length of the equivalent regular expression using every possible order of state elimination.

**Return type** list of tuples (*int*, list of states)

**cutPoints** ()

Set of FA's cut points

**Returns** set of states

**Return type** set of int

**deleteStates** (*del\_states*)

To be implemented below

**Parameters** **del\_states** (*list*) – states to be deleted

**static dotDrawTransition** (*st1, label, st2, sep='\n'*)

Draw a transition in Dot Format

**Parameters**

- **st1** (*str*) – starting state
- **st2** (*str*) – ending state
- **label** (*str*) – symbol
- **sep** (*str*) – separator

**Return type** *str*

**dump** ()

Returns a python representation of the object

**Returns** the python representation (Tags,States,Sigma,delta,Initial,Final)

**Return type** *tuple*

**dup** ()

Duplicate OFA

**Returns** duplicate object

**eliminateSingles** ()

Eliminates every state that only have one successor and one predecessor.

**Returns** GFA after eliminating states

**Return type** *GFA*

**eliminateStout** (*st*)

Eliminate all transitions outgoing from a given state

**Parameters** **st** (*int*) – the state index to loose all outgoing transitions

<b>Attention:</b> performs in place alteration of the automata
--

New in version 0.9.6.

**emptyP** ()

Tests if the automaton accepts a empty language

**Return type** *bool*

New in version 1.0.

**evalNumberOfStateCycles** ()

Evaluates the number of cycles each state participates

**Returns** state->list of cycle lengths

**Return type** *dict*

**evalSymbol** ()

Eval symbol

**finalCompP** (*s*)

To be implemented below

**Parameters** **s** – state

**Return type** *list*

**initialComp** ()

Initial component

**Return type** *list*

**minimalBrzozowski** ()

Constructs the equivalent minimal DFA using Brzozowski's algorithm

**Returns** equivalent minimal DFA

**Return type** *DFA*

**minimalBrzozowskiP** ()

Tests if the FA is minimal using Brzozowski's algorithm

**Return type** *bool*

**reCG** ()

Regular expression from state elimination whose language is recognised by the FA. Uses a heuristic to choose the order of elimination.

**Returns** the equivalent regular expression

**Return type** *reex.regexp*

**reCG\_nn** ()

Regular expression from state elimination whose language is recognised by the FA. Uses a heuristic to choose the order of elimination. The FA is not normalized before the state elimination.

**Returns** the equivalent regular expression

**Return type** *reex.regexp*

**reDynamicCycleHeuristic** ()

State elimination Heuristic based on the number of cycles that passes through each state. Here those numbers are evaluated dynamically after each elimination step

**Returns** an equivalent regular expression

**Return type** *reex.regexp*

**See also:**

Nelma Moreira, Davide Nabais, and Rogério Reis. State elimination ordering strategies: Some experimental results. Proc. of 11th Workshop on Descriptive Complexity of Formal Systems (DCFS10), pages 169-180.2010. DOI: 10.4204/EPTCS.31.16

**reStaticCycleHeuristic** ()

State elimination Heuristic based on the number of cycles that passes through each state. Here those numbers are evaluated statically in the beginning of the process

**Returns** a equivalent regular expression

**Return type** *reex.regexp*

**See also:**

Nelma Moreira, Davide Nabais, and Rogério Reis. State elimination ordering strategies: Some experimental results. Proc. of 11th Workshop on Descriptive Complexity of Formal Systems (DCFS10), pages 169-180.2010. DOI: 10.4204/EPTCS.31.16

**re\_stateElimination** (*order=None*)

Regular expression from state elimination whose language is recognised by the FA. The FA is normalized before the state elimination.

**Parameters** **order** (*list*) – state elimination sequence

**Returns** the equivalent regular expression

**Return type** *reex.regexp*

**re\_stateElimination\_nn** (*order=None*)

Regular expression from state elimination whose language is recognised by the FA. The FA is not normalized before the state elimination.

**Parameters** **order** (*list*) – state elimination sequence

**Returns** the equivalent regular expression

**Return type** *reex.regexp*

**regexpSE** ()

A regular expression obtained by state elimination algorithm whose language is recognised by the FA.

**Returns** the equivalent regular expression

**Return type** *reex.regexp*

**stateChildren** (\_, \_a=None)

To be implemented below

**Parameters** **s** – state

**Return type** list

**succintTransitions** ()

Collapsed transitions

**toGFA** ()

To be implemented below

**topoSort** ()

Topological order for the FA

**Returns** List of state indexes

**Return type** list of int

---

**Note:** self loops are taken in consideration

---

**trim** ()

Removes the states that do not lead to a final state, or, inclusively, that can't be reached from the initial state. Only useful states remain.

**Attention:** in place transformation

**trimP** ()

Tests if the FA is trim: initially connected and co-accessible

**Returns** bool

**uniqueRepr** ()

Abstract method

**usefulStates** ()

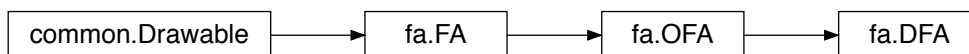
To be implemented below

## 2.3 Class DFA (Deterministic Finite Automata)

**class** `fa.DFA`

Bases: `fa.OFA`

Class for Deterministic Finite Automata.



**Delta** (*state, symbol*)

Evaluates the action of a symbol over a state

**Parameters**

- **state** (*int*) – state index
- **symbol** – symbol

**Returns** the action of symbol over state

**Return type** *int*

**HKeqP** (*other, strict=True*)

Tests the DFA's equivalence using Hopcroft and Karp's state equivalence algorithm

**Parameters** **other** –

**Returns** *bool*

**See also:**

J. E. Hopcroft and R. M. Karp. A Linear Algorithm for Testing Equivalence of Finite Automata. TR 71–114. U. California. 1971

**Attention:** The automaton must be complete.

**MyhillNerodePartition** ()

Myhill-Nerode partition, Moore's way

New in version 1.3.5.

**Attention:** No state should be named with `DeadName`. This states is removed from the obtained partition.

**See also:**

F.Bassino, J.David and C.Nicaud, On the Average Complexity of Moores's State Minimization Algorihm, Symposium on Theoretical Aspects of Computer Science

**aEquiv** ()

Computes almost equivalence, used by hyperMinimalial

**Returns** partition of states

**Return type** dictionary

---

**Note:** may be optimized to avoid dupped

---

**addTransition** (*sti1, sym, sti2*)

Adds a new transition from *sti1* to *sti2* consuming symbol *sym*.

**Parameters**

- **sti1** (*int*) – state index of departure
- **sti2** (*int*) – state index of arrival
- **sym** (*str*) – symbol consumed

**Raises** `DFAnotNFA` – if one tries to add a non deterministic transition

**compat** (*s1*, *s2*, *data*)

Tests compatibility between two states.

**Parameters**

- **data** –
- **s1** (*int*) – state index
- **s2** (*int*) – state index

**Return type** `bool`

**complete** (*dead*=*'Dead'*)

Transforms the automata into a complete one. If Sigma is empty nothing is done.

**Parameters** **dead** (*str*) – dead state name

**Returns** the complete FA

**Return type** `DFA`

---

**Note:** Adds a dead state (if necessary) so that any word can be processed with the automata. The new state is named `dead`, so this name should never be used for other purposes.

---

**Attention:** The object is modified in place.

Changed in version 1.0.

**completeMinimal** ()

Completes a DFA assuming it is a minimal and avoiding de destruction of its minimality If the automaton is not complete, all the non final states are checked to see if they are not already a dead state. Only in the negative case a new (dead) state is added to the automaton.

**Return type** `DFA`

**Attention:** The object is modified in place. If the alphabet is empty nothing is done

**completeP** ()

Checks if it is a complete FA (if delta is total)

**Returns** `bool`

**completeProduct** (*other*)

Product structure

**Parameters** **other** – the other DFA

**computeKernel** ()

The Kernel of a IC DFA is the set of states that accept a non finite language.

**Returns** triple (comp, center , mark) where comp are the strongly connected components, center the set of center states and mark the kernel states

**Return type** `tuple`



**concat** (*fa2*, *strict=False*)

Concatenation of two DFAs. If DFAs are not complete, they are completed.

**Parameters**

- **strict** (*bool*) – should alphabets be checked?
- **fa2** (*DFA*) – the second DFA

**Returns** the result of the concatenation

**Return type** *DFA*

**Raises** **DFAdifferentSigma** – if alphabet are not equal

**concatI** (*fa2*, *strict=False*)

Concatenation of two DFAs.

**Parameters**

- **fa2** (*DFA*) – the second DFA
- **strict** (*bool*) – should alphabets be checked?

**Returns** the result of the concatenation

**Return type** *DFA*

**Raises** **DFAdifferentSigma** – if alphabet are not equal

New in version 0.9.5.

---

**Note:** this is to be used with non complete DFAs

---

**delTransition** (*sti1*, *sym*, *sti2*, *\_no\_check=False*)

Remove a transition if existing and perform cleanup on the transition function's internal data structure.

**Parameters**

- **\_no\_check** (*bool*) – use unsecure code?
- **sti1** (*int*) – state index of departure
- **sti2** (*int*) – state index of arrival
- **sym** (*str*) – symbol consumed

---

**Note:** Unused alphabet symbols will be discarded from Sigma.

---

**deleteState** (*sti*)

Delete state from a DFA

**Parameters** **sti** (*int*) – state insdex

**deleteStates** (*del\_states*)

Delete given iterable collection of states from the automaton.

**Parameters** **del\_states** – collection of int representing states

---

**Note:** in-place action

---

---

**Note:** delta function will always be rebuilt, regardless of whether the states list to remove is a suffix, or a sublist, of the automaton's states list.

---

**static deterministicP** ()

Yes it is deterministic!

**Return type** *bool*

**dist** ()

Evaluate the distinguishability language for a DFA

**Return type** *DFA*

**See also:**

Cezar Câmpeanu, Nelma Moreira, Rogério Reis: The distinguishability operation on regular languages. NCMA 2014: 85-100

New in version 0.9.8.

**distMin** ()

Evaluates the list of minimal words that distinguish each pair of states

**Returns** set of minimal distinguishing words

**Return type** *FL*

New in version 0.9.8.

<b>Attention:</b> If the DFA is not minimal, the method loops forever
---

**distR** ()

Evaluate the right distinguishability language for a DFA

**Return type** *DFA*

**..seealso::** Cezar Câmpeanu, Nelma Moreira, Rogério Reis: The distinguishability operation on regular languages. NCMA 2014: 85-100

**distRMin** ()

Compute distRMin for DFA

:rtype *FL*

**..seealso::** Cezar Câmpeanu, Nelma Moreira, Rogério Reis: The distinguishability operation on regular languages. NCMA 2014: 85-100

**distTS** ()

Evaluate the two-sided distinguishability language for a DFA

**Return type** *DFA*

**..seealso::** Cezar Câmpeanu, Nelma Moreira, Rogério Reis: The distinguishability operation on regular languages. NCMA 2014: 85-100

**dup** ()

Duplicate the basic structure into a new DFA. Basically a copy.deep.

**Return type** *DFA*

**equal** (*other*)

Verify if the two automata are equivalent. Both are verified to be minimum and complete, and then one is matched against the other... Doesn't destroy either dfa...

**Parameters** **other** (DFA) – the other DFA

**Return type** `bool`

**evalSymbol** (*init, sym*)

Returns the state reached from given state through a given symbol.

**Parameters**

- **init** (*int*) – set of current states indexes
- **sym** (*str*) – symbol to be consumed

**Returns** reached state

**Return type** `int`

**Raises**

- **DFAsymbolUnknown** – if symbol not in alphabet
- **DFAstopped** – if transition function is not defined for the given input

**evalSymbolI** (*init, sym*)

Returns the state reached from a given state.

**Parameters**

- **init** (*init*) – current state
- **sym** (*str*) – symbol to be consumed

**Returns** reached state or -1

**Return type** set of int

**Raises** **DFAsymbolUnknown** – if symbol not in alphabet

New in version 0.9.5.

---

**Note:** this is to be used with non complete DFAs

---

**evalSymbolL** (*ls, sym*)

Returns the set of states reached from a given set of states through a given symbol

**Parameters**

- **ls** (*set of int*) – set of states indexes
- **sym** (*str*) – symbol to be read

**Returns** set of reached states

**Return type** set of int

**evalSymbolLI** (*ls, sym*)

Returns the set of states reached from a given set of states through a given symbol

**Parameters**

- **ls** (*set of int*) – set of current states
- **sym** (*str*) – symbol to be consumed

**Returns** set of reached states

**Return type** set of int

New in version 0.9.5.

---

**Note:** this is to be used with non complete DFAs

---

**evalWord** (*wrđ*)

Evaluates a word

**Parameters** **wrđ** (*Word*) – word

**Returns** final state or None

**Return type** int | None

New in version 1.3.3.

**evalWordP** (*word, initial=None*)

Verifies if the DFA recognises a given word

**Parameters**

- **word** (*list of symbols.*) – word to be recognised
- **initial** (*int*) – starting state index

**Return type** bool

**finalCompP** (*s*)

Verifies if there is a final state in strongly connected component containing *s*.

**Parameters** **s** (*int*) – state

**Returns** 1 if yes, 0 if no

**hasTrapStateP** ()

Tests if the automaton has a dead trap state

**Return type** bool

New in version 1.1.

**hyperMinimal** (*strict=False*)

Hyperminimization of a minimal DFA

**Parameters** **strict** (*bool*) – if strict=True it first minimizes the DFA

**Returns** an hyperminimal DFA

**Return type** *DFA*

**See also:**

M. Holzer and A. Maletti, An nlogn Algorithm for Hyper-Minimizing a (Minimized) Deterministic Automata, TCS 411(38-39): 3404-3413 (2010)

---

**Note:** if strict=False minimality is assumed

---

**inDegree** (*st*)

Returns the in-degree of a given state in an FA

**Parameters** **st** (*int*) – index of the state

**Return type** `int`

**infix** ()

Returns a dfa that recognizes infix(L(a))

**Return type** `DFA`

**initialComp** ()

Evaluates the connected component starting at the initial state.

**Returns** list of state indexes in the component

**Return type** list of int

**initialP** (*state*)

Tests if a state is initial

**Parameters** **state** (*int*) – state index

**Return type** `bool`

**initialSet** ()

The set of initial states

**Returns** the set of the initial states

**Return type** set of States

**joinStates** (*lst*)

Merge a list of states.

**Parameters** **lst** (*iterable of state indexes.*) – set of equivalent states

**makeReversible** ()

Make a DFA reversible (if possible)

**See also:**

M.Holzer, S. Jakobi, M. Kutrib ‘Minimal Reversible Deterministic Finite Automata’

**Return type** `DFA`

**markNonEquivalent** (*s1, s2, data*)

Mark states with indexes *s1* and *s2* in given map as non equivalent states. If any back-effects exist, apply them.

**Parameters**

- **s1** (*int*) – one state’s index
- **s2** (*int*) – the other state’s index
- **data** – the matrix relating *s1* and *s2*

**mergeStates** (*f, t*)

Merge the first given state into the second. If the first state is an initial state the second becomes the initial state.

**Parameters**

- **f** (*int*) – index of state to be absorbed
- **t** (*int*) – index of remaining state

**Attention:** It is up to the caller to remove the disconnected state. This can be achieved with ``trim()`.

**minimal** (*method='minimalHopcroft', complete=True*)

Evaluates the equivalent minimal complete DFA

**Parameters**

- **method** – method to use in the minimization
- **complete** (*bool*) – should the result be completed?

**Returns** equivalent minimal DFA

**Return type** *DFA*

**minimalHopcroft** ()

Evaluates the equivalent minimal complete DFA using Hopcroft algorithm

**Returns** equivalent minimal DFA

**Return type** *DFA*

**See also:**

John Hopcroft, An  $n \log\{n\}$  algorithm for minimizing states in a finite automaton. The Theory of Machines and Computations. AP. 1971

**minimalHopcroftP** ()

Tests if a DFA is minimal

**Return type** *bool*

**minimalIncremental** (*minimal\_test=False*)

Minimizes the DFA with an incremental method using the Union-Find algorithm and memoized non-equivalence intermediate results

**Parameters** **minimal\_test** (*bool*) – starts by verifying that the automaton is not minimal?

**Returns** equivalent minimal DFA

**Return type** *DFA*

**See also:**

M. Almeida and N. Moreira and R. Reis. Incremental DFA minimisation. CIAA 2010. LNCS 6482. pp 39-48. 2010

**minimalIncrementalP** ()

Tests if a DFA is minimal

**Return type** *bool*

**minimalMoore** ()

Evaluates the equivalent minimal automata with Moore's algorithm

**See also:**

John E. Hopcroft and Jeffrey D. Ullman, Introduction to Automata Theory, Languages, and Computation, AW, 1979

**Returns** minimal complete DFA

**Return type** *DFA*

**minimalMooreSq** ()

Evaluates the equivalent minimal complete DFA using Moore's (quadratic) algorithm

**See also:**

John E. Hopcroft and Jeffrey D. Ullman, Introduction to Automata Theory, Languages, and Computation, AW, 1979

**Returns** equivalent minimal DFA

**Return type** *DFA*

**minimalMooreSqP** ()

Tests if a DFA is minimal using the quadratic version of Moore's algorithm

**Return type** *bool*

**minimalNCompleteP** ()

Tests if a non necessarily complete DFA is minimal, i.e., if the DFA is non complete, if the minimal complete has only one more state.

**Returns** True if not minimal

**Return type** *bool*

**Attention:** obsolete: use minimalP

**minimalNotEquivP** ()

Tests if the DFA is minimal by computing the set of distinguishable (not equivalent) pairs of states

**Return type** *bool*

**minimalP** (*method='minimalMooreSq'*)

Tests if the DFA is minimal

**Parameters** *method* – the minimization algorithm to be used

**Return type** *bool*

..note: if DFA non complete test if complete minimal has one more state

**minimalWatson** (*test\_only=False*)

Evaluates the equivalent minimal complete DFA using Watson's incremental algorithm

**Parameters** *test\_only* (*bool*) – is it only to test minimality

**Returns** equivalent minimal DFA

**Return type** *DFA*

**Raises** *DFAnotComplete* – if automaton is not complete

..attention:: automaton must be complete

**minimalWatsonP** ()

Tests if a DFA is minimal using Watson's incremental algorithm

**Return type** *bool*

**notequal** (*other*)

Test non equivalence of two DFAs

**Parameters** *other* (*DFA*) – the other DFA

**Return type** `bool`

**orderedStrConnComponents** ()  
Topological ordered list of strong components  
New in version 1.3.3.

**Return type** `list`

**pairGraph** ()  
Returns pair graph

**Return type** `DiGraphVM`

**See also:**

A graph theoretic approach to automata minimality. Antonio Restivo and Roberto Vaglica. Theoretical Computer Science, 429 (2012) 282-291. doi:10.1016/j.tcs.2011.12.049 Theoretical Computer Science, 2012 vol. 429 (C) pp. 282-291. http://dx.doi.org/10.1016/j.tcs.2011.12.049

**possibleToReverse** ()  
Tests if language is reversible  
New in version 1.3.3.

**pref** ()  
Returns a dfa that recognizes `pref(L(self))`

**Return type** `DFA`

New in version 1.1.

**print\_data** (`data`)  
Prints table of compatibility (in the context of the minimalization algorithm).

**Parameters** `data` – data to print

**product** (`other`)  
Returns a DFA resulting of the simultaneous execution of two DFA. No final states set.

---

**Note:** this is a fast version of the method. The resulting state names are not meaningful.

---

**Parameters** `other` – the other DFA

**Return type** `DFA`

**productSlow** (`other`, `complete=True`)  
Returns a DFA resulting of the simultaneous execution of two DFA. No final states set.

---

**Note:** this is a slow implementation for those that need meaningful state names

---

New in version 1.3.3.

**Parameters**

- `other` – the other DFA
- `complete` (`bool`) – evaluate product as a complete DFA

**Return type** `DFA`



**regex** ()

Returns a regexp for the current DFA considering the recursive method. Very inefficient.

**Returns** a regexp equivalent to the current DFA

**Return type** *reex.regexp*

**reorder** (*dicti*)

Reorders states according to given dictionary. Given a dictionary (not necessarily complete)... reorders states accordingly.

**Parameters** **dicti** (*dict*) – reorder dictionary

**reverseTransitions** (*rev*)

Evaluate reverse transition function.

**Parameters** **rev** (*DFA*) – DFA in which the reverse function will be stored

**reversibleP** ()

Test if an automaton is reversible

**Return type** *bool*

**sMonoid** ()

Evaluation of the syntactic monoid of a DFA

**Returns** the semigroup

**Return type** *SSemiGroup*

**sSemigroup** ()

Evaluation of the syntactic semigroup of a DFA

**Returns** the semigroup

**Return type** *SSemiGroup*

**shuffle** (*other, strict=False*)

Shuffle of two languages: L1 W L2

**Parameters**

- **other** (*DFA*) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

**See also:**

C. Câmpeanu, K. Salomaa and S. Yu, *Tight lower bound for the state complexity of shuffle of regular languages*. J. Autom. Lang. Comb. 7 (2002) 303–310.

**simDiff** (*other*)

Symmetrical difference

**Parameters** **other** –

**Returns**

**sop** (*other*)

Strange operation

**Parameters** **other** (*DFA*) – the other automaton

**Return type** *DFA*

**See also:**

Nelma Moreira, Giovanni Pighizzini, and Rogério Reis. Universal disjunctive concatenation and star. In Jeffrey Shallit and Alexander Okhotin, editors, Proceedings of the 17th Int. Workshop on Descriptive Complexity of Formal Systems (DCFS15), number 9118 in LNCS, pages 197–208. Springer, 2015.

New in version 1.2b2.

**star** (*flag=False*)

Star of a DFA. If the DFA is not complete, it is completed.

..versionchanged: 0.9.6

**Parameters** **flag** (*bool*) – plus instead of star

**Returns** the result of the star

**Return type** *DFA*

**starI** ()

Star of an incomplete DFA.

**Returns** the Kleene closure DFA

**Return type** *DFA*

**stateChildren** (*state, strict=False*)

Set of children of a state

**Parameters**

- **strict** (*bool*) – if not strict a state is never its own child even if a self loop is in place
- **state** (*int*) – state id queried

**Returns** map children -> multiplicity

**Return type** dictionary

**stronglyConnectedComponents** ()

Dummy method that uses the NFA counterpart

New in version 1.3.3.

**Return type** *list*

**subword** ()

Returns a dfa that recognizes subword(L(self))

**Return type** *dfa*

New in version 1.1.

**succintTransitions** ()

Collects the transition information in a compact way suitable for graphical representation. :rtype: list of tuples

New in version 0.9.8.

**suff** ()

Returns a dfa that recognizes suff(L(self))

**Return type** *DFA*

New in version 0.9.8.

**syncPower** ()

Evaluates the power automata for the action of each symbol

**Returns** The power automata being the set of all states the initial state and all singleton states final.

**Return type** *DFA*

**syncWords** ()

Evaluates the regular expression corresponding to the synchronizing pwords of the automata.

**Returns** a regular expression of the sync words of the automata

**Return type** *reex.regexp*

**toADFA** ()

Try to convert DFA to ADFA

**Returns** the same automaton as a ADFA

**Return type** *ADFA*

**Raises** **notAcyclic** – if this is not an acyclic DFA

New in version 1.2.

Changed in version 1.2.1.

**toDFA** ()

Dummy function. It is already a DFA

**Returns** a self deep copy

**Return type** *DFA*

**toGFA** ()

Creates a GFA equivalent to DFA

**Returns** GFA deep copy

**Return type** *GFA*

**toNFA** ()

Migrates a DFA to a NFA as dup()

**Returns** DFA seen as new NFA

**Return type** *NFA*

**transitions** ()

Iterator over transitions :rtype: symbol, int

**transitionsA** ()

Iterator over transitions :rtype: symbol, int

**uniqueRepr** ()

Normalise unique string for the string icdfa's representation.

**See also:**

TCS 387(2):93-102, 2007 <http://www.ncc.up.pt/~nam/publica/tcsamr06.pdf>

**Returns** normalised representation

**Return type** *list*

**Raises** **DFAnotComplete** – if DFA is not complete

**universalP** (*minimal=False*)

Checks if the automaton is universal through minimisation

**Parameters** **minimal** (*bool*) – is the automaton already minimal?

**Return type** *bool*

**unmark** ()

Unmarked NFA that corresponds to a marked DFA: in which each alphabetic symbol is a tuple (symbol, index)

**Returns** a NFA

**Return type** *NFA*

**usefulStates** (*initial\_states=None*)

Set of states reachable from the given initial state(s) that have a path to a final state.

**Parameters** **initial\_states** (*iterable of int*) – starting states

**Returns** set of state indexes

**Return type** set of int

**static vDescription** ()

Generation of Verso interface description

New in version 0.9.5.

**Returns** the interface list

**witness** ()

Witness of non emptyness

**Returns** word

**Return type** *str*

**witnessDiff** (*other*)

Returns a witness for the difference of two DFAs and:

0	if the witness belongs to the <b>other</b> language
1	if the witness belongs to the <b>self</b> language

**Parameters** **other** (*DFA*) – the other DFA

**Returns** a witness word

**Return type** list of symbols

**Raises** **DFAequivalent** – if automata are equivalent

## 2.4 Class NFA (Nondeterministic Finite Automata)

**class** *fa.NFA*

Bases: *fa.OFA*

Class for Non-deterministic Finite Automata (epsilon-transitions allowed).



**HKeqP** (*other, strict=True*)

Test NFA equivalence with extended Hopcroft-Karp method

**See also:**

J. E. Hopcroft and R. M. Karp. A Linear Algorithm for Testing Equivalence of Finite Automata. TR 71-114. U. California. 1971

**Parameters**

- **other** – NFA
- **strict** – if True checks for same alphabets

**Returns** Boolean

**addEpsilonLoops** ()

Add epsilon loops to every state :return: self

**Attention:** in-place modification

New in version 1.0.

**addInitial** (*stateindex*)

Add a new state to the set of initial states.

**Parameters** **stateindex** (*int*) – index of new initial state

**addTransition** (*sti1, sym, sti2*)

Adds a new transition. Transition is from *sti1* to *sti2* consuming symbol *sym*. *sti2* is a unique state, not a set of them.

**Parameters**

- **sti1** (*int*) – state index of departure
- **sti2** (*int*) – state index of arrival
- **sym** (*str*) – symbol consumed

**addTransitionQ** (*srcI, dest, symb, qfuture, qpast*)

Add transition to the new transducer instance.

**Parameters**

- **qpast** (*set*) – past queue
- **qfuture** (*set*) – future queue
- **symb** – symbol
- **dest** – destination state

- **srcI** (*int*) – source state

New in version 1.0.

**autobisimulation** ()

Largest right invariant equivalence between states of the NFA

**Returns** Incomplete equivalence relation (transitivity, and reflexivity not calculated) as a set of unordered pairs of states

**Return type** Set of frozensets

**See also:**

Ilie&Yu, 2003

**autobisimulation2** ()

Alternative space-efficient definition of NFA.autobisimulation.

**Returns** Incomplete equivalence relation (reflexivity, symmetry, and transitivity not calculated) as a set of pairs of states

**Return type** list of tuples

**closeEpsilon** (*st*)

Add all non epsilon transitions from the states in the epsilon closure of given state to given state.

**Parameters** **st** (*int*) – state index

**computeFollowNames** ()

Computes the follow set to use in names

**Return type** list

**concat** (*other, middle='middle'*)

Concatenation of NFA

**Parameters**

- **middle** (*str*) – glue state name
- **other** (*NFA/DFA*) – the other NFA

**Returns** the result of the concatenation

**Return type** *NFA*

**countTransitions** ()

Number of transitions of a NFA

**Return type** *int*

**delTransition** (*sti1, sym, sti2, \_no\_check=False*)

Remove a transition if existing and perform cleanup on the transition function's internal data structure.

**Parameters**

- **sti1** (*int*) – state index of departure
- **sti2** (*int*) – state index of arrival
- **sym** (*str*) – symbol consumed
- **\_no\_check** (*bool*) – dismiss secure code

---

**Note:** unused alphabet symbols will be discarded from Sigma.

---

**deleteStates** (*del\_states*)

Delete given iterable collection of states from the automaton.

**Parameters** **del\_states** (*set/list*) – collection of int representing states

---

**Note:** delta function will always be rebuilt, regardless of whether the states list to remove is a suffix, or a sublist, of the automaton's states list.

---

**detSet** (*generic=False*)

Computes the determination upon a followFromPosition result

**Return type** *NFA*

**deterministicP** ()

Verify whether this NFA is actually deterministic

**Return type** *bool*

**dotFormat** (*size='20, 20', direction='LR', sep='\n', strict=False, maxLblSz=6*)

A dot representation

**Parameters**

- **direction** (*str*) – direction of drawing
- **size** (*str*) – size of image
- **sep** (*str*) – line separator
- **maxLblSz** – max size of labels before getting removed
- **strict** – use limitations of label sizes

**Returns** the dot representation

**Return type** *str*

New in version 0.9.6.

Changed in version 1.2.1.

**dup** ()

Duplicate the basic structure into a new NFA. Basically a copy.deep.

**Return type** *NFA*

**elimEpsilon** ()

Eliminate epsilon-transitions from this automaton.

:rtype : *NFA*

**Attention:** performs in place modification of automaton

Changed in version 1.1.1.

**eliminateEpsilonTransitions** ()

Eliminates all epsilon-transitions with no state addition

**Attention:** in-place modification

**eliminateTSymbol** (*symbol*)

Delete all transitions through a given symbol

**Parameters** **symbol** (*str*) – the symbol to be excluded from delta

**Attention:** in place alteration of the automata

New in version 0.9.6.

**epsilonClosure** (*st*)

Returns the set of states epsilon-connected to from given state or set of states.

**Parameters** **st** (*int/set*) – state index or set of state indexes

**Returns** the list of state indexes epsilon connected to *st*

**Return type** set of int

**Attention:** *st* must exist.

**epsilonP** ()

Whether this NFA has epsilon-transitions

**Return type** bool

**epsilonPaths** (*start, end*)

All states in all paths (DFS) through empty words from a given starting state to a given ending state.

**Parameters**

- **start** (*int*) – start state
- **end** (*int*) – end state

**Returns** states in epsilon paths from start to end

**Return type** set of states

**equivReduced** (*equiv\_classes*)

Equivalent NFA reduced according to given equivalence classes.

**Parameters** **equiv\_classes** (*UnionFind*) – Equivalence classes

**Returns** Equivalent NFA

**Return type** *NFA*

**evalSymbol** (*stil, sym*)

Set of states reachable from given states through given symbol and epsilon closure.

**Parameters**

- **stil** (*set/list*) – set of current states
- **sym** (*str*) – symbol to be consumed

**Returns** set of reached state indexes

**Return type** *set*

**Raises** **DFASymbolUnknown** – if symbol is not in alphabet



**evalWordP** (*word*)

Verify if the NFA recognises given word.

**Parameters** **word** (*str*) – word to be recognised

**Return type** `bool`

**finalCompP** (*s*)

Verify whether there is a final state in strongly connected component containing given state.

**Parameters** **s** (*int*) – state index

**Returns** `:: bool`

**followFromPosition** ()

computes follow automaton from a position automaton :rtype: NFA

**half** ()

Half operation

New in version 0.9.6.

**hasTransitionP** (*state, symbol=None, target=None*)

Whether there's a transition from given state, optionally through given symbol, and optionally to a specific target.

**Parameters**

- **state** (*int*) – source state
- **symbol** (*str*) – optional transition symbol
- **target** (*int*) – optional target state

**Returns** if there is a transition

**Return type** `bool`

**homogeneousFinalityP** ()

Tests if states have incoming transitions froms states with different finalities

**Return type** `bool`

**homogenousP** (*x*)

Whether this NFA is homogenous; that is, for all states, whether all incoming transitions to that state are through the same symbol.

**Parameters** **x** – dummy parameter to agree with the method in DFAR

**Return type** `bool`

**initialComp** ()

Evaluate the connected component starting at the initial state.

**Returns** list of state indexes in the component

**Return type** list of int

**lEquivNFA** ()

Equivalent NFA obtained from merging equivalent states from autobisimulation of this NFA's reversal.

**Return type** *NFA*

---

**Note:** returns copy of self if autobisimulation renders no equivalent states.

---

**lrEquivNFA()**

Equivalent NFA obtained from merging equivalent states from autobisimulation of this NFA, and from autobisimulation of its reversal; i.e., merges all states that are equivalent w.r.t. the largest right invariant and largest left invariant equivalence relations.

**Return type** *NFA*

---

**Note:** returns copy of self if autobisimulations render no equivalent states.

---

**minimal()**

Evaluates the equivalent minimal DFA

**Returns** equivalent minimal DFA

**Return type** *DFA*

**minimalDFA()**

Evaluates the equivalent minimal complete DFA

**Returns** equivalent minimal DFA

**Return type** *DFA*

**oldAnd(*other*)**

Conjunction of automata

**Parameters** *other* (*NFA / DFA*) – the right hand operand

**Return type** *NFA*

**Raises** **FAdoGeneralError** – if any operand is not an NFA

**product(*other*)**

Returns a NFA (skeleton) resulting of the simultaneous execution of two DFA.

**Parameters** *other* (*NFA*) – the other automata

**Return type** *NFA*

---

**Note:** No final states are set.

---

**Attention:**

- the name `EmptySet` is used in a unique special state name
- the method uses 3 internal functions for simplicity of code (really!)

**rEquivNFA()**

Equivalent NFA obtained from merging equivalent states from autobisimulation of this NFA.

**Return type** *NFA*

---

**Note:** returns copy of self if autobisimulation renders no equivalent states.

---

**renameStatesFromPosition()**

Rename states of a Glushkov automaton using the positions of the marked RE

**Return type** *NFA*

**reorder** (*dicti*)

Reorder states indexes according to given dictionary.

**Parameters** **dicti** (*dict*) – state name reorder

---

**Note:** dictionary does not have to be complete

---

**reversal** ()

Returns a NFA that recognizes the reversal of the language

**Returns** NFA recognizing reversal language

**Return type** *NFA*

**reverseTransitions** (*rev*)

Evaluate reverse transition function.

**Parameters** **rev** (*NFA*) – NFA in which the reverse function will be stored

**setInitial** (*statelist*)

Sets the initial states of an NFA

**Parameters** **statelist** (*set/list/int*) – an iterable of initial state indexes

**shuffle** (*other*)

Shuffle of a NFA

**Parameters** **other** (*FA*) – an FA

**Returns** the resulting NFA

**Return type** *NFA*

**star** (*flag=False*)

Kleene star of a NFA

**Parameters** **flag** (*bool*) – plus instead of star

**Returns** the resulting NFA

**Return type** *NFA*

**stateChildren** (*state, strict=False*)

Set of children of a state

**Parameters**

- **strict** (*bool*) – if not strict a state is never its own child even if a self loop is in place
- **state** (*int*) – state id queried

**Returns** children states

**Return type** Set of int

**stronglyConnectedComponents** ()

Strong components

**Return type** *list*

New in version 1.0.

**subword** ()

returns a nfa that recognizes subword(L(self))

**Return type** *nfa*

**succintTransitions** ()

Collects the transition information in a compact way suitable for graphical representation. :rtype: list

**toDFA** ()

Construct a DFA equivalent to this NFA, by the subset construction method.

**Return type** *DFA*

---

**Note:** valid to epsilon-NFA

---

**toGFA** ()

Creates a GFA equivalent to NFA

**Returns** a GFA deep copy

**Return type** *GFA*

**toNFA** ()

Dummy identity function

**Return type** *NFA*

**toNFAr** ()

NFA with the reverse mapping of the delta function.

**Returns** shallow copy with reverse delta function added

**Return type** *NFAr*

**uniqueRepr** ()

Dummy representation. Used DFA.uniqueRepr() :rtype: tuple

**usefulStates** (*initial\_states=None*)

Set of states reachable from the given initial state(s) that have a path to a final state.

**Parameters** *initial\_states* (*set of int or list of int*) – set of initial states

**Returns** set of state indexes

**Return type** set of int

**static vDescription** ()

Generation of Verso interface description

New in version 0.9.5.

**Returns** the interface list

**witness** ()

Witness of non emptyness

**Returns** word

**Return type** *str*

**wordImage** (*word, ist=None*)

Evaluates the set of states reached consuming given word

**Parameters**

- **word** (*list of strings*) – the word
- **ist** (*int*) – starting state index (or set of)

**Returns** the set of ending states

**Return type** Set of int

## 2.5 Class NFAr (Nondeterministic Finite Automata w/ reverse transition f.)

**class** `fa.NFAr`

Bases: `fa.NFA`

Class for Non-deterministic Finite Automata with reverse delta function added by construction.



**Variables** `deltaReverse` – the reversed transition function

---

**Note:** Includes efficient methods for merging states.

---

**addTransition** (`sti1`, `sym`, `sti2`)

Adds a new transition. Transition is from `sti1` to `sti2` consuming symbol `sym`. `sti2` is a unique state, not a set of them. Reversed transition function is also computed

**Parameters**

- **sti1** (`int`) – state index of departure
- **sti2** (`int`) – state index of arrival
- **sym** (`str`) – symbol consumed

**delTransition** (`sti1`, `sym`, `sti2`, `_no_check=False`)

Remove a transition if existing and perform cleanup on the transition function's internal data structure and in the reversal transition function

**Parameters**

- **sti1** (`int`) – state index of departure
- **sti2** (`int`) – state index of arrival
- **sym** (`str`) – symbol consumed
- **\_no\_check** (`bool`) – dismiss secure code

**deleteStates** (`del_states`)

Delete given iterable collection of states from the automaton. Performe deletion in the transition function and its reversal.

**Parameters** `del_states` (`set` or `list` of `int`) – collection of int representing states

**elimEpsilonO** ()

Eliminate epsilon-transitions from this automaton, with reduction of states through elimination of epsilon-cycles, and single epsilon-transition cases.

**Returns** itself

**Return type**

**Attention:** performs inplace modification of automaton

**homogenousP** (*inplace=False*)

Checks is the automaton is homogenous, i.e.the transitions that reaches a state have all the same label.

**Parameters** **inplace** (*bool*) – if True performs epsilon transitions elimination

**Returns** True if homogenous

**Return type** *bool*

**mergeStates** (*f, t*)

Merge the first given state into the second. If first state is an initial or final state, the second becomes respectively an initial or final state.

**Parameters**

- **f** (*int*) – index of state to be absorbed
- **t** (*int*) – index of remaining state

**Attention:** It is up to the caller to remove the disconnected state. This can be achieved with `trim()`.

**mergeStatesSet** (*tomerge, target=None*)

Merge a set of states with a target merge state. If the states in the set have transitions among them, those transitions will be directly merged into the target state.

**Parameters**

- **tomerge** (*Set of int*) – set of states to merge with target
- **target** (*int*) – optional target state

---

**Note:** if target state is not given, the minimal index will be considered.

---

**Attention:** The states of the list will become unreachable, but won't be removed. It is up to the caller to remove them. That can be achieved with `trim()`.

**toNFA** ()

Turn into an instance of NFA, and remove the reverse mapping of the delta function.

**Returns** shallow copy without reverse delta function

**Return type** *NFA*

**unlinkSoleIncoming** (*state*)

If given state has only one incoming transition (indegree is one), and it's through epsilon, then remove such transition and return the source state.

**Parameters** **state** (*int*) – state to check

**Returns** source state

**Return type** *int* or *None*

---

**Note:** if conditions aren't met, returned source state is None, and automaton remains unmodified.

---

**unlinkSoleOutgoing** (*state*)

If given state has only one outgoing transition (outdegree is one), and it's through epsilon, then remove such transition and return the target state.

**Parameters** *state* (*int*) – state to check

**Returns** target state

**Return type** *int* or None

---

**Note:** if conditions aren't met, returned target state is None, and automaton remains unmodified.

---

## 2.6 Class GFA (Generalized Finite Automata)

**class** `fa.GFA`

Bases: `fa.OFA`

Class for Generalized Finite Automata: NFA with a unique initial state and transitions are labeled with regexp.



**DFS** (*io*)

Depth first search

**Parameters** *io* –

**addTransition** (*sti1*, *sym*, *sti2*)

Adds a new transition from *sti1* to *sti2* consuming symbol *sym*. Label of the transition function is a regexp.

**Parameters**

- **sti1** (*int*) – state index of departure
- **sti2** (*int*) – state index of arrival
- **sym** (*str*) – symbol consumed

**Raises** `DFAepsilonRedefinition` – if *sym* is Epsilon

**assignLow** (*st*)

**Parameters** *st* –

**assignNum** (*st*)

**Parameters** *st* –

**completeDelta** ()

Adds empty set transitions between the automaton's final and initial states in order to make it complete. It's only meant to be used in the final stage of SEA...

**deleteState** (*sti*)

Deletes a state from the GFA :param sti:

**deleteStates** (*del\_states*)

To be implemented below

**Parameters** *del\_states* (*list*) – states to be deleted

**dfs\_visit** (*s, visited, io*)

**Parameters**

- *s* – state
- **visited** – list of states visited
- *io* –

**dup** ()

Returns a copy of a GFA

**Return type** *GFA*

**eliminate** (*st*)

Eliminate a state.

**Parameters** *st* (*int*) – state to be eliminated

**eliminateAll** (*lr*)

Eliminate a list of states.

**Parameters** *lr* (*list*) – list of states indexes

**eliminateState** (*st*)

Deletes a state and updates the automaton

**Parameters** *st* (*int*) – the state to be deleted

**evalSymbol** ()

Eval symbol

**finalCompP** (*s*)

To be implemented below

**Parameters** *s* – state

**Return type** *list*

**initialComp** ()

Initial component

**Return type** *list*

**normalize** ()

Create a single initial and final state with Epsilon transitions.

**Attention:** works in place



**reorder** (*dictio*)

Reorder states indexes according to given dictionary.

**Parameters** **dictio** (*dict*) – order

---

**Note:** dictionary does not have to be complete

---

**stateChildren** (*state, strict=False*)

Set of children of a state

**Parameters**

- **strict** (*bool*) – a state is never its own children even if a self loop is in place
- **state** (*int*) – state id queried

**Returns** map: children -> alphabetic length

**Return type** dictionary

**succintTransitions** ()

Collapsed transitions

**toGFA** ()

To be implemented below

**uniqueRepr** ()

Abstract method

**usefulStates** ()

To be implemented below

**weight** (*state*)

Calculates the weight of a state based on a heuristic

**Parameters** **state** (*int*) – state

**Returns** the weight of the state

**Return type** *int*

**weightWithCycles** (*state, cycles*)

**Parameters**

- **state** –
- **cycles** –

**Returns**

## 2.7 Class SSemiGroup (Syntactic SemiGroup)

**class** *fa*.SSemiGroup

Bases: *object*

Class support for the Syntactic SemiGroup.

**Variables**

- **elements** – list of tuples representing the transformations
- **words** – a list of pairs (index of the prefix transformation, index of the suffix char)

- **gen** – a list of the max index of each generation
- *Sigma* – set of symbols

**WordI** (*i*)

Representative of an element given as index

**Parameters** **i** (*int*) – index of the element

**Returns** the first word originating the element

**Return type** *str*

**WordPS** (*pref, sym*)

Representative of an element given as prefix symb

**Parameters**

- **pref** (*int*) – prefix index
- **sym** (*int*) – symbol index

**Returns** *word*

**Return type** *str*

**add** (*tr, pref, sym, tmpLists*)

Try to add a new transformation to the monoid

**Parameters**

- **tr** (*tuple of int*) – transformation
- **pref** (*int or None*) – prefix of the generating word
- **sym** (*int*) – suffix symbol
- **tmpLists** (*pairs of lists as (elements, words)*) – this generation lists

**addGen** (*tmpLists*)

Add a new generation to the monoid

**Parameters** **tmpLists** (*pair of lists as (elements, words)*) – the new generation data

## 2.8 Class EnumL (Language Enumeration)

## 2.9 Functions

**fa.saveToString** (*aut, sep='&'*)

Finite automata definition as a string using the input format.

New in version 0.9.5.

Changed in version 0.9.6: Names are now used instead of indexes.

Changed in version 0.9.7: New format with quotes and alphabet

**Parameters**

- **aut** (*FA*) – the FA
- **sep** (*str*) – separation between *lines*

**Returns** the representation

**Return type** *str*

`fa.stringToDFA(s, f, n, k)`

Converts a string icdfa's representation to dfa.

**Parameters**

- **s** (*list*) – canonical string representation
- **f** (*list*) – bit map of final states
- **n** (*int*) – number of states
- **k** (*int*) – number of symbols

**Returns** a complete dfa with Sigma [k], States [n]

**Return type** *DFA*

Changed in version 0.9.8: symbols are converted to str



## MODULE: COMMON DEFINITIONS (COMMON)

Common definitions for FAdo files

### 3.1 Class Word

**class** `common.Word` (*data=None, it=None*)

Bases: `object`

Class to implement generic words as iterables with pretty-print

Basically a unified way to deal with words with characters of of sizes different of one with no much fuss



## MODULE: FADO IO FUNCTIONS (FIO)

### In/Out.

FAdo IO.

```
# ----- # Class ParserFAdo (Yappy parser for FAdo FA files) #  
----- ## .. autoclass:: ParserFAdo # :no-members:
```

## 4.1 Functions

`fio.readFromFile` (*FileName*)

Reads list of finite automata definition from a file.

**Parameters** `FileName` (*str*) – file name

**Return type** `list`

The format of these files must be the as simple as possible:

- # begins a comment
- @DFA or @NFA begin a new automata (and determines its type) and must be followed by the list of the final states separated by blanks
- fields are separated by a blank and transitions by a CR: `state symbol new state`
- in case of a NFA declaration, the “symbol” @epsilon is interpreted as a epsilon-transition
- the source state of the first transition is the initial state
- in the case of a NFA, its declaration @NFA can, after the declaration of the final states, have a \* followed by the list of initial states
- both, NFA and DFA, may have a declaration of alphabet starting with a \$ followed by the symbols of the alphabet
- a line with a sigle name, decrares a state

```
FAdo      ::= FA | FA CR FAdo  
FA        ::= DFA | NFA | Transducer  
DFA       ::= "@DFA" LsStates Alphabet CR dTrans  
NFA       ::= "@NFA" LsStates Initials Alphabet CR nTrans  
Transducer ::= "@Transducer" LsStates Initials Alphabet Output CR tTrans  
Initials  ::= "*" LsStates | \epsilon  
Alphabet  ::= "$" LsSymbols | \epsilon  
Output    ::= "$" LsSymbols | \epsilon  
nSymbol   ::= symbol | "@epsilon"  
LsStates  ::= stateid | stateid , LsStates  
LsSymbols ::= symbol | symbol , LsSymbols
```

```
dTrans ::= stateid symbol stateid |
        | stateid symbol stateid CR dTrans
nTrans ::= stateid nSymbol stateid |
        | stateid nSymbol stateid CR nTrans
tTrans ::= stateid nSymbol nSymbol stateid |
        | stateid nSymbol nSymbol stateid CR nTrans
```

---

**Note:** If an error occur, either syntactic or because of a violation of the declared automata type, an exception is raised

---

Changed in version 0.9.6.

Changed in version 1.0.

`fiO.saveToFile` (*FileName*, *fa*, *mode*='a')

Saves a list finite automata definition to a file using the input format

Changed in version 0.9.5.

Changed in version 0.9.6.

Changed in version 0.9.7: New format with quotes and alphabet

#### Parameters

- **FileName** (*str*) – file name
- **fa** (*list of FA*) – the FA
- **mode** (*str*) – writing mode



## MODULE: REGULAR EXPRESSIONS (REEX)

### Regular expressions manipulation

Regular expression classes and manipulation

## 5.1 Class `RegularExpression`

**class** `reex.RegularExpression`

Bases: `object`

Abstract base class for all regular expression objects

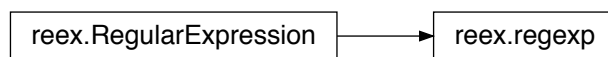
## 5.2 Class `regexp` (regular expression)

**class** `reex.regexp` (*sigma=None*)

Bases: `reex.RegularExpression`

Base class for regular expressions.

**Variables** *Sigma* – alphabet set of strings



**alphabeticLength** ()

Number of occurrences of alphabet symbols in the regular expression.

**Return type** integer

**Attention:** Doesn't include the empty word.

**compare** (*r*, *cmp\_method='compareMinimalDFA'*, *nfa\_method='nfaPD'*)

Compare with another regular expression for equivalence. :param r: :param cmp\_method: :param nfa\_method:

**compareMinimalDFA** (*r*, *nfa\_method*='nfaPosition')

Compare with another regular expression for equivalence through minimal DFAs. :param r: :param nfa\_method:

**dfaAuPoint** ()

DFA “au-point” according to Nipkow

**Returns** “au-point” DFA

**Return type** *fa.DFA*

**See also:**

Andrea Asperti, Claudio Sacerdoti Coen and Enrico Tassi, Regular Expressions, au point. arXiv 2010

**See also:**

Tobias Nipkow and Dmitriy Traytel, Unified Decision Procedures for Regular Expression Equivalence

**dfaBrzozowski** (*memo*=None)

Word derivatives automaton of the regular expression

**Returns** word derivatives automaton

**Return type** *DFA*

**See also:**

J. A. Brzozowski, Derivatives of Regular Expressions. J. ACM 11(4): 481-494 (1964)

**dfaYMG** ()

DFA Yamada-McNaughton-Gluskov according to Nipkow

**Returns** Y-M-G DFA

**Return type** *DFA*

**See also:**

Tobias Nipkow and Dmitriy Traytel, Unified Decision Procedures for Regular Expression Equivalence

**static emptysetP** ()

Whether the regular expression is the empty set.

**Return type** Boolean

**epsilonLength** ()

Number of occurrences of the empty word in the regular expression.

**Return type** integer

**epsilonP** ()

Whether the regular expression is the empty word.

**Return type** Boolean

**equivP** (*other*, *strict*=True)

Test RE equivalence with extended Hopcroft-Karp method

**Parameters**

- **other** – RE
- **strict** – if True checks for same alphabets

**Returns** Boolean

**equivalentP** (*other*)

Tests equivalence

**Parameters** **other** –

**Return type** `bool`

**evalWordP** (*word*)

Verifies if a word is a member of the language represented by the regular expression.

**Parameters** **word** (*str*) – the word

**Return type** `bool`

**ewp** ()

Whether the empty word property holds for this regular expression's language.

**Return type** Boolean

**first** ()

**Return type** `set`

**last** ()

**Return type** `set`

**linearForm** ()

**Return type** `dic`

**mark** ()

Make all atoms maked (tag False) :rtype: reex.regexp

**marked** ()

Regular expression in which every alphabetic symbol is marked with its position.

The kind of regular expression returned is known, depending on the literary source, as marked, linear or restricted regular expression.

**Returns** linear regular expression

**Return type** *reex.regexp*

**See also:**

R. McNaughton and H. Yamada, Regular Expressions and State Graphs for Automata, IEEE Transactions on Electronic Computers, V.9 pp:39-47, 1960

..attention: mark and unmark do not preserve the alphabet, neither set the new alphabet

**nfaFollow** ()

NFA that accepts the regular expression's language, whose structure, equiand construction.

**Return type** *NFA*

**See also:**

Ilie & Yu (Follow Automata, 03)

**nfaFollowEpsilon** (*trim=True*)

Epsilon-NFA constructed with Ilie and Yu's method () that accepts the regular expression's language.

**Parameters** **trim** –

**Returns** NFA possibly with epsilon transitions

**Return type** NFAe

---

**Note:** The regular expression must be reduced

---

**See also:**

Ilie & Yu, Follow automta, Inf. Comp. ,v. 186 (1),140-162,2003

**nfaGlushkov** ()

Position or Glushkov automaton of the regular expression. Recursive method.

**Returns** NFA

**nfaNaiveFollow** ()

NFA that accepts the regular expression's language, and is equal in structure to the follow automaton.

**Return type** NFA

---

**Note:** Included for testing purposes.

---

**See also:**

Ilie & Yu (Follow Automata, 2003)

**nfaPD** ()

**NFA that accepts the regular expression's language**, and which is constructed from the expression's partial derivatives.

**Returns** partial derivatives [or equation] automaton

**Return type** NFA

**See also:**

V. M. Antimirov, Partial Derivatives of Regular Expressions and Finite Automaton Constructions .Theor. Comput. Sci.155(2): 291-319 (1996)

**nfaPDO** ()

**NFA that accepts the regular expression's language, and which is constructed from the expression's partial derivatives.**

---

**Note:** optimized version

---

**Returns** partial derivatives [or equation] automaton

**Return type** NFA

**nfaPSNF** ()

Position or Glushkov automaton of the regular expression constructed from the expression's star normal form.

**Returns** position automaton

**Return type** NFA

**nfaPosition** (*lstar=True*)

Position automaton of the regular expression.

**Parameters** **lstar** (*boolean*) – if not None followlists are computed disjunct

**Returns** position NFA

**Return type** *NFA*

**nfaPre** ()

Prefix NFA of a regular expression :return: prefix automaton :rtype: NFA .. seealso:: Maia et al, Prefix and Right-partial derivative automata, 11th CIE 2015, 258-267 LNCS 9136, 2015

**notEmptyW** ()

Witness of non emptyness

**Returns** word or None

**rpn** ()

RPN representation :rtype: str :return: printable RPN representation

**setOfSymbols** ()

**Return type** *set*

**setSigma** (*symbolSet=None, strict=False*)

Set the alphabet for a regular expression and all its nodes

**Parameters**

- **symbolSet** (*list or set of str*) – accepted symbols. If None, alphabet is unset.
- **strict** (*bool*) – if True checks if setOfSymbols is included in symbolSet

..attention: Normally this attribute is not defined in a regexp()

**starHeight** ()

Maximum level of nested regular expressions with a star operation applied.

For instance, starHeight(((a\*b)\*+b\*)\*) is 3.

**Return type** *integer*

**tailForm** ()

**Return type** *dict*

**toDFA** ()

DFA that accepts the regular expression's language

**toNFA** (*nfa\_method='nfaPD'*)

NFA that accepts the regular expression's language. :param nfa\_method:

**treeLength** ()

Number of nodes of the regular expression's syntactical tree.

**Return type** *integer*

**unionSigma** (*other*)

Returns the union of two alphabets

**Return type** *set*

**wordDerivative** (*word*)

**Derivative of the regular expression in relation to the given word**, which is represented by a list of symbols.

**Parameters** `word` – list of arbitrary symbols.

**Return type** regular expression

**See also:**

J. A. Brzozowski, Derivatives of Regular Expressions. J. ACM 11(4): 481-494 (1964)

## 5.3 Class `specialConstant`

**class** `reex.specialConstant` (*sigma=None*)

Bases: `reex.regexp`

Base class for Epsilon and EmptySet



**Parameters** `sigma` – alphabet

**static** `alphabeticLength()`

**Returns**

**derivative** (*sigma*)

**Parameters** `sigma` –

**Returns**

**distDerivative** (*sigma*)

**Parameters** `sigma` – an arbitrary symbol.

**Return type** regular expression

**static** `first` (*parent\_first=None*)

**Parameters** `parent_first` –

**Returns**

**followLists** (*lists=None*)

**Parameters** `lists` –

**Returns**

**followListsD** (*lists=None*)

**Parameters** `lists` –

**Returns**

**static followListsStar** (*lists=None*)

**Parameters** *lists* –

**Returns**

**last** (*parent\_last=None*)

**Parameters** *parent\_last* –

**Returns**

**linearForm** ()

**Returns**

**mark** ()

Make all atoms marked (tag False) :rtype: reex.regexp

**partialDerivativesC** (*sigma*)

**Parameters** *sigma* –

**Returns**

**reversal** ()

Reversal of regexp

**Return type** *reex.regexp*

**rpn** ()

RPN representation :rtype: str :return: printable RPN representation

**static setOfSymbols** ()

**Returns**

**support** (*side=True*)

**Returns**

**supportlast** (*side=True*)

**Returns**

**tailForm** ()

**Returns**

**unmark** ()

Conversion back to unmarked atoms :rtype: specialConstant

**unmarked** ()

The unmarked form of the regular expression. Each leaf in its syntactical tree becomes a regexp(), the epsilon() or the emptyset().

**Return type** (general) regular expression

**wordDerivative** (*word*)

**Parameters** *word* –

**Returns**

## 5.4 Class epsilon

**class** `reex.epsilon` (*sigma=None*)  
Bases: `reex.specialConstant`  
Class that represents the empty word.



Parameters **sigma** – alphabet

**static** `epsilonLength()`  
Return type `int`

**static** `epsilonP()`  
Return type `bool`

**static** `ewp()`  
Return type `bool`

**static** `measure` (*from\_parent=None*)  
Parameters **from\_parent** –  
Returns `measures`

`nfaThompson()`  
Return type `NFA`

**static** `partialDerivatives()`  
Returns

`partialDerivativesC()`  
Parameters **sigma** –  
Returns

`rpn()`  
Returns `str`

`snf` (*\_hollowdot=False*)  
Parameters **\_hollowdot** –  
Returns

## 5.5 Class emptyset

**class** `reex.emptyset` (*sigma=None*)  
Bases: `reex.specialConstant`



Class that represents the empty set.



Parameters **sigma** – alphabet

**static emptysetP** ()

Returns

**epsilonLength** ()

Returns

**epsilonP** ()

Returns

**ewp** ()

Returns

**static measure** (*from\_parent=None*)

Parameters **from\_parent** –

Returns

**partialDerivativesC** (\_)

Parameters **sigma** –

Returns

**rpn** ()

Returns

## 5.6 Class sigmaP

**class** `reex.sigmaP` (*sigma=None*)

Bases: `reex.specialConstant`

**Special regular expressions modulo associativity, commutativity, idempotence of disjunction and intersection;**  
 associativity of concatenation; identities  $\Sigma^*$  and  $\Sigma^+$ .

`sigmaP`: Class that represents the complement of the emptyset word ( $\Sigma^+$ )



Parameters **sigma** – alphabet

**derivative** (*sigma*)

Parameters **sigma** –

Returns

**ewp** ()

Returns

**linearForm** ()

Returns

**linearFormC** ()

Returns

**partialDerivatives** (*sigma*)

Parameters **sigma** –

Returns

**static partialDerivativesC** (\_)

Parameters \_ –

Returns

**support** (*side=True*)

Returns

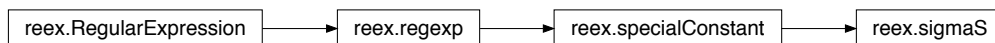
## 5.7 Class sigmaS

**class** `reex.sigmaS` (*sigma=None*)

Bases: `reex.specialConstant`

**Special regular expressions modulo associativity, commutativity, idempotence of disjunction and intersection; associativity of concatenation; identities  $\Sigma^*$  and  $\Sigma^+$ .**

`sigmaS`: Class that represents the complement of the emptyset set ( $\Sigma^*$ )



Parameters **sigma** – alphabet

**derivative** (*sigma*)

Parameters **sigma** –

Returns

**ewp** ()

Returns

**linearForm** ()

**Returns**

`linearFormC()`

**Returns**

`partialDerivatives(sigma)`

**Parameters** `sigma` –

**Returns**

`partialDerivativesC(sigma)`

**Parameters** `sigma` –

**Returns**

`support(side=True)`

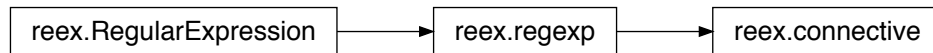
**Returns**

## 5.8 Class connective

**class** `reex.connective` (*arg1, arg2, sigma=None*)

Bases: `reex.regexp`

Base class for (binary) operations: concatenation, disjunction, etc



**alphabeticLength()**

Number of occurrences of alphabet symbols in the regular expression.

**Return type** integer

**Attention:** Doesn't include the empty word.

**epsilonLength()**

Number of occurrences of the empty word in the regular expression.

**Return type** integer

**first** (*parent\_first=None*)

**Return type** set

**last** (*parent\_last=None*)

**Return type** set

**linearForm()**

**Return type** dic

**mark** ()  
 Make all atoms maked (tag False) :rtype: reex.regexp

**rpn** ()  
 RPN representation :rtype: str :return: printable RPN representation

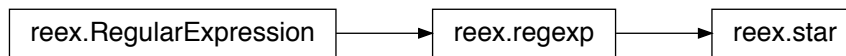
**setOfSymbols** ()  
**Return type** set

**starHeight** ()  
 Maximum level of nested regular expressions with a star operation applied.  
 For instance, starHeight(((a\*b)\*+b\*)\*) is 3.  
**Return type** integer

**treeLength** ()  
 Number of nodes of the regular expression's syntactical tree.  
**Return type** integer

## 5.9 Class star

**class** reex.star (*arg, sigma=None*)  
 Bases: *reex.regexp*  
 Class for iteration operation (aka Kleene star, or Kleene closure) on regular expressions.



**alphabeticLength** ()  
 Number of occurrences of alphabet symbols in the regular expression.  
**Return type** integer

**Attention:** Doesn't include the empty word.

**epsilonLength** ()  
 Number of occurrences of the empty word in the regular expression.  
**Return type** integer

**ewp** ()  
 Whether the empty word property holds for this regular expression's language.  
**Return type** Boolean

**first** (*parent\_first=None*)  
**Return type** set

**last** (*parent\_first=None*)

**Return type** *set*

**linearForm** ()

**Return type** *dic*

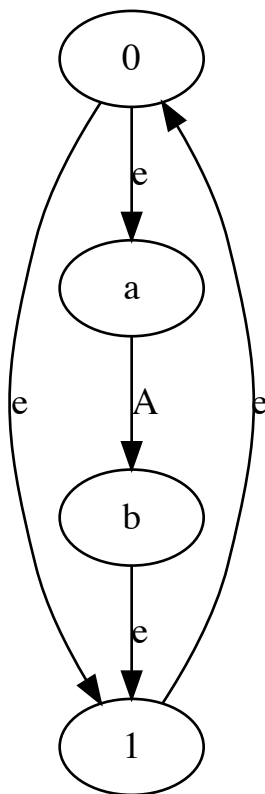
**mark** ()

Make all atoms maked (tag False) :rtype: reex.regexp

**nfaThompson** ()

Returns a NFA that accepts the RE.

**Return type** *NFA*



**reversal** ()

Reversal of regexp

**Return type** *reex.regexp*

**rpn** ()

RPN representation :rtype: str :return: printable RPN representation

**setOfSymbols** ()

**Return type** *set*

**starHeight** ()

Maximum level of nested regular expressions with a star operation applied.

For instance, `starHeight(((a*b)*+b*)*)` is 3.

**Return type** integer

**tailForm** ()

**Return type** dict

**treeLength** ()

Number of nodes of the regular expression's syntactical tree.

**Return type** integer

**unmark** ()

Conversion back to `regexp`

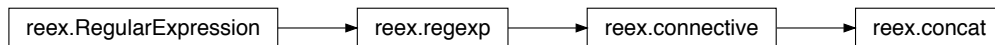
**Return type** *reex.star*

## 5.10 Class concat

**class** `reex.concat` (*arg1, arg2, sigma=None*)

Bases: *reex.connective*

Class for catenation operation on regular expressions.



**ewp** ()

Whether the empty word property holds for this regular expression's language.

**Return type** Boolean

**first** (*parent\_first=None*)

**Return type** set

**last** (*parent\_last=None*)

**Return type** set

**linearForm** ()

**Return type** dic

**mark** ()

Make all atoms maked (tag False) :rtype: `reex.regexp`

**reversal** ()

Reversal of `regexp`

**Return type** *reex.regexp*

**rpn** ()

**Return type** `str`

`tailForm()`

**Return type** `dict`

`unmark()`

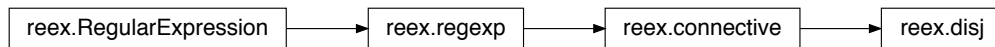
Conversion back to unmarked atoms :rtype: concat

## 5.11 Class `disj`

**class** `reex.disj` (*arg1*, *arg2*, *sigma=None*)

Bases: `reex.connective`

Class for disjunction operation on regular expressions.



`ewp()`

Whether the empty word property holds for this regular expression's language.

**Return type** `Boolean`

`first` (*parent\_first=None*)

**Return type** `set`

`last` (*parent\_last=None*)

**Return type** `set`

`linearForm()`

**Return type** `dic`

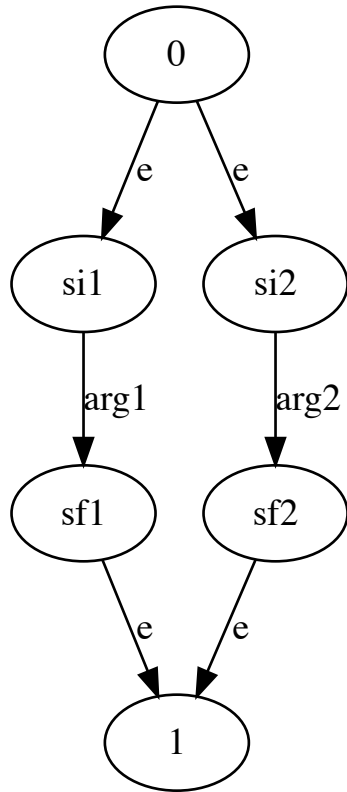
`mark()`

Conversion to marked atoms :rtype: disj

`nfaThompson()`

Returns an NFA (Thompson) that accepts the RE.

**Return type** `NFA`



**reversal ()**

Reversal of regexp

**Return type** *reex.regexp*

**rpn ()**

RPN representation :rtype: str :return: printable RPN representation

**tailForm ()**

**Return type** *dict*

**unmark ()**

Conversion back to unmarked atoms :rtype: disj

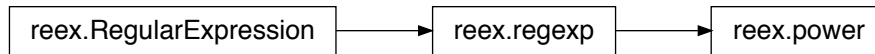
## 5.12 Class power

**class** *reex.power* (*arg, n=1, sigma=None*)

Bases: *reex.regexp*

Class for power operation on regular expressions.



**alphabeticLength()**

Number of occurrences of alphabet symbols in the regular expression.

**Return type** integer

**Attention:** Doesn't include the empty word.

**epsilonLength()**

Number of occurrences of the empty word in the regular expression.

**Return type** integer

**first()**

**Return type** set

**last()**

**Return type** set

**linearForm()**

**Return type** dic

**mark()**

Make all atoms maked (tag False) :rtype: reex.regexp

**reversal()**

Reversal of regexp

**Return type** *reex.regexp*

**rpn()**

RPN representation :rtype: str :return: printable RPN representation

**setOfSymbols()**

**Return type** set

**starHeight()**

Maximum level of nested regular expressions with a star operation applied.

For instance, starHeight(((a\*b)\*+b\*)\*) is 3.

**Return type** integer

**treeLength()**

Number of nodes of the regular expression's syntactical tree.

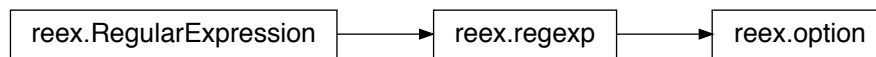
**Return type** integer

## 5.13 Class option

**class** `reex.option` (*arg*, *sigma=None*)

Bases: `reex.regexp`

Class for option operation on regular expressions.



**alphabeticLength** ()

Number of occurrences of alphabet symbols in the regular expression.

**Return type** integer

**Attention:** Doesn't include the empty word.

**epsilonLength** ()

Number of occurrences of the empty word in the regular expression.

**Return type** integer

**ewp** ()

Whether the empty word property holds for this regular expression's language.

**Return type** Boolean

**first** (*parent\_first=None*)

**Return type** set

**followListsStar** (*lists=None*)

to be fixed

**last** (*parent\_first=None*)

**Return type** set

**linearForm** ()

**Return type** dic

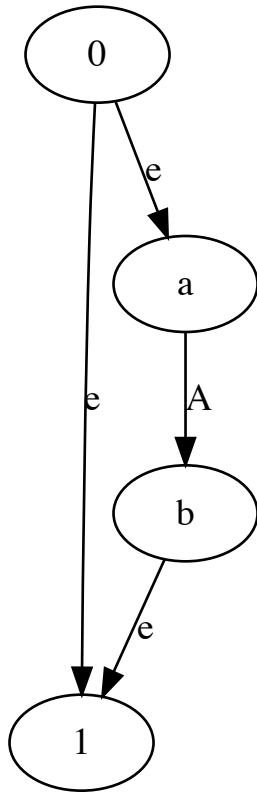
**mark** ()

Make all atoms maked (tag False) :rtype: reex.regexp

**nfaThompson** ()

Returns a NFA that accepts the RE.

**Return type** *NFA*



**reversal** ()

Reversal of regexp

**Return type** *reex.regexp*

**rpn** ()

RPN representation :rtype: str :return: printable RPN representation

**setOfSymbols** ()

**Return type** *set*

**starHeight** ()

Maximum level of nested regular expressions with a star operation applied.

For instance, `starHeight(((a*b)*+b*)*)` is 3.

**Return type** *integer*

**treeLength** ()

Number of nodes of the regular expression's syntactical tree.

**Return type** *integer*

## 5.14 Class conj (intersection)

**class** `reex.conj` (*arg1, arg2, sigma=None*)

Bases: `reex.connective`

Intersection operation of regexps

**ewp** ()

Whether the empty word property holds for this regular expression's language.

**Return type** Boolean

**linearForm** ()

**Return type** dic

**mark** ()

Make all atoms maked (tag False) :rtype: reex.regexp

**rpn** ()

RPN representation :rtype: str :return: printable RPN representation

**support** (*side=True*)

## 5.15 Class shuffle

**class** `reex.shuffle` (*arg1, arg2, sigma=None*)

Bases: `reex.connective`

Shuffle operation of regexps

**ewp** ()

Whether the empty word property holds for this regular expression's language.

**Return type** Boolean

**first** (*parent\_list=None*)

**Parameters** `parent_list` –

**Returns**

**followListsD** (*lists=None*)

in progress

**linearForm** ()

**Return type** dic

**mark** ()

Make all atoms maked (tag False) :rtype: reex.regexp

**rpn** ()

RPN representation :rtype: str :return: printable RPN representation

**support** (*side=True*)

**supportlast** (*side=True*)

## 5.16 Class atom

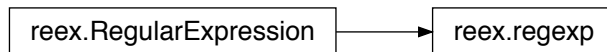
**class** `reex.atom` (*val*, *sigma=None*)

Bases: `reex.regexp`

Simple atom (symbol)

### Variables

- *Sigma* – alphabet set of strings
- **val** – the actual symbol



Constructor of a regular expression symbol.

**Parameters** **val** – the actual symbol

**PD** ()

Closure of partial derivatives of the regular expression in relation to all words.

**Returns** set of regular expressions

**Return type** `set`

**See also:**

Antimirov, 95

**static alphabeticLength** ()

Number of occurrences of alphabet symbols in the regular expression.

**Return type** `integer`

**Attention:** Doesn't include the empty word.

**derivative** (*sigma*)

Derivative of the regular expression in relation to the given symbol.

**Parameters** **sigma** – an arbitrary symbol.

**Return type** `regular expression`

---

**Note:** whether the symbols belong to the expression's alphabet goes unchecked. The given symbol will be matched against the string representation of the regular expression's symbol.

---

**See also:**

J. A. Brzozowski, Derivatives of Regular Expressions. J. ACM 11(4): 481-494 (1964)

**static** `epsilonLength()`

Number of occurrences of the empty word in the regular expression.

**Return type** integer

**first** (*parent\_first=None*)

List of possible symbols matching the first symbol of a string in the language of the regular expression.

**Parameters** `parent_first` –

**Returns** list of symbols

**followLists** (*lists=None*)

Map of each symbol's follow list in the regular expression.

**Parameters** `lists` –

**Returns** map of symbols' follow lists

**Return type** {symbol: list of symbols}

**Attention:** For `first()` and `last()` return lists, the follow list for certain symbols might have repetitions in the case of follow maps calculated from star operators. The union of `last()`, `first()` and `follow()` sets are always disjoint when the regular expression is in star normal form ( Bruggemann-Klein, 92), therefore FAdo implements them as lists. You should order exclusively, or take a set from a list in order to resolve repetitions.

**followListsD** (*lists=None*)

Map of each symbol's follow list in the regular expression.

**Parameters** `lists` –

**Returns** map of symbols' follow lists

**Return type** {symbol: list of symbols}

**Attention:** For `first()` and `last()` return lists, the follow list for certain symbols might have repetitions in the case of follow maps calculated from star operators. The union of `last()`, `first()` and `follow()` sets are always disjoint

**See also:**

Sabine Broda, António Machiavelo, Nelma Moreira, and Rogério Reis. On the average size of glushkov and partial derivative automata. International Journal of Foundations of Computer Science, 23(5):969-984, 2012.

**followListsStar** (*lists=None*)

Map of each symbol's follow list in the regular expression under a star.

**Parameters** `lists` –

**Returns** map of symbols' follow lists

**Return type** {symbol: list of symbols}

**last** (*parent\_last=None*)

List of possible symbols matching the last symbol of a string in the language of the regular expression.

**Parameters** `parent_last` –

**Returns** list of symbols

**Return type** `list`

**linearForm()**

Linear form of the regular expression, as a mapping from heads to sets of tails, so that each pair (head, tail) is a monomial in the set of linear forms.

**Returns** dictionary mapping heads to sets of tails

**Return type** {symbol: set([regular expressions])}

**See also:**

Antimirov, 95

**linearFormC()**

**Returns**

**linearP()**

Whether the regular expression is linear; i.e., the occurrence of a symbol in the expression is unique.

**Return type** `boolean`

**mark()**

**Return type** `m_atom`

**static measure** (*from\_parent=None*)

A list with four measures for regular expressions.

**Parameters** `from_parent` –

**Return type** `[int,int,int,int]`

[`alphabeticLength`, `treeLength`, `epsilonLength`, `starHeight`]

1. `alphabeticLength`: number of occurrences of symbols of the alphabet;
2. `treeLength`: number of functors in the regular expression, including constants.
3. `epsilonLength`: number of occurrences of the empty word.
4. `starHeight`: highest level of nested Kleene stars, starting at one for one star occurrence.
5. `disjLength`: number of occurrences of the disj operator
6. `concatLength`: number of occurrences of the concat operator
7. `starLength`: number of occurrences of the star operator
8. `conjLength`: number of occurrences of the conj operator
9. `starLength`: number of occurrences of the shuffle operator

**Attention:** Methods for each of the measures are implemented independently. This is the most effective for obtaining more than one measure.

**nfaThompson()**

Epsilon-NFA constructed with Thompson's method that accepts the regular expression's language.

**Return type** *NFA*

**See also:**

K. Thompson. Regular Expression Search Algorithm. CACM 11(6), 419-422 (1968)

**partialDerivatives** (*sigma*)

Set of partial derivatives of the regular expression in relation to given symbol.

**Parameters** **sigma** – symbol in relation to which the derivative will be calculated.

**Returns** set of regular expressions

**See also:**

Antimirov, 95

**partialDerivativesC** (*sigma*)

**Parameters** **sigma** –

**Returns**

**reduced** (*hasEpsilon=False*)

Equivalent regular expression with the following cases simplified:

1.  $\text{Epsilon.RE} = \text{RE.Epsilon} = \text{RE}$
2.  $\text{EmptySet.RE} = \text{RE.EmptySet} = \text{EmptySet}$
3.  $\text{EmptySet} + \text{RE} = \text{RE} + \text{EmptySet} = \text{RE}$
4.  $\text{Epsilon} + \text{RE} = \text{RE} + \text{Epsilon} = \text{RE}$ , where  $\text{Epsilon}$  is in  $L(\text{RE})$
5.  $\text{RE}^{**} = \text{RE}^*$
6.  $\text{EmptySet}^* = \text{Epsilon}^* = \text{Epsilon}$
7.  $\text{Epsilon:RE} = \text{RE:Epsilon} = \text{RE}$

**Parameters** **hasEpsilon** – used internally to indicate that the language of which this term is a subterm has the empty word.

**Returns** regular expression

**Attention:** Returned structure isn't strictly a duplicate. Use `__copy__()` for that purpose.

**reversal** ()

Reversal of regexp

**Return type** *reex.regexp*

**rpn** ()

RPN representation :return: printable RPN representation

**setOfSymbols** ()

Set of symbols that occur in a regular expression..

**Returns** set of symbols

**Return type** set of symbols

**snf** (*hollowdot=False*)

Star Normal Form (SNF) of the regular expression.

**Parameters** **hollowdot** –

**Returns** regular expression in star normal form



**static starHeight ()**

Maximum level of nested regular expressions with a star operation applied.

For instance, `starHeight(((a*b)*+b*)*)` is 3.

**Return type** integer

**stringLength ()**

Length of the string representation of the regular expression.

**Return type** integer

**support (side=True)**

Support of a regular expression. :param side: if True concatenation of a set on the left if False on the right (prefix support) :return: set of regular expressions :rtype: set

**See also:**

Champarnaud, J.M., Ziadi, D.: From Mirkin's prebases to Antimirov's word partial derivative. *Fundam. Inform.* 45(3), 195-205 (2001)

**See also:**

Maia et al, Prefix and Right-partial derivative automata, 11th CIE 2015, 258-267 LNCS 9136, 2015

**supportlast (side=True)**

Subset of support such that elements have ewp

**static syntacticLength ()**

Number of nodes of the regular expression's syntactical tree (sets).

**Return type** integer

**tailForm ()**

**Returns**

**static treeLength ()**

Number of nodes of the regular expression's syntactical tree.

**Return type** integer

**unmarked ()**

The unmarked form of the regular expression. Each leaf in its syntactical tree becomes a `regexp()`, the `epsilon()` or the `emptyset()`.

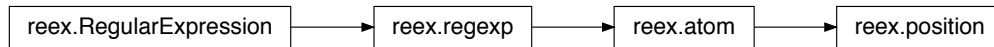
**Return type** (general) regular expression

## 5.17 Class position

**class** `reex.position` (*val, sigma=None*)

Bases: `reex.atom`

Class for marked regular expression symbols.



Constructor of a regular expression symbol.

**Parameters** `val` – the actual symbol

**setOfSymbols** ()

Set of symbols that occur in a regular expression..

**Returns** set of symbols

**Return type** set of symbols

**unmarked** ()

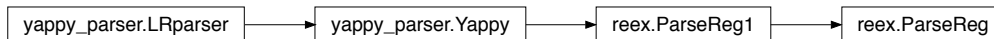
The unmarked form of the regular expression. Each leaf in its syntactical tree becomes a `regexp()`, the `epsilon()` or the `emptyset()`.

**Return type** (general) regular expression

## 5.18 Class ParseReg

**class** `reex.ParseReg` (*no\_table=1, table='.tableambreg'*)

Bases: `reex.ParseReg1`



A parser for regular expressions with ambiguous rules: not working

## 5.19 Class sconnective (special connective)

**class** `reex.sconnective` (*arg, sigma=None*)

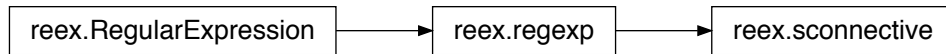
Bases: `reex.regexp`

**Special regular expressions modulo associativity, commutativity, idempotence of disjunction and intersection;**

**associativity of concatenation; identities  $\Sigma^*$  and  $\Sigma^+$ . Connectives are:** `sdisj`: disjunction

`sconj`: intersection `sconcat`: concatenation

For parsing use `str2sre`



**alphabeticLength()**

Returns

**epsilonLength()**

Returns

**first()**

Return type *set*

**last()**

Return type *set*

**linearForm()**

Return type *dic*

**mark()**

Make all atoms maked (tag False) :rtype: reex.regexp

**rpn()**

RPN representation :rtype: str :return: printable RPN representation

**setOfSymbols()**

Returns

**starHeight()**

Maximum level of nested regular expressions with a star operation applied.

For instance, starHeight(((a\*b)\*+b\*)\*) is 3.

Return type *integer*

**syntacticLength()**

Returns

**treeLength()**

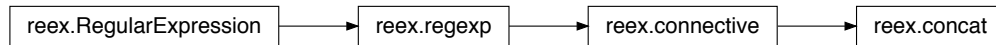
Returns

## 5.20 Class sconcat

**class** reex.sconcat (*arg, sigma=None*)

Bases: *reex.sconnective*

Class that represents the concatenation operation.



**derivative** (*sigma*)

Parameters **sigma** –

Returns

**ewp** ()

Returns

**head** ()

Returns

**head\_rev** ()

Returns

**linearForm** ()

Returns

**linearFormC** ()

Returns

**partialDerivatives** (*sigma*)

Parameters **sigma** –

Returns

**partialDerivativesC** (*sigma*)

Parameters **sigma** –

Returns

**support** (*side=True*)

Returns

**tail** ()

Returns

**tail\_rev** ()

Returns

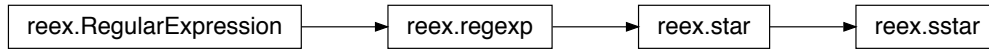
## 5.21 Class **sstar**

**class** `reex.sstar` (*arg, sigma=None*)

Bases: `reex.star`

**Special regular expressions modulo associativity, commutativity, idempotence of disjunction and intersection;**  
 associativity of concatenation; identities  $\Sigma^*$  and  $\Sigma^+$ .

sstar: Class that represents Kleene star



**derivative** (*sigma*)

**Parameters** *sigma* –

**Returns**

**linearForm** ()

**Returns**

**partialDerivatives** (*sigma*)

**Parameters** *sigma* –

**Returns**

**partialDerivativesC** (*sigma*)

**Parameters** *sigma* –

**Returns**

**support** (*side=True*)

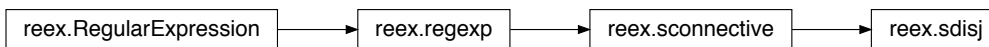
**Returns**

## 5.22 Class sdisj

**class** `reex.sdisj` (*arg*, *sigma=None*)

Bases: `reex.sconnective`

Class that represents the disjunction operation for special regular expressions.



**cross** (*ri*, *s*, *lists*)

**Returns**

**derivative** (*sigma*)

**Parameters** `sigma` –

**Returns**

`ewp()`

**Returns**

`first()`

**Returns**

`followLists (lists=None)`

**Parameters** `lists` –

**Returns**

`followListsStar (lists=None)`

**Parameters** `lists` –

**Returns**

`last()`

**Returns**

`linearForm()`

**Returns**

`linearFormC()`

**Returns**

`partialDerivatives (sigma)`

**Parameters** `sigma` –

**Returns**

`partialDerivativesC (sigma)`

**Parameters** `sigma` –

**Returns**

`support (side=True)`

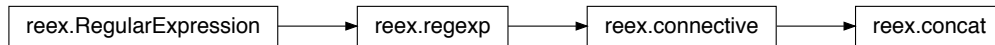
**Returns**

## 5.23 Class `sconj`

**class** `reex.sconj (arg, sigma=None)`

Bases: `reex.sconnective`

Class that represents the conjunction operation.



**derivative** (*sigma*)

Parameters **sigma** –

Returns

**ewp** ()

Returns

**linearForm** ()

Returns

**partialDerivatives** (*sigma*)

Parameters **sigma** –

Returns

**partialDerivativesC** (*sigma*)

Parameters **sigma** –

Returns

**support** (*side=True*)

Returns

## 5.24 Class snot

**class** `reex.snot` (*arg*, *sigma=set([])*)

Bases: `reex.regexp`

**Special regular expressions modulo associativity, commutativity, idempotence of disjunction and intersection; associativity of concatenation; identities  $\Sigma^*$  and  $\Sigma^+$ . snot: negation**



**alphabeticLength** ()

Returns

**derivative** (*sigma*)

:param *sigma* :return:

**epsilonLength()**

**Returns**

**ewp()**

**Returns**

**first()**

**Return type** *set*

**last()**

**Return type** *set*

**linearForm()**

**Returns**

**linearFormC()**

**Returns**

**mark()**

Make all atoms maked (tag False) :rtype: reex.regexp

**partialDerivatives** (*sigma*)

**Parameters** *sigma* –

**Returns**

**partialDerivativesC** (*sigma*)

**Parameters** *sigma* –

**Returns**

**rpn()**

RPN representation :rtype: str :return: printable RPN representation

**setOfSymbols()**

**Returns**

**starHeight()**

Maximum level of nested regular expressions with a star operation applied.

For instance, starHeight(((a\*b)\*+b\*)) is 3.

**Return type** integer

**support** (*side=True*)

**Returns**

**syntacticLength()**

**Returns**

**treeLength()**

**Returns**



## 5.25 Functions

`reex.str2regexp` (*s*, *parser*=<class 'reex.ParseReg1'>, *no\_table*=1, *sigma*=None, *strict*=False)

Reads a regexp from string.

### Parameters

- **s** (*string*) – the string representation of the regular expression
- **parser** (*Yappy*) – a parser generator for regexps
- **no\_table** (*integer*) – if 0 table is created
- **sigma** (*list or set of symbols*) – alphabet of the regular expression
- **strict** (*boolean*) – if True tests if the symbols of the regular expression are included in sigma

**Return type** *reex.regexp*

`reex.str2sre` (*s*, *parser*=<class 'reex.ParseS'>, *no\_table*=1, *sigma*=None, *strict*=False)

Reads a sre from string. Arguments as `str2regexp`.

**Return type** *regexp*

`reex.rpn2regexp` (*s*, *sigma*=None, *strict*=False)

Reads a (simple) regexp from a RPN representation

```
R ::= .RR | +RR | \*R | L | @
L ::= [a-z] | [A-Z]
```

**Parameters** **s** (*string*) – RPN representation

**Return type** *reex.regexp*

---

**Note:** This method uses python stack... thus depth limitations apply

---



## MODULE: TRANSDUCERS (TRANSDUCERS)

### Finite Tranducer Support

Transducer manipulation.

New in version 1.0.

## 6.1 Class Transducer

**class** `transducers.Transducer`

Bases: `fa.NFA`

Base class for Transducers



**setOutput** (*listOfSymbols*)

Set Output

**Parameters** `listOfSymbols` (*set/list*) – output symbols

**succinctTransitions** ()

Collects the transition information in a concat way suitable for graphical representation. `:rtype:` list of tuples

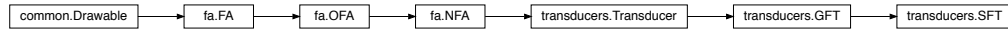
## 6.2 Class SFT (Standard Form Transducers)

**class** `transducers.SFT`

Bases: `transducers.GFT`

Standard Form Tranducer

**Variables** `Output` (*set*) – output alphabet



**addEpsilonLoops ()**

Add a loop transition with epsilon input and output to every state in the transducer.

**addTransition (stsrc, symi, symo, sti2)**

Adds a new transition

**Parameters**

- **stsrc** (*int*) – state index of departure
- **sti2** (*int*) – state index of arrival
- **symi** (*str*) – symbol consumed
- **symo** (*str*) – symbol output

**addTransitionProductQ (src, dest, ddest, sym, out, futQ, pastQ)**

Add transition to the new transducer instance.

Version for the optimized product

**Parameters**

- **src** – source state
- **dest** – destination state
- **ddest** – destination as tuple
- **sym** – symbol
- **out** – output
- **futQ** (*set*) – queue for later
- **pastQ** (*set*) – past queue

**addTransitionQ (src, dest, sym, out, futQ, pastQ)**

Add transition to the new transducer instance.

**Parameters**

- **src** – source state
- **dest** – destination state
- **sym** – symbol
- **out** – output
- **futQ** (*set*) – queue for later
- **pastQ** (*set*) – past queue

**composition (other)**

Composition operation of a transducer with a transducer.

**Parameters other** (SFT) – the second transducer

**Return type** *SFT*

**concat** (*other*)

Concatenation of transducers

**Parameters** **other** (*SFT*) – the other operand

**Return type** *SFT*

**delTransition** (*sti1, sym, symo, sti2, \_no\_check=False*)

Remove a transition if existing and perform cleanup on the transition function's internal data structure.

**Parameters**

- **symo** – symbol output
- **sti1** (*int*) – state index of departure
- **sti2** (*int*) – state index of arrival
- **sym** – symbol consumed
- **\_no\_check** (*bool*) – dismiss secure code

**deleteState** (*sti*)

Remove given state and transitions related with that state.

**Parameters** **sti** (*int*) – index of the state to be removed

**Raises** **DFAstateUnknown** – if state index does not exist

**deleteStates** (*lstates*)

Delete given iterable collection of states from the automaton.

**Parameters** **lstates** (*set/list*) – collection of int representing states

**dup** ()

Duplicate of itself :rtype: *SFT*

**Attention:** only duplicates the initially connected component

**emptyP** ()

Tests if the relation realized the empty transducer

**Return type** *bool*

**epsilonOutP** ()

Tests if epsilon occurs in transition outputs

**Return type** *bool*

**epsilonP** ()

Test whether this transducer has input epsilon-transitions

**Return type** *bool*

**evalWordP** (*wp*)

Tests whether the transducer returns the second word using the first one as input

**Parameters** **wp** (*tuple*) – pair of words

**Return type** *bool*

**evalWordSlowP** (*wp*)

Tests whether the transducer returns the second word using the first one as input

Note: original :param tuple wp: pair of words :rtype: bool

**functionalP** ()

Tests if a transducer is functional using Allauzer & Mohri and Béal&Carton&Prieur&Sakarovitch algorithms.

**Return type** *bool*

**See also:**

Cyril Allauzer and Mehryar Mohri, Journal of Automata Languages and Combinatorics, Efficient Algorithms for Testing the Twins Property, 8(2): 117-144, 2003.

**See also:**

M.P. Béal, O. Carton, C. Prieur and J. Sakarovitch. Squaring transducers: An efficient procedure for deciding functionality and sequentiality. Theoret. Computer Science 292:1 (2003), 45-63.

---

**Note:** This is implemented using `nonFunctionalW()`

---

**inIntersection** (*other*)

Conjunction of transducer and automata: X & Y.

---

**Note:** This is a fast version of the method that does not produce meaningful state names.

---

---

**Note:** The resulting transducer is not trim.

---

**Parameters** *other* (*DFA/NFA*) – the automata needs to be operated.

**Return type** *SFT*

**inIntersectionSlow** (*other*)

Conjunction of transducer and automata: X & Y.

---

**Note:** This is the slow version of the method that keeps meaningful names of states.

---

**Parameters** *other* (*DFA/NFA*) – the automata needs to be operated.

**Return type** *SFT*

**inverse** ()

Switch the input label with the output label.

No initial or final state changed.

**Returns** Transducer with transitions switched.

**Return type** *SFT*

**nonEmptyW** ()

Witness of non emptiness

**Returns** pair (in-word, out-word)

**Return type** tuple

**nonFunctionalW** ()

Returns a witness of non functionality (if is that the case) or a None filled triple

**Returns** witness

**Return type** tuple

**outIntersection** (*other*)

Conjunction of transducer and automaton: X & Y using output intersect operation.

**Parameters** *other* (*DFA/NFA*) – the automaton used as a filter of the output

**Return type** *SFT*

**outIntersectionDerived** (*other*)

Naive version of outIntersection

**Parameters** *other* (*DFA/NFA*) – the automaton used as a filter of the output

**Return type** *SFT*

**outputS** (*s*)

Output label coming out of the state *i*

**Parameters** *s* (*int*) – index state

**Return type** set

**productInput** (*other*)

Returns a transducer (skeleton) resulting from the execution of the transducer with the automaton as filter on the input.

---

**Note:** This version does not use stateIndex() with the price of generating some unreachable sates

---

**Parameters** *other* (*NFA*) – the automaton used as filter

**Return type** *SFT*

Changed in version 1.3.3.

**productInputSlow** (*other*)

Returns a transducer (skeleton) resulting from the execution of the transducer with the automaton as filter on the input.

---

**Note:** This is the slow version of the method that keeps meaningful names of states.

---

**Parameters** *other* (*NFA*) – the automaton used as filter

**Return type** *SFT*

**reversal** ()

Returns a transducer that recognizes the reversal of the relation.

**Returns** Transducer recognizing reversal language

**Return type** *SFT*

**runOnNFA** (*nfa*)

Result of applying a transducer to an automaton

**Parameters** **nfa** (*DFA/NFA*) – input language to transducer

**Returns** resulting language

**Return type** *NFA*

**runOnWord** (*word*)

Returns the automaton accepting the output of the transducer on the input word

**Parameters** **word** – the word

**Return type** *NFA*

**setInitial** (*sts*)

Sets the initial state of a Transducer

**Parameters** **sts** (*list*) – list of states

**square** ()

Conjunction of transducer with itself

**Return type** *NFA*

**square\_fv** ()

Conjunction of transducer with itself (Fast Version)

**Return type** *NFA*

**star** (*flag=False*)

Kleene star

**Parameters** **flag** (*bool*) – plus instead of star

**Returns** the resulting Transducer

**Return type** *SFT*

**toInNFA** ()

Delete the output labels in the transducer. Translate it into an NFA

**Return type** *NFA*

**toNFT** ()

Transformation into Normal Form Transducer

**Return type** *NFT*

**toOutNFA** ()

Returns the result of considering the output symbols of the transducer as input symbols of a NFA (ignoring the input symbol, thus)

**Returns** the NFA

**Return type** *NFA*

**toSFT** ()

Pacifying rule

**Return type** *SFT*

**trim** ()

Remove states that do not lead to a final state, or, inclusively, that can't be reached from the initial state. Only useful states remain.



**Attention:** in place transformation

**union** (*other*)

Union of the two transducers

**Parameters** **other** (*SFT*) – the other operand

**Return type** *SFT*

## 6.3 Functions



## MODULE: FINITE LANGUAGES (FL)

Finite languages and related automata manipulation

Finite languages manipulation

### 7.1 Class FL (Finite Language)

**class** fl.**FL** (*wordsList=None, Sigma=None*)

Bases: `object`

Finite Language Class

#### Variables

- **Words** – the elements of the language
- ***Sigma*** – the alphabet

**MADFA** ()

Generates the minimal acyclical DFA using specialized algorithm

New in version 1.3.3.

#### See also:

Incremental Construction of Minimal Acyclic Finite-State Automata, J.Daciuk, S.Mihov, B.Watson and R.E.Watson

**Return type** *ADFA*

**addWord** (*word*)

Adds a word to a FL :type word: Word :rtype: FL

**addWords** (*wList*)

Adds a list of words to a FL

**Parameters** **wList** (*list*) – words to add

**diff** (*other*)

Difference of FL: a - b

**Parameters** **other** (FL) – right hand operand

**Return type** *FL*

**Raises** **FAdoGeneralError** – if both arguments are not FL

**filter** (*automata*)

Separates a language in two other using a DFA of NFA as a filter

**Parameters** **automata** (*DFA/NFA*) – the automata to be used as a filter

**Returns** the accepted/unaccepted pair of languages

**Return type** tuple of FL

**intersection** (*other*)

Intersection of FL: a & b

**Parameters** **other** (FL) – right hand operand

**Raises** **FAdoGeneralError** – if both arguments are not FL

**multiLineAutomaton** ()

Generates the trivial linear ANFA equivalent to this language

**Return type** *ANFA*

**setSigma** (*Sigma, Strict=False*)

Sets the alphabet of a FL

**Parameters**

- **Sigma** (*set*) – alphabet
- **Strict** (*bool*) – behaviour

**Attention:** Unless Strict flag is set to True, alphabet can only be enlarged. The resulting alphabet is in fact the union of the former alphabet with the new one. If flag is set to True, the alphabet is simply replaced.

**suffixClosedP** ()

Tests if a language is suffix closed

**Return type** *bool*

**toDFA** ()

Generates a DFA recognizing the language

**Return type** *ADFA*

New in version 1.2.

**toNFA** ()

Generates a NFA recognizing the language

**Return type** *ANFA*

New in version 1.2.

**trieFA** ()

Generates the trie automaton that recognises this language

**Returns** the trie automaton

**Return type** *ADFA*

**union** (*other*)

union of FL: a | b

**Parameters** **other** (FL) – right hand operand

**Return type** *FL*

**Raises** `FAdoGeneralError` – if both arguments are not FL

## 7.2 Class DFCA (Deterministic Finite Cover Automata)

**class** `fl.DFCA`

Bases: `fa.DFA`

Deterministic Cover Automata class



**length**

size of the longest word :rtype: int

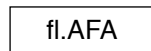
**Type** return

## 7.3 Class AFA (Acyclic Finite Automata)

**class** `fl.AFA`

Bases: `object`

Base class for Acyclic Finite Automata




---

**Note:** This is just a container for some common methods. **Not to be used directly!!**

---

**addState** (`_`)

**Return type** int

**directRank** (`()`)

Compute rank function

**Returns** ranf map

**Return type** dict

**ensureDead ()**

Ensures that a state is defined as dead

**evalRank ()**

Evaluates the rank map of a automaton

**Returns** pair of sets of states by rank map, reverse delta accessibility map

**Return type** tuple

**getLeaves ()**

The set of leaves, i.e. final states for last symbols of language words

**Returns** set of leaves

**Return type** set

**ordered ()**

Orders states names in its topological order

**Returns** ordered list of state indexes

**Return type** list of int

---

**Note:** one could use the FA.toposort() method, but special care must be taken with the dead state for the algorithms related with cover automata.

---

**setDeadState (sti)**

Identifies the dead state

**Parameters** **sti** (*int*) – index of the dead state

**Attention:** nothing is done to ensure that the state given is legitimate

---

**Note:** without dead state identified, most of the methods for acyclic automata can not be applied

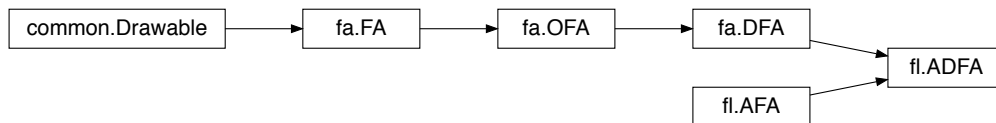
---

## 7.4 Class ADFA (Acyclic Deterministic Finite Automata)

**class fl.ADFA**

Bases: *fa.DFA*, *fl.AFA*

Acyclic Deterministic Finite Automata class



Changed in version 1.3.3.

**addSuffix** (*st*, *w*)

Adds a suffix starting in *st*

**Parameters**

- **st** (*int*) – state
- **w** (*Word*) – suffix

New in version 1.3.3.

**Attention:** in place transformation

**complete** (*dead=None*)

Make the ADFA complete

**Parameters** **dead** (*int*) – a state to be identified as dead state if one was not identified yet

**Return type** *ADFA*

**Attention:** The object is modified in place

Changed in version 1.3.3.

**diss** ()

Evaluates the dissimilarity language

**Return type** *FL*

New in version 1.2.1.

**dissMin** (*witnesses=None*)

Evaluates the minimal dissimilarity language :param dict witnesses: optional witness dictionary :rtype: FL

New in version 1.2.1.

**dup** ()

Duplicate the basic structure into a new ADFA. Basically a copy.deepcopy.

**Return type** *ADFA*

**forceToDFA** ()

Conversion to DFA

**Return type** *DFA*

**forceToDFCA** ()

Conversion to DFCA

**Return type** *DFA*

**level** ()

Computes the level for each state

**Returns** levels of states

**Return type** *dict*

New in version 0.9.8.

**minDFCA** ()

Generates a minimal deterministic cover automata from a DFA

**Return type** *DFCA*

New in version 0.9.8.

**See also:**

Cezar Campeanu, Andrei Păun, and Sheng Yu, An efficient algorithm for constructing minimal cover automata for finite languages, IJFCS

**minReversible** ()

Returns the minimal reversible equivalent automaton

**Return type** *ADFA*

**minimal** ()

Finds the minimal equivalent ADFA

**See also:**

[TCS 92 pp 181-189] Minimisation of acyclic deterministic automata in linear time, Dominique Revuz

Changed in version 1.3.3.

**Returns** the minimal equivalent ADFA

**Return type** *ADFA*

**minimalP** (*method=None*)

Tests if the DFA is minimal

**Parameters** **method** – minimization algorithm (here void)

**Return type** *bool*

Changed in version 1.3.3.

**possibleToReverse** ()

Tests if language is reversible

New in version 1.3.3.

**statePairEquiv** (*s1, s2*)

Tests if two states of a ADFA are equivalent

**Parameters**

- **s1** (*int*) – state1
- **s2** (*int*) – state2

**Return type** *bool*

New in version 1.3.3.

**toANFA** ()

Converts the ADFA in a equivalent ANFA

**Return type** *ANFA*

**toNFA** ()

Converts the ADFA in a equivalent NFA

**Return type** *ANFA*

New in version 1.2.



**trim()**

Remove states that do not lead to a final state, or, inclusively, that can't be reached from the initial state. Only useful states remain.

**Attention:** in place transformation

**wordGenerator()**

Creates a random word generator

**Returns** the random word generator

**Return type** *RndWGen*

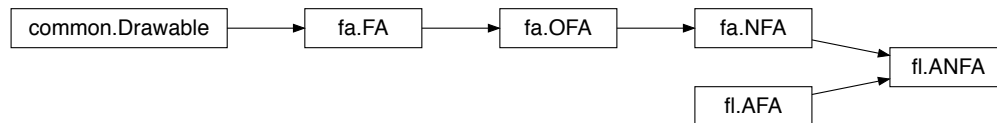
New in version 1.2.

## 7.5 Class ANFA (Acyclic Non-deterministic Finite Automata)

**class** `fl.ANFA`

Bases: `fa.NFA`, `fl.AFA`

Acyclic Nondeterministic Finite Automata class

**mergeInitial()**

Merge initial states

**Attention:** object is modified in place

**mergeLeaves()**

Merge leaves

**Attention:** object is modified in place

**mergeStates(s1, s2)**

Merge state `s2` into state `s1`

**Parameters**

- `s1` (*int*) – state
- `s2` (*int*) – state

---

**Note:** no attempt is made to check if the merging preserves the language of the automaton

---

**Attention:** the object is modified in place

**moveFinal** (*st*, *stf*)

Unsets a set as final transferring transition to another final :param int st: the state to be ‘moved’ :param int stf: the destination final state

---

**Note:** stf must be a ‘last’ final state, i.e., must have no out transitions to anywhere but to a possible dead state

---

**Attention:** the object is modified in place

## 7.6 Class RndWGen (Random Word Generator)

**class** fl.RndWGen (*aut*)

Bases: `object`

Word random generator class

New in version 1.2.

**Parameters** **aut** (ADFA) – automata recognizing the language

**next** ()

Next word

**Returns** a new random word

## 7.7 Functions

fl.**sigmaInitialSegment** (*Sigma*, *l*, *exact=False*)

Generates the ADFA recognizing  $\Sigma^i$  for  $i \leq l$  :param set Sigma: the alphabet :param int l: length :param bool exact: only the words with exactly that length? :returns: the automaton :rtype: ADFA

fl.**genRndTrieBalanced** (*maxL*, *Sigma*, *safe=True*)

Generates a random trie automaton for a binary language of balanced words of a given length for max word :param int maxL: length of the max word :param set Sigma: alphabet to be used :param bool safe: should a word of size maxL be present in every language? :return: the generated trie automaton :rtype: ADFA

fl.**genRndTrieUnbalanced** (*maxL*, *Sigma*, *ratio*, *safe=True*)

Generates a random trie automaton for a binary language of balanced words of a given length for max word

**Parameters**

- **maxL** (*int*) – length of the max word
- **Sigma** (*set*) – alphabet to be used
- **ratio** (*int*) – the ratio of the unbalance

- **safe** (*bool*) – should a word of size `maxl` be present in every language?

**Returns** the generated trie automaton

**Return type** *ADFA*

f1. **genRandomTrie** (*maxL, Sigma, safe=True*)

Generates a random trie automaton for a finite language with a given length for max word :param int maxL: length of the max word :param set Sigma: alphabet to be used :param bool safe: should a word of size `maxl` be present in every language? :return: the generated trie automaton :rtype: *ADFA*

f1. **genRndTriePrefix** (*maxL, Sigma, ClosedP=False, safe=True*)

Generates a random trie automaton for a finite (either prefix free or prefix closed) language with a given length for max word :param int maxL: length of the max word :param set Sigma: alphabet to be used :param bool ClosedP: should it be a prefix closed language? :param bool safe: should a word of size `maxl` be present in every language? :return: the generated trie automaton :rtype: *ADFA*

f1. **DFAtoADFA** (*aut*)

Transforms an acyclic DFA into a *ADFA*

**Parameters** **aut** (*DFA*) – the automaton to be transformed

**Raises** **notAcyclic** – if the DFA is not acyclic

**Returns** the converted automaton

**Return type** *ADFA*

f1. **stringToADFA** (*s*)

Convert a canonical string representation of a *ADFA* to a *ADFA* :param list s: the string in its canonical order :returns: the *ADFA* :rtype: *ADFA*

**See also:**

Marco Almeida, Nelma Moreira, and Rogério Reis. Exact generation of minimal acyclic deterministic finite automata. *International Journal of Foundations of Computer Science*, 19(4):751-765, August 2008.



## MODULE: GRAPHS (GRAPH CREATION AND MANIPULATION)

### Graph support

Basic Graph object support and manipulation

**class** `graphs.Graph`

Bases: `common.Drawable`

Graph base class

#### Variables

- **Vertices** (*list*) – Vertices' names
- **Edges** (*set*) – set of pairs (always sorted)



**addEdge** (*v1*, *v2*)

Adds an edge :param int *v1*: vertex 1 index :param int *v2*: vertex 2 index :raises GraphError: if edge is loop

**addVertex** (*vname*)

Adds a vertex (by name)

**Parameters** *vname* – vertex name

**Returns** vertex index

**Return type** `int`

**Raises** **DuplicateName** – if *vname* already exists

**dotFormat** (*size*)

Some dot representation

**Parameters** *size* (*str*) – size parameter for dotviz

**Return type** `str`

**vertexIndex** (*vname*, *autoCreate=False*)

Return vertex index

**Parameters**

- **autoCreate** (*bool*) – auto creation of non existing states
- **vname** – vertex name

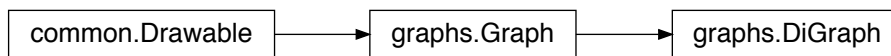
**Return type** *int*

**Raises** **GraphError** – if vname not found

**class** `graphs.DiGraph`

Bases: `graphs.Graph`

Directed graph base class



**addEdge** (*v1*, *v2*)

Adds an edge

**Parameters**

- **v1** (*int*) – vertex 1 index
- **v2** (*int*) – vertex 2 index

**static dotDrawEdge** (*st1*, *st2*, *sep*='\\n')

Draw a transition in Dot Format

**Parameters**

- **st1** (*str*) – starting state
- **st2** (*str*) – ending state
- **sep** (*str*) – separator

**Return type** *str*

**dotDrawVertex** (*sti*, *sep*='\\n')

Draw a Vertex in Dot Format

**Parameters**

- **sti** (*int*) – index of the state
- **sep** (*str*) – separator

**Return type** *str*

**dotFormat** (*size*='20, 20', *direction*='LR', *sep*='\\n', *strict*=False, *maxLblSz*=10)

A dot representation

**Parameters**

- **direction** (*str*) – direction of drawing
- **size** (*str*) – size of image
- **sep** (*str*) – line separator

- **maxLblSz** – max size of labels before getting removed
- **strict** – use limitations of label sizes

**Returns** the dot representation

**Return type** `str`

New in version 0.9.6.

Changed in version 0.9.8.

**inverse** ()

Inverse of a digraph

**class** `graphs.DiGraphVm`

Bases: `graphs.DiGraph`

Directed graph with marked vertices

**Variables** **MarkedV** (`set`) – set of marked vertices



**markVertex** (`v`)

Mark vertex `v`

**Parameters** **v** (`int`) – vertex





## MODULE: CONTEXT FREE GRAMMARS MANIPULATION (CFG)

### Context Free Grammars Manipulation.

Basic context-free grammars manipulation for building uniform random generetors

## 9.1 Class CFGGrammar (Context Free Grammar)

```
class cfg.CFGGrammar (gram)
```

Bases: `object`

Class for context-free grammars

### Variables

- **Rules** – grammar rules
- **Terminals** – terminals symbols
- **Nonterminals** – nonterminals symbols
- **Start** (*str*) – start symbol
- **ntr** – dictionary of rules for each nonterminal

Initialization

**Parameters** **gram** – is a list for productions; each production is a tuple (LeftHandside, RightHandside) with LeftHandside nonterminal, RightHandside list of symbols, First production is for start symbol

**NULLABLE** ()

Determines which nonterminals  $X \rightarrow^* []$

**makenonterminals** ()

Extracts  $C\{\text{nonterminals}\}$  from grammar rules.

**maketerminals** ()

Extracts  $C\{\text{terminals}\}$  from the rules. Nonterminals must already exist

## 9.2 Class CNF

```
class cfg.CNF (gram, mark='A@')
```

Bases: `cfg.CFGGrammar`

No useless nonterminals or epsilon rules are ALLOWED... Given a CFG grammar description generates one in CNF Then its possible to random generate words of a given size. Before some pre-calculations are nedded.

**Chomsky** ()  
Transform to CNF

**elim\_unitary** ()  
Elimination of unitary rules

## 9.3 Class `cfgGenerator`

**class** `cfg.cfgGenerator` (*cfgr, size*)  
Bases: `object`

CFG uniform genetaror

Object initialization :param cfgr: grammar for the random objects :type cfgr: CNF :param size: size of objects :type size: integer

**generate** ()  
Generates a new random object generated from the start symbol

**Returns** object

**Return type** string

## 9.4 Class `reStringRGenerator` (Reg Exp Generator)

**class** `cfg.reStringRGenerator` (*Sigma=None, size=10, cfgr=None, epsilon=None, empty=None, ident='Ti'*)  
Bases: `cfg.cfgGenerator`

Uniform random Generator for reStrings

**Uniform random generator for regular expressions. Used without arguments generates an uncollapsible re over {a,b} with size 10. For generate an arbitrary re over an alphabet of 10 symbols of size 100: `reStringRGenerator (smallAlphabet(10),100,reGrammar["g_regular_base"])`**

**Parameters**

- **Sigma** (*list/set*) – re alphabet (that will be the set of grammar terminals)
- **size** (*int*) – word size
- **cfgr** – base grammar
- **epsilon** – if not None is added to a grammar terminals
- **empty** – if not None is added to a grammar terminals

---

**Note:** the grammar can have already this symbols

---

## 9.5 Functions

`cfg.gRules` (*rules\_list, rulesym='->', rhssep=None, rulesep='|'*)  
Transforms a list of rules into a grammar description.

**Parameters**

- **rules\_list** – is a list of rule where rule is a string of the form: Word rulesym Word1 ... Word2 or Word rulesym []
- **rulesym** – LHS and RHS rule separator
- **rhssep** – RHS values separator (None for white chars)

**Returns** a grammar description

cfg.**smallAlphabet** (*k*, *sigma\_base*='a')

Easy way to have small alphabets

**Parameters**

- **k** – alphabet size (must be less than 52)
- **sigma\_base** – initial symbol

**Returns** alphabet

**Return type** [list](#)



## MODULE: RANDOM DFA GENERATOR (RNDFA)

### Random DFA generation

ICDFA Random generation binding

Changed in version 0.9.4: Interface python to the C code

Changed in version 0.9.6: Working with incomplete automata

Changed in version 0.9.8: distinct classes for complete and incomplete ICDFA

## 10.1 Class `ICDFArgen` (Generator container)

**class** `rndfa.ICDFArgen`

Bases: `object`

Generic ICDFA random generator class

---

**Note:** This is an abstract class, not to be used directly

---

### See also:

Marco Almeida, Nelma Moreira, and Rogério Reis. Enumeration and generation with a string automata representation. *Theoretical Computer Science*, 387(2):93-102, 2007

**next** ()

Get the next generated DFA

**Returns** a random generated ICDFA

**Return type** *DFA*

## 10.2 Class `ICDFArnd` (Complete ICDFA random generator)

**class** `rndfa.ICDFArnd` (*n*, *k*, *seed=0*)

Bases: `rndfa.ICDFArgen`

Complete ICDFA random generator class

This is the class for the uniform random generator for Initially Connected DFAs

### Variables

- `n` (*int*) – number of states

- **k** (*int*) – size of the alphabet
- **seed** (*int*) – seed for the random generator (if 0 uses time as seed)

**Attention:** At the moment, if two generators are ‘simultaneous’ used, and seed where provided, the repeatable aspect of the generated sequences is *not* warranted. To achieve that behaviour use one generator at a time.

Changed in version 1.3.4: seed added to the random generator

## 10.3 Class `ICDFArndIncomplete` (Incomplete IC DFA generator)

**class** `rndfa.ICDFArndIncomplete` (*n*, *k*, *bias=None*, *seed=0*)

Bases: `rndfa.ICDFArgen`

Incomplete IC DFA random generator class

### Variables

- **n** (*int*) – number of states
- **k** (*int*) – size of alphabet
- **bias** (*float*) – how often must the gost sink state appear (default None)
- **seed** (*int*) – seed for the random generator (if 0 uses time as seed)

**Raises** `IllegalBias` – if a *bias*  $\geq 1$  or  $\leq 0$  is provided

Changed in version 1.3.4: seed added to the random generator

## MODULE: RANDOM ADFA GENERATOR (RNDADFA)

### Random ADFA generation

ADFA Random generation binding

New in version 1.2.1.

## 11.1 Class ADFArnd (ADFA random generator)

**class** rndadfa.**ADFArnd** (*n*, *k*=2, *s*=1)

Sets a random generator for Adfas by sources. By default, *s*=1 to be initially connected

#### Variables

- **n** (*int*) – number of states
- **k** (*int*) – size of the alphabet
- **s** (*int*) – number of sources

---

**Note:** For IC DFA *s*=1

---

**alpha** (*n*, *s*, *k*=2)

Number of labeled acyclic initially connected DFA by states and by sources

#### Parameters

- **k** (*int*) – alphabet size
- **n** (*int*) – number of states
- **s** (*int*) – number of sources

**Return type** `int`

---

**Note:** uses `countAdfabySource`

---

**alpha0** (*n*, *s*, *k*=2)

Number of labeled acyclic initially connected DFA by states and by sources

#### Parameters

- **k** (*int*) – alphabet size
- **n** (*int*) – number of states

- **s** (*int*) – number of souces

**Return type** *int*

---

**Note:** uses gamma instead of beta or rndAdfa

---

**beta** (*n, s, u, k=2*)

Number of valid configurations of transitions

**Parameters**

- **k** (*int*) – alphabet size
- **n** (*int*) – number of states
- **s** (*int*) – number of souces
- **u** (*int*) – number of souces of n-s

**Return type** *int*

---

**Note:** not used by alpha or rndAdfa

---

**beta0** (*n, s, u, k=2*)

Function beta computed using sets

**countAdfaBySources** (*n, s, k=2*)

Number of labelled (initially connected) acyclic automata with n states, alphabet size k, and s sources

**Parameters**

- **k** (*int*) – alphabet size
- **n** (*int*) – number of states
- **s** (*int*) – number of souces

**Raises** **IndexError** – if number of states less than number of sources

**gamma** (*t, u, r*)

**Parameters**

- **t** (*int*) – size of T
- **u** (*int*) – size of U
- **r** (*int*) – size of R

**Return type** *int*

**next** ()

Generates a random adfa

**Returns** an dfa if number of sources is 1; otherwise self.transitions has the transitions of an adfa with s sources

**Return type** *DFA*

**rndAdfa** (*n, s*)

Recursively generates a initially connected adfa

**Parameters**



- **n** (*int*) – number of states
- **s** (*int*) – number of sources

**See also:**

Felice & Nicaud, CSR 2013 Lncs 7913, pp 88-99, Random Generation of Deterministic Acyclic Automata Using the Recursive Method, DOI:10.1007/978-3-642-38536-0\_8

**rndNumberSecondSources** (*n, s*)

Uniformly random generates the number of secondary sources

**Parameters**

- **n** (*int*) – number of states
- **s** (*int*) – number of sources

**Return type** *int***rndTransitionsFromSources** (*n, s, u*)

Generates the transitions from the sources, ensuring that all secondary sources are connected

**Parameters**

- **n** (*int*) – number of states
- **s** (*int*) – number of sources
- **u** (*int*) – number of secondary sources



## MODULE: COMBO OPERATIONS (COMBOOPERATIONS)

### Several combined operations for DFAs

Combined operations

`comboperations.starConcat` (*fa1*, *fa2*, *strict=False*)

Star of concatenation of two languages:  $(L1.L2)^*$

#### Parameters

- **f a1** (DFA) – first automaton
- **fa2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

#### See also:

Yuan Gao, Kai Salomaa, and Sheng Yu. ‘The state complexity of two combined operations: Star of catenation and star of reversal’. *Fundamenta Informaticae*, 83:75–89, Jan 2008.

`comboperations.concatWStar` (*fa1*, *fa2*, *strict=False*)

Concatenation combined with star:  $(L1.L2)^*$

#### Parameters

- **fa1** (DFA) – first automaton
- **fa2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

#### See also:

Bo Cui, Yuan Gao, Lila Kari, and Sheng Yu. ‘State complexity of two combined operations: Reversal-catenation and star-catenation’. *CoRR*, abs/1006.4646, 2010.

`comboperations.starWConcat` (*fa1*, *fa2*, *strict=False*)

Star combined with concatenation:  $(L1^*.L2)$

#### Parameters

- **fa1** (DFA) – first automaton
- **fa2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

**See also:**

Bo Cui, Yuan Gao, Lila Kari, and Sheng Yu. ‘State complexity of catenation combined with star and reversal’. CoRR, abs/1008.1648, 2010

`comboperations.starDisj` (*fa1, fa2, strict=False*)  
 Star of Union of two DFAs:  $(L1 + L2)^*$

**Parameters**

- **fa1** (DFA) – first automaton
- **fa2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

**See also:**

Arto Salomaa, Kai Salomaa, and Sheng Yu. ‘State complexity of combined operations’. Theor. Comput. Sci., 383(2-3):140–152, 2007.

`comboperations.starInter0` (*fa1, fa2, strict=False*)  
 Star of Intersection of two DFAs:  $(L1 \& L2)^*$

**Parameters**

- **fa1** (DFA) – first automaton
- **fa2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

**See also:**

Arto Salomaa, Kai Salomaa, and Sheng Yu. ‘State complexity of combined operations’. Theor. Comput. Sci., 383(2-3):140–152, 2007.

`comboperations.starInter` (*fa1, fa2, strict=False*)  
 Star of Intersection of two DFAs:  $(L1 \& L2)^*$

**Parameters**

- **fa1** (DFA) – first automaton
- **fa2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

`comboperations.disjWStar` (*f1, f2, strict=True*)  
 Union with star:  $(L1 + L2)^*$

**Parameters**

- **f1** (DFA) – first automaton
- **f2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

**See also:**

Yuan Gao and Sheng Yu. ‘State complexity of union and intersection combined with star and reversal’. CoRR, abs/1006.3755, 2010.

`comboperations.interwStar(f1, f2, strict=True)`

Intersection with star:  $(L1 \& L2^*)$

**Parameters**

- **f1** (DFA) – first automaton
- **f2** (DFA) – second automaton
- **strict** (*bool*) – should the alphabets be necessary equal?

**Return type** *DFA*

**See also:**

Yuan Gao and Sheng Yu. ‘State complexity of union and intersection combined with star and reversal’. CoRR, abs/1006.3755, 2010.



MODULE: CODES (CODES)

Code theory module

New in version 1.0.

## 13.1 Class CodeProperty

**class** `codes.CodeProperty` (*name*, *alph*)  
Bases: `object`

**See also:**

K. Dudzinski and S. Konstantinidis: Formal descriptions of code properties: decidability, complexity, implementation. International Journal of Foundations of Computer Science 23:1 (2012), 67–85.

**Variables** *Sigma* – the alphabet

## 13.2 Class TrajProp

**class** `codes.TrajProp` (*aut*, *Sigma*)  
Bases: `codes.IATProp`

Class of trajectory properties



Constructor

**Parameters**

- **aut** (*DFA/NFA*) – regular expression over {0,1}
- **Sigma** (*set*) – the alphabet

**static** `trajToTransducer` (*traj*, *Sigma*)

Input Altering Transducer corresponding to a Trajectory

**Parameters**

- **traj** (*NFA*) – trajectory language
- **Sigma** (*set*) – alphabet

Return type *SFT*

## 13.3 Class IPTProp

**class** `codes.IPTProp` (*aut, name=None*)

Bases: `codes.CodeProperty`

Input Preserving Transducer Property



### Variables

- **Aut** (*SFT*) – the transducer defining the property
- **Sigma** (*set*) – alphabet

Constructor :param *SFT* aut: Input preserving transducer

**addToCode** (*aut, N, n=2000*)

Returns an NFA and a list *W* of up to *N* words of length *ell*, such that the NFA accepts  $L(\text{aut}) \cup W$ , which is an error-detecting language. *ell* is computed from *aut*

### Parameters

- **aut** (*NFA*) – the automaton
- **N** (*int*) – the number of words to construct
- **n** (*int*) – number of tries when needing a new word

**Returns** an automaton and a list of strings

**Return type** *tuple*

**makeCode** (*N, ell, s, n=2000, ov\_free=False*)

Returns an NFA and a list *W* of up to *N* words of length *ell*, such that the NFA accepts *W*, which is an error-detecting language. The alphabet to use is  $\{0, 1, \dots, s-1\}$ . where  $s \leq 10$ .

### Parameters

- **N** (*int*) – the number of words to construct
- **ell** (*int*) – the codeword length
- **s** (*int*) – the alphabet size (must be  $\leq 10$ )
- **n** (*int*) – number of tries when needing a new word

**Returns** an automaton and a list of strings

**Return type** *tuple*



**makeCodeO** (*N, ell, s, n=2000, end=None, ov\_free=False*)

Returns an NFA and a list *W* of up to *N* words of length *ell*, such that the NFA accepts *W*, which is an error-detecting language. The alphabet to use is  $\{0,1,\dots,s-1\}$ . where  $s \leq 10$ .

**Parameters**

- **N** (*int*) – the number of words to construct
- **ell** (*int*) – the codeword length
- **s** (*int*) – the alphabet size (must be  $\leq 10$ )
- **n** (*int*) – number of tries when needing a new word
- **end** (*Word*) – a *Word* or *None* that should much the end of code words
- **ov\_free** (*Boolean*) – if *True* code words much be overlap free

**Returns** an automaton and a list of strings

**Return type** *tuple*

Note: not *ov\_free* and *end* defined simultaneously Note: *end* should be a *Word*

**maximalP** (*aut, U=None*)

Tests if the language is maximal w.r.t. the property

**Parameters**

- **aut** (*NFA*) – the automaton
- **U** (*NFA*) – Universe of permitted words ( $\Sigma^*$  as default)

**Return type** *bool*

**notMaxStatW** (*aut, ell, n=2000, ov\_free=False*)

Returns a word of length *ell* to add into *aut* or *None*; simpler version of function *nonMaxStatFEpsW*

**Parameters**

- **aut** (*NFA*) – the automaton
- **ell** (*int*) – the length of the words in *aut*
- **n** (*int*) – number of words to try

**Returns** a string or *None*

**Return type** *str*

**notMaximalW** (*aut, U=None*)

Tests if the language is maximal w.r.t. the property

**Parameters**

- **aut** (*DFA / NFA*) – the automaton
- **U** (*DFA / NFA*) – Universe of permitted words ( $\Sigma^*$  as default)

**Return type** *bool*

**Raises** **PropertyNotSatisfied** – if not satisfied

**notSatisfiesW** (*aut*)

Return a witness of non-satisfaction of the property by the automaton language

**Parameters** **aut** (*DFA / NFA*) – the automaton

**Returns** word witness pair

**Return type** `tuple`

**satisfiesP** (*aut*)

Satisfaction of the property by the automaton language

**Parameters** *aut* (*DFA/NFA*) – the automaton

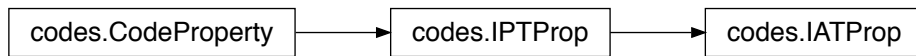
**Return type** `bool`

## 13.4 Class IATProp

**class** `codes.IATProp` (*aut*, *name=None*)

Bases: `codes.IPTProp`

Input Altering Transducer Property



Constructor :param SFT *aut*: Input preserving transducer

**notSatisfiesW** (*aut*)

Return a witness of non-satisfaction of the property by the automaton language

**Parameters** *aut* (*DFA/NFA*) – the automaton

**Returns** word witness pair

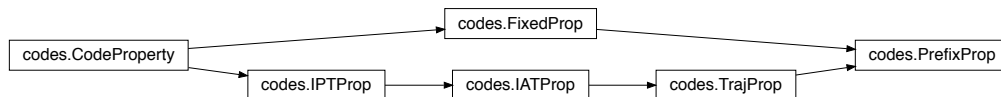
**Return type** `tuple`

## 13.5 Class PrefixProp

**class** `codes.PrefixProp` (*t*)

Bases: `codes.TrajProp`, `codes.FixedProp`

Prefix Property



**satisfiesPrefixP** (*aut*)

Satisfaction of property by the automaton language: faster than `satisfiesP`

**Parameters** `aut` (*DFA/NFA*) – the automaton

**Return type** `bool`

## 13.6 Class ErrDetectProp

`codes.ErrDetectProp`

alias of `codes.IPTProp`

## 13.7 Class ErrCorrectProp

**class** `codes.ErrCorrectProp` (*t*)

Bases: `codes.IPTProp`

Error Correcting Property



**notMaximalW** (*aut, U=None*)

Tests if the language is maximal w.r.t. the property

**Parameters**

- `aut` (*DFA/NFA*) – the automaton
- `U` (*DFA/NFA*) – Universe of permitted words ( $\Sigma^*$  as default)

**Return type** `bool`

**notSatisfiesW** (*aut*)

Satisfaction of the code property by the automaton language

**Parameters** `aut` (*DFA/NFA*) – the automaton

**Return type** `tuple`

**satisfiesP** (*aut*)

Satisfaction of the property by the automaton language

**See also:**

S. Konstantinidis: Transducers and the Properties of Error-Detection, Error-Correction and Finite-Delay Decodability. Journal Of Universal Computer Science 8 (2002), 278-291.

**Parameters** `aut` (*DFA/NFA*) – the automaton

**Return type** `bool`

## 13.8 Functions

`codes.buildTrajPropS` (*regex*, *sigma*)

Builds a TrajProp from a string regexp

**Parameters**

- **regex** (*str*) – the regular expression
- **sigma** (*set*) – alphabet

**Return type** *TrajProp*

`codes.buildIATPropF` (*fname*)

Builds a IATProp from a FAdo SFT file

**Parameters** **fname** (*str*) – file name

**Return type** *IATProp*

`codes.buildIPTPropF` (*fname*)

Builds a IPTProp from a FAdo SFT file

**Parameters** **fname** (*str*) – file name

**Return type** *IPTProp*

`codes.buildIATPropS` (*s*)

Builds a IATProp from a FAdo SFT string

**Parameters** **s** (*str*) – string containing SFT

**Return type** *IATProp*

`codes.buildIPTPropS` (*s*)

Builds a IPTProp from a FAdo SFT string

**Parameters** **s** (*str*) – file name

**Return type** *IPTProp*

`codes.buildErrorDetectPropF` (*fname*)

Builds an Error Detecting Property

**Parameters** **fname** (*str*) – file name

**Return type** *ErrDetectProp*

`codes.buildErrorCorrectPropF` (*fname*)

Builds an Error Correcting Property

**Parameters** **fname** (*str*) – file name

**Return type** *ErrCorrectProp*

`codes.buildErrorDetectProps` (*s*)

Builds an Error Detecting Property from string

**Parameters** **s** (*str*) – transducer string

**Return type** *ErrDetectProp*

`codes.buildErrorCorrectProps` (*s*)

Builds an Error Correcting Property from string

**Parameters** **s** (*str*) – transducer string

**Return type** *ErrCorrectProp*

`codes.buildPrefixProperty` (*alphabet*)

Builds a Prefix Code Property

**Parameters** `alphabet` (*set*) – alphabet

**Return type** *PrefixProp*

`codes.buildTrajProps` (*regex*, *sigma*)

Builds a TrajProp from a string regexp

**Parameters**

- `regex` (*str*) – the regular expression
- `sigma` (*set*) – alphabet

**Return type** *TrajProp*

`codes.editDistanceW` (*auto*)

Compute the edit distance of a given regular language accepted by the NFA via Input-altering transducer.

**Attention:** language should have at least two words

**See also:**

Lila Kari, Stavros Konstantinidis, Steffen Kopecki, Meng Yang. An efficient algorithm for computing the edit distance of a regular language via input-altering transducers. arXiv:1406.1041 [cs.FL]

**Parameters** `auto` (*NFA*) – language recogniser

**Returns** The edit distance of the given regular language plus a witness pair

**Return type** *tuple*

`codes.exponentialDensityP` (*aut*)

Checks if language density is exponential

Using breadth first search (BFS)

**Attention:** `aut` should not have Epsilon transitions

**Parameters** `aut` (*NFA*) – the representation of the language

**Return type** *bool*

`codes.createInputAlteringSIDTrans` (*n*, *sigmaSet*)

Create an input-altering SID transducer based

**Parameters**

- `n` (*int*) – max number of errors
- `sigmaSet` (*set*) – alphabet

**Returns** a transducer representing the SID channel

**Return type** *SFT*



## MODULE: GRAIL COMPATIBILITY (GRAIL)

### GRAIL support.

GRAIL formats support. This is an auxiliary module that could be imported by fa.py

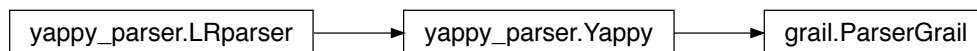
New in version 0.9.4.

### 14.1 Class ParserGrail

```
class grail.ParserGrail (no_table=1, table='.tableGrail')
```

Bases: `yappy_parser.Yappy`

A parser form GRAIL standard automata descriptions



### 14.2 Class Grail

```
class grail.Grail
```

Bases: `object`

A class for Grail execution

Changed in version 0.9.8: tries to initialise `execPath` from `fadorc`

```
do (cmd, *args)
```

Execute Grail command

#### Parameters

- **cmd** (*string*) – name of the command
- **args** – arguments

#### Raises

- **GrailCommandError** – if the syntax is not correct an exception is raised

- **FAdoGeneralError** – if Grail fails to execute something

**setExecPath** (*path*)

Sets the path to the Grail executables

**Parameters** *path* (*str*) – the path to Grail executables

## 14.3 Functions

`grail.exportToGrail` (*fileName*, *fa*)

Saves a finite automaton definition to a file using Grail format

**Parameters**

- **fileName** (*string*) – file name
- **fa** (*FA*) – the FA

`grail.FAToGrail` (*f*, *fa*)

Saves a finite automaton definition to an open file using Grail format

**Parameters**

- **f** (*file*) – opened file
- **fa** (*FA*) – the FA

`grail.importFromGrailFile` (*fileName*)

Imports a finite automaton from a file in GRAIL format

The type of the object returned depends on the transition definition red as well as the number of initial states declared

**Parameters** **fileName** (*str*) – file name

**Returns** the automata red

**Return type** *FA*

`grail.FAFromGrail` (*buffer*)

Imports a finite automaton from a buffer in GRAIL format

The type of the object returned depends on the transition definition red as well as the number of initial states declared

**Parameters** **buffer** (*str*) – buffer file

**Returns** the automata red

**Return type** *FA*

```
# ===== # Module: Verso Language (verso) #
===== # # .. automodule:: verso # :no-members: # # .. autoclass::
ParserVerso # :no-members: #
```



**MODULE: SET SPECIFICATION TRANSDUCERS AND AUTOMATA  
(SST)**

**Set Specification Transducer supportt**

New in version 1.4.

## 15.1 Class PSP

**class** `sst.PSP`

Bases: `object`

Relation pair of set specifications



**SMALL TUTORIAL**



## A SMALL TUTORIAL FOR FADO

FAdo system is a set tools for regular languages manipulation.

Regular languages can be represented by regular expressions (regexp) or finite automata, among other formalisms. Finite automata may be deterministic (DFA) or non-deterministic (NFA). In FAdo these representations are implemented as Python classes. A full documentation of all classes and methods is [here](#).

To work with FAdo, after installation, import the following modules on a Python interpreter:

```
>>> from FAdo.fa import *
>>> from FAdo.reex import *
>>> from FAdo.fio import *
```

The module `fa` implements the classes for finite automata and the module `reex` the classes for regular expressions. The module `fio` implements methods for IO of automata and related models.

General conventions

Methods which name ends in `P` test if the object verifies a given property and return `True` or `False`.

Finite Automata

The top class for finite automata is the class `FA`, which has two main subclasses: `OFA` for one way finite automata and the class `TFA` for two-way finite automata. The class `OFA` implements the basic structure of a finite automaton shared by DFAs and NFAs. This class defines the following attributes:

`Sigma`: the input alphabet (set)

`States`: the list of states. It is a list such that each state is referred by its index whenever it is used (transitions, `Final`, etc).

`Initial`: the initial state (or a set of initial states for NFA). It is an index or list of indexes.

`Final`: the set of final states. It is a list of indexes.

In general, one should not create instances (objects) of class `OFA`. The class `DFA` and `NFA` implement DFAs and NFAs, respectively. The class `GFA` implements generalized NFAs that are used in the conversion between finite automata and regular expressions. All three classes inherit from class `OFA`.

For each class there are special methods for add/delete/modify alphabet symbols, states and transitions.

DFAs

The following example shows how to build a DFA that accepts the words of  $\{0,1\}^*$  that are multiples of 3.

```
>>> m3= DFA()
>>> m3.setSigma(['0','1'])
>>> m3.addState('s1')
>>> m3.addState('s2')
```

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```

>>> m3.addState('s3')
>>> m3.setInitial(0)
>>> m3.addFinal(0)
>>> m3.addTransition(0, '0', 0)
>>> m3.addTransition(0, '1', 1)
>>> m3.addTransition(1, '0', 2)
>>> m3.addTransition(1, '1', 0)
>>> m3.addTransition(2, '0', 1)
>>> m3.addTransition(2, '1', 2)

```

It is now possible, for instance, to see the structure of the automaton or to test if a word is accepted by it.

```

>>> m3
DFA([[('s1', 's2', 's3'), ('1', '0'), 's1', ['s1'], "[('s1', '1', 's2'), ('s1', '0',
↪ 's1'), ('s2', '1', 's1'), ('s2', '0', 's3'), ('s3', '1', 's3'), ('s3', '0', 's2')]
↪ ")])
>>> m3.evalWordP("011")
True
>>> m3.evalWordP("1011")
False
>>>

```

If graphviz is installed it is also possible to display the diagram of an automaton as follows:

```
>>>m3.display()
```

Instead of constructing the DFA directly we can load (and save) it in a simple text format. For the previous automaton the description will be:

```

@DFA 0
0 1 1
0 0 0
1 1 0
1 0 2
2 1 2
2 0 1

```

Then, if this description is saved in file mul3.fa, we have

```
>>> m3=readFromFile("mul3.fa")[0]
```

As the set of states is represented by a Python list, the list method len can be used to determine the number of states of a FA:

```

>>> len(m3.States)
3

```

For the number of Transitions the countTransitions() method must be used

```

>>> m3.countTransitions()
6

```

To minimize a DFA any of the minimization algorithms implemented can be used:

```
>>> min=m3.minimalHopcroft()
```

In this case, the DFA was already minimal so min has the same number of states as m3.

Several (regularity preserving) operations of DFAs are implemented in FAdo: boolean (union (| or `__or__`), intersection (& or `__and__`) and complementation (~ or `__invert__`), concatenation (concat), reversal (reversal) and star (star).

```
>>> u = m3 | ~m3
>>> u
DFA(((1, 1), (0, 0), (2, 2)], set(['1', '0']), 0, set([0, 1, 2]), {0: {'1': 1, '0': 0}
↳, 1: {'1': 0, '0': 2}, 2: {'1': 2, '0': 1}}))
```

```
>>> m = u.minimal()
>>> m
DFA(((1, 1), ['1', '0'], '(1, 1)', ['(1, 1)'], "[('1, 1)', '1', '(1, 1)'], ('1, 1, 1)')
↳), '0', '(1, 1)'))
```

State names can be renamed in-place using:

```
>>> m.renameStates(range(len(m)))
```

```
DFA(((0), ['1', '0'], '0', ['0'], "[('1, 0), (0, '0', 0)"])))
```

Notice that m recognize all words over the alphabet {0,1}.

It is possible to generate a word recognisable by an automata (witness)

```
>>> u.witness()
'@epsilon'
```

In this case this allows to ensure that u recognizes the empty word.

This method is also useful for obtain a witness for the difference of two DFAs (witnessDiff).

To test if two DFAs are equivalent the the operator == (equivalenceP) can be used.

## NFAs

NFAs can be built and manipulated in a similar way. There is no distinction between NFAs with and without epsilon-transitions. But it is possible to test if a NFA has epsilon-transitions and convert between a NFA with epsilon-transitions to a (equivalent) NFA without them.

## Converting between NFAs and DFAs

The method toDFA allows to convert a NFA to an equivalent DFA by the subset construction method. The method toNFA migrates trivially a DFA to a NFA.

## Regular Expressions

A regular expression can be a symbol of the alphabet, the empty set (@emptyset), the empty word (@epsilon) or the concatenation or the union (+) or the Kleene star (\*) of a regular expression. Examples of regular expressions are a+b, (a+ba)\*, and (@epsilon+ a)(ba+ab+@emptyset).

The class regexp is the base class for regular expressions and is used to represent an alphabet symbol. The classes epsilon and emptyset are the subclasses used for the empty set and empty word, respectively. Complex regular expressions are concat, disj, and star.

As for DFAs (and NFAs) we can build directly a regular expressions as a Python class:

```
>>> r = star(disj(regexp("a"), concat(regexp("b"), regexp("a"))))
>>> print r
(a + (b a))*
```

But we can convert a string to a regexp class or subclass, using the method `str2regexp`.

```
>>> r = str2regexp("(a+ba)*")
>>> print r
(a + (b a))*
```

For regular expressions there are several measures available: alphabetic size, (parse) tree size, string length, number of epsilons and star height. It is also possible to explicitly associate an alphabet to regular expression (even if some symbols do not appear in it) (`setSigma`)

There are several algebraic properties that can be used to obtain equivalent regular expressions of a smaller size. The method `reduced` transforms a regular expression into one equivalent without some obvious unnecessary epsilons, emptysets or stars.

Several methods that allows the manipulation of derivatives (or partial derivatives) by a symbol or by a word are implemented. However, the class `regexp` does not deal with regular expressions module ACI properties (associativity, commutativity and idempotence of the union) (see class `xre`), so it is not possible to obtain all word derivatives of a given regular expression. This is not the case for partial derivatives.

To test if two regular expressions are equivalent the method `compare` can be used.

```
>>> r.compare(str2regexp("(a*(ba)*a)*"))
True
>>>
```

### Converting Finite Automata to Regular Expressions

For pedagogical purposes, it is implemented a recursive method that constructs a regular expression equivalent to a given DFA (`regexp`).

```
>>> print m3.regexp()
((0 + ((@epsilon + 0) (0* (@epsilon + 0)))) + ((1 + ((@epsilon + 0) (0* 1))) ((1 (0* 1)*
→1)) * (1 + (1 (0* (@epsilon + 0)))))) + (((1 + ((@epsilon + 0) (0* 1))) ((1 (0* 1)*
→0)) ((1 + (0 ((1 (0* 1))* 0))) * (0 ((1(0* 1))* (1 + (1 (0* (@epsilon + 0))))))))
```

Methods based on state elimination techniques are usually more efficient, and produces much smaller regular expressions. We have implemented several heuristics for the elimination order.

```
>>> print m3.reCG()
((0 + (1 1)) + (((1 0) (1 + (0 0))* (0 1)))*
```

### Converting Regular Expressions to Finite Automata

Several methods to convert between regular expressions and NFAs are implemented. With the Thompson construction a NFA with epsilon transitions is obtained (`nfaThompson`). Epsilon free NFAs can be obtained by the Glushkov method (Position automata) (`nfaPosition`), the partial derivatives method (`nfaPD`) or by the follow method (`nfaFollow`). The two last methods usually allows to obtain smaller NFAs.

```
>>> r.nfaThompson()
NFA([[', ' ', ' ', ' ', '0', '1', '2', '3', '8', '9'], ['a', 'b'], ['8'], ['9'], "[('',
→ '@epsilon', ''), ('', '@epsilon', 0), ('', '@epsilon', 9), ('', 'a', ''), ('',
→ '@epsilon', ''), (0, 'b', 1), (1, '@epsilon', 2), (2, 'a', 3), (3, '@epsilon', ''),
→ ('8', '@epsilon', ''), ('8', '@epsilon', 9), ('9', '@epsilon', 8)]]")
```



```
>>> r.nfaPosition()
NFA([('Initial', "('a', 1)", "('b', 2)", "('a', 3)"), ['a', 'b'], ['Initial'], [
↪ 'Initial', "('a', 1)", "('a', 3)"], '[(\\"Initial\\', \\'a\\', "\\'a\\', 1)"), (\
↪ 'Initial\\', \\'b\\', "\\'b\\', 2)"), ("(\\'a\\', 1)", \\'a\\', "\\'a\\', 1)"), ("(\\'a\\', 1)
↪ ", \\'b\\', "\\'b\\', 2)"), ("(\\'b\\', 2)", \\'a\\', "\\'a\\', 3)"), ("(\\'a\\', 3)", \\'a\\',
↪ "\\'a\\', 1)"), ("(\\'a\\', 3)", \\'b\\', "\\'b\\', 2)"]])
```

```
>>> r.nfaPD()
NFA([(' (a + (b a))*', 'a (a + (b a))*'], ['a', 'b'], ['(a + (b a))*'], ['(a + (b a))*
↪ ', "(star(disj(regexp(a), concat(regexp(b), regexp(a))))", 'a', star(disj(regexp(a),
↪ concat(regexp(b), regexp(a))))), (star(disj(regexp(a), concat(regexp(b), regexp(a))))),
↪ 'b', concat(regexp(a), star(disj(regexp(a), concat(regexp(b), regexp(a))))),
↪ (concat(regexp(a), star(disj(regexp(a), concat(regexp(b), regexp(a))))), 'a',
↪ star(disj(regexp(a), concat(regexp(b), regexp(a))))]"]])
```

### General Example

Considering the several methods described before it is possible to convert between the different equivalent representations of regular languages, as well to perform several regularity preserving operations.

```
>>> r.nfaPosition().toDFA().minimal(complete=False)
DFA([('0', '2'], ['a', 'b'], '0', ['0'], ["('0', 'a', '0'), ('0', 'b', '2'), ('2', 'a
↪ ', '0')"]])
>>> m3 == m3.reCG().nfaPD().toDFA().minimal()
True
>>>
```

### More classes and modules

Several other classes and modules are also available, including:

class ICDFArnd (module rndfa.py): Random DFA generation

class FL (module fl.py): special methods for finite languages

module comboperations.py: implementation of several algorithms for several combined operations with DFAs and NFAs

module grail.py: compatibility with GRAIL

module transducers.py: several classes and methods for transducers

module codes.py: language tests for a property (set of languages) specified by a transducer



## INDICES AND TABLES

- genindex
- modindex
- search



## PYTHON MODULE INDEX

### C

cfg, 107  
codes, 121  
comboperations, 117  
common, 47

### f

fa, 5  
fio, 49  
fl, 93

### g

grail, 129  
graphs, 103

### r

reex, 51  
rndadfa, 113  
rndfa, 111

### s

sst, 131

### t

transducers, 85



## A

acyclicP () (*fa.OFA method*), 13  
 add () (*fa.SSemiGroup method*), 44  
 addEdge () (*graphs.DiGraph method*), 104  
 addEdge () (*graphs.Graph method*), 103  
 addEpsilonLoops () (*fa.NFA method*), 31  
 addEpsilonLoops () (*transducers.SFT method*), 86  
 addFinal () (*fa.FA method*), 5  
 addGen () (*fa.SSemiGroup method*), 44  
 addInitial () (*fa.NFA method*), 31  
 addSigma () (*fa.FA method*), 5  
 addState () (*fa.FA method*), 6  
 addState () (*fl.AFA method*), 95  
 addSuffix () (*fl.ADFA method*), 96  
 addToCode () (*codes.IPTProp method*), 122  
 addTransition () (*fa.DFA method*), 17  
 addTransition () (*fa.GFA method*), 41  
 addTransition () (*fa.NFA method*), 31  
 addTransition () (*fa.NFAr method*), 39  
 addTransition () (*fa.OFA method*), 13  
 addTransition () (*transducers.SFT method*), 86  
 addTransitionProductQ () (*transducers.SFT method*), 86  
 addTransitionQ () (*fa.NFA method*), 31  
 addTransitionQ () (*transducers.SFT method*), 86  
 addVertex () (*graphs.Graph method*), 103  
 addWord () (*fl.FL method*), 93  
 addWords () (*fl.FL method*), 93  
 ADFA (*class in fl*), 96  
 ADFArnd (*class in rndadfa*), 113  
 aEquiv () (*fa.DFA method*), 17  
 AFA (*class in fl*), 95  
 allRegExps () (*fa.OFA method*), 13  
 alpha () (*rndadfa.ADFArnd method*), 113  
 alpha0 () (*rndadfa.ADFArnd method*), 113  
 alphabeticLength () (*reex.atom static method*), 71  
 alphabeticLength () (*reex.connective method*), 61  
 alphabeticLength () (*reex.option method*), 68  
 alphabeticLength () (*reex.power method*), 67  
 alphabeticLength () (*reex.regexp method*), 51  
 alphabeticLength () (*reex.sconnective method*), 77  
 alphabeticLength () (*reex.snot method*), 81

alphabeticLength () (*reex.specialConstant static method*), 56  
 alphabeticLength () (*reex.star method*), 62  
 ANFA (*class in fl*), 99  
 assignLow () (*fa.GFA method*), 41  
 assignNum () (*fa.GFA method*), 41  
 atom (*class in reex*), 71  
 autobisimulation () (*fa.NFA method*), 32  
 autobisimulation2 () (*fa.NFA method*), 32

## B

beta () (*rndadfa.ADFArnd method*), 114  
 beta0 () (*rndadfa.ADFArnd method*), 114  
 buildErrorCorrectPropF () (*in module codes*), 126  
 buildErrorCorrectPropS () (*in module codes*), 126  
 buildErrorDetectPropF () (*in module codes*), 126  
 buildErrorDetectPropS () (*in module codes*), 126  
 buildIATPropF () (*in module codes*), 126  
 buildIATPropS () (*in module codes*), 126  
 buildIPTPropF () (*in module codes*), 126  
 buildIPTPropS () (*in module codes*), 126  
 buildPrefixProperty () (*in module codes*), 127  
 buildTrajPropS () (*in module codes*), 126, 127

## C

cfg (*module*), 107  
 cfgGenerator (*class in cfg*), 108  
 CFGrammar (*class in cfg*), 107  
 Chomsky () (*cfg.CNF method*), 107  
 closeEpsilon () (*fa.NFA method*), 32  
 CNF (*class in cfg*), 107  
 CodeProperty (*class in codes*), 121  
 codes (*module*), 121  
 comboperations (*module*), 117  
 common (*module*), 47  
 compare () (*reex.regexp method*), 51  
 compareMinimalDFA () (*reex.regexp method*), 51  
 compat () (*fa.DFA method*), 18  
 complete () (*fa.DFA method*), 18  
 complete () (*fl.ADFA method*), 97

completeDelta() (*fa.GFA method*), 42  
 completeMinimal() (*fa.DFA method*), 18  
 completeP() (*fa.DFA method*), 18  
 completeProduct() (*fa.DFA method*), 18  
 composition() (*transducers.SFT method*), 86  
 computeFollowNames() (*fa.NFA method*), 32  
 computeKernel() (*fa.DFA method*), 18  
 concat (*class in reex*), 64  
 concat() (*fa.DFA method*), 18  
 concat() (*fa.NFA method*), 32  
 concat() (*transducers.SFT method*), 87  
 concatI() (*fa.DFA method*), 19  
 concatWStar() (*in module comboperations*), 117  
 conj (*class in reex*), 70  
 conjunction() (*fa.FA method*), 6  
 connective (*class in reex*), 61  
 countAdfaBySources() (*rndadfa.ADFArnd method*), 114  
 countTransitions() (*fa.FA method*), 6  
 countTransitions() (*fa.NFA method*), 32  
 createInputAlteringSIDTrans() (*in module codes*), 127  
 cross() (*reex.sdisj method*), 79  
 cutPoints() (*fa.OFA method*), 13

## D

deleteState() (*fa.DFA method*), 19  
 deleteState() (*fa.FA method*), 6  
 deleteState() (*fa.GFA method*), 42  
 deleteState() (*transducers.SFT method*), 87  
 deleteStates() (*fa.DFA method*), 19  
 deleteStates() (*fa.GFA method*), 42  
 deleteStates() (*fa.NFA method*), 32  
 deleteStates() (*fa.NFAr method*), 39  
 deleteStates() (*fa.OFA method*), 13  
 deleteStates() (*transducers.SFT method*), 87  
 delFinal() (*fa.FA method*), 6  
 delFinals() (*fa.FA method*), 6  
 delta (*fa.FA attribute*), 5  
 delta (*fa.SemiDFA attribute*), 12  
 Delta() (*fa.DFA method*), 16  
 delTransition() (*fa.DFA method*), 19  
 delTransition() (*fa.NFA method*), 32  
 delTransition() (*fa.NFAr method*), 39  
 delTransition() (*transducers.SFT method*), 87  
 derivative() (*reex.atom method*), 71  
 derivative() (*reex.sconcat method*), 78  
 derivative() (*reex.sconj method*), 81  
 derivative() (*reex.sdisj method*), 79  
 derivative() (*reex.sigmaP method*), 59  
 derivative() (*reex.sigmaS method*), 60  
 derivative() (*reex.snot method*), 81  
 derivative() (*reex.specialConstant method*), 56  
 derivative() (*reex.sstar method*), 79

deterministicP() (*fa.DFA static method*), 20  
 deterministicP() (*fa.NFA method*), 33  
 detSet() (*fa.NFA method*), 33  
 DFA (*class in fa*), 16  
 dfaAuPoint() (*reex.regex method*), 52  
 dfaBrzozowski() (*reex.regex method*), 52  
 DFAtoADFA() (*in module fl*), 101  
 dfaYMG() (*reex.regex method*), 52  
 DFCA (*class in fl*), 95  
 DFS() (*fa.GFA method*), 41  
 dfs\_visit() (*fa.GFA method*), 42  
 diff() (*fl.FL method*), 93  
 DiGraph (*class in graphs*), 104  
 DiGraphVm (*class in graphs*), 105  
 directRank() (*fl.AFA method*), 95  
 disj (*class in reex*), 65  
 disj() (*fa.FA method*), 6  
 disjunction() (*fa.FA method*), 6  
 disjWStar() (*in module comboperations*), 118  
 diss() (*fl.ADFA method*), 97  
 dissMin() (*fl.ADFA method*), 97  
 dist() (*fa.DFA method*), 20  
 distDerivative() (*reex.specialConstant method*), 56  
 distMin() (*fa.DFA method*), 20  
 distR() (*fa.DFA method*), 20  
 distRMin() (*fa.DFA method*), 20  
 distTS() (*fa.DFA method*), 20  
 do() (*grail.Grail method*), 129  
 dotDrawEdge() (*graphs.DiGraph static method*), 104  
 dotDrawState() (*fa.FA method*), 7  
 dotDrawState() (*fa.SemiDFA method*), 12  
 dotDrawTransition() (*fa.FA method*), 7  
 dotDrawTransition() (*fa.OFA static method*), 13  
 dotDrawTransition() (*fa.SemiDFA static method*), 12  
 dotDrawVertex() (*graphs.DiGraph method*), 104  
 dotFormat() (*fa.FA method*), 7  
 dotFormat() (*fa.NFA method*), 33  
 dotFormat() (*fa.SemiDFA method*), 12  
 dotFormat() (*graphs.DiGraph method*), 104  
 dotFormat() (*graphs.Graph method*), 103  
 dump() (*fa.OFA method*), 13  
 dup() (*fa.DFA method*), 20  
 dup() (*fa.GFA method*), 42  
 dup() (*fa.NFA method*), 33  
 dup() (*fa.OFA method*), 13  
 dup() (*fl.ADFA method*), 97  
 dup() (*transducers.SFT method*), 87

## E

editDistanceW() (*in module codes*), 127  
 elim\_unitary() (*cfg.CNF method*), 108  
 elimEpsilon() (*fa.NFA method*), 33



- elimEpsilonO() (*fa.NFAr method*), 39
  - eliminate() (*fa.GFA method*), 42
  - eliminateAll() (*fa.GFA method*), 42
  - eliminateDeadName() (*fa.FA method*), 7
  - eliminateEpsilonTransitions() (*fa.NFA method*), 33
  - eliminateSingles() (*fa.OFA method*), 14
  - eliminateState() (*fa.GFA method*), 42
  - eliminateStout() (*fa.OFA method*), 14
  - eliminateTSymbol() (*fa.NFA method*), 33
  - emptyP() (*fa.OFA method*), 14
  - emptyP() (*transducers.SFT method*), 87
  - emptyset (*class in reex*), 58
  - emptysetP() (*reex.emptyset static method*), 59
  - emptysetP() (*reex.regexp static method*), 52
  - ensureDead() (*fl.AFA method*), 95
  - epsilon (*class in reex*), 58
  - epsilonClosure() (*fa.NFA method*), 34
  - epsilonLength() (*reex.atom static method*), 71
  - epsilonLength() (*reex.connective method*), 61
  - epsilonLength() (*reex.emptyset method*), 59
  - epsilonLength() (*reex.epsilon static method*), 58
  - epsilonLength() (*reex.option method*), 68
  - epsilonLength() (*reex.power method*), 67
  - epsilonLength() (*reex.regexp method*), 52
  - epsilonLength() (*reex.sconnective method*), 77
  - epsilonLength() (*reex.snot method*), 82
  - epsilonLength() (*reex.star method*), 62
  - epsilonOutP() (*transducers.SFT method*), 87
  - epsilonP() (*fa.NFA method*), 34
  - epsilonP() (*reex.emptyset method*), 59
  - epsilonP() (*reex.epsilon static method*), 58
  - epsilonP() (*reex.regexp method*), 52
  - epsilonP() (*transducers.SFT method*), 87
  - epsilonPaths() (*fa.NFA method*), 34
  - equal() (*fa.DFA method*), 20
  - equivalentP() (*fa.FA method*), 8
  - equivalentP() (*reex.regexp method*), 53
  - equivP() (*reex.regexp method*), 52
  - equivReduced() (*fa.NFA method*), 34
  - ErrCorrectProp (*class in codes*), 125
  - ErrDetectProp (*in module codes*), 125
  - evalNumberOfStateCycles() (*fa.OFA method*), 14
  - evalRank() (*fl.AFA method*), 96
  - evalSymbol() (*fa.DFA method*), 21
  - evalSymbol() (*fa.FA method*), 8
  - evalSymbol() (*fa.GFA method*), 42
  - evalSymbol() (*fa.NFA method*), 34
  - evalSymbol() (*fa.OFA method*), 14
  - evalSymbolI() (*fa.DFA method*), 21
  - evalSymbolL() (*fa.DFA method*), 21
  - evalSymbolLI() (*fa.DFA method*), 21
  - evalWord() (*fa.DFA method*), 22
  - evalWordP() (*fa.DFA method*), 22
  - evalWordP() (*fa.NFA method*), 34
  - evalWordP() (*reex.regexp method*), 53
  - evalWordP() (*transducers.SFT method*), 87
  - evalWordSlowP() (*transducers.SFT method*), 87
  - ewp() (*reex.concat method*), 64
  - ewp() (*reex.conj method*), 70
  - ewp() (*reex.disj method*), 65
  - ewp() (*reex.emptyset method*), 59
  - ewp() (*reex.epsilon static method*), 58
  - ewp() (*reex.option method*), 68
  - ewp() (*reex.regexp method*), 53
  - ewp() (*reex.sconcat method*), 78
  - ewp() (*reex.sconj method*), 81
  - ewp() (*reex.sdisj method*), 80
  - ewp() (*reex.shuffle method*), 70
  - ewp() (*reex.sigmaP method*), 60
  - ewp() (*reex.sigmaS method*), 60
  - ewp() (*reex.snot method*), 82
  - ewp() (*reex.star method*), 62
  - exponentialDensityP() (*in module codes*), 127
  - exportToGrail() (*in module grail*), 130
- ## F
- FA (*class in fa*), 5
  - fa (*module*), 5
  - FAFromGrail() (*in module grail*), 130
  - FAToGrail() (*in module grail*), 130
  - filter() (*fl.FL method*), 93
  - Final (*fa.FA attribute*), 5
  - finalCompP() (*fa.DFA method*), 22
  - finalCompP() (*fa.GFA method*), 42
  - finalCompP() (*fa.NFA method*), 35
  - finalCompP() (*fa.OFA method*), 14
  - finalP() (*fa.FA method*), 8
  - finalsP() (*fa.FA method*), 8
  - fio (*module*), 49
  - first() (*reex.atom method*), 72
  - first() (*reex.concat method*), 64
  - first() (*reex.connective method*), 61
  - first() (*reex.disj method*), 65
  - first() (*reex.option method*), 68
  - first() (*reex.power method*), 67
  - first() (*reex.regexp method*), 53
  - first() (*reex.sconnective method*), 77
  - first() (*reex.sdisj method*), 80
  - first() (*reex.shuffle method*), 70
  - first() (*reex.snot method*), 82
  - first() (*reex.specialConstant static method*), 56
  - first() (*reex.star method*), 62
  - FL (*class in fl*), 93
  - fl (*module*), 93
  - followFromPosition() (*fa.NFA method*), 35
  - followLists() (*reex.atom method*), 72

followLists() (*reex.sdisj method*), 80  
 followLists() (*reex.specialConstant method*), 56  
 followListsD() (*reex.atom method*), 72  
 followListsD() (*reex.shuffle method*), 70  
 followListsD() (*reex.specialConstant method*), 56  
 followListsStar() (*reex.atom method*), 72  
 followListsStar() (*reex.option method*), 68  
 followListsStar() (*reex.sdisj method*), 80  
 followListsStar() (*reex.specialConstant static method*), 56  
 forceToDFA() (*fl.ADFA method*), 97  
 forceToDFCA() (*fl.ADFA method*), 97  
 functionalP() (*transducers.SFT method*), 88

## G

gamma() (*rndadfa.ADFArnd method*), 114  
 generate() (*cfg.cfgGenerator method*), 108  
 genRandomTrie() (*in module fl*), 101  
 genRndTrieBalanced() (*in module fl*), 100  
 genRndTriePrefix() (*in module fl*), 101  
 genRndTrieUnbalanced() (*in module fl*), 100  
 getLeaves() (*fl.AFA method*), 96  
 GFA (*class in fa*), 41  
 Grail (*class in grail*), 129  
 grail (*module*), 129  
 Graph (*class in graphs*), 103  
 graphs (*module*), 103  
 gRules() (*in module cfg*), 108

## H

half() (*fa.NFA method*), 35  
 hasStateIndexP() (*fa.FA method*), 8  
 hasTransitionP() (*fa.NFA method*), 35  
 hasTrapStateP() (*fa.DFA method*), 22  
 head() (*reex.sconcat method*), 78  
 head\_rev() (*reex.sconcat method*), 78  
 HKeqP() (*fa.DFA method*), 17  
 HKeqP() (*fa.NFA method*), 31  
 homogeneousFinalityP() (*fa.NFA method*), 35  
 homogenousP() (*fa.NFA method*), 35  
 homogenousP() (*fa.NFAr method*), 40  
 hyperMinimal() (*fa.DFA method*), 22

## I

IATProp (*class in codes*), 124  
 ICDFArgen (*class in rndfa*), 111  
 ICDFArnd (*class in rndfa*), 111  
 ICDFArndIncomplete (*class in rndfa*), 112  
 images() (*fa.FA method*), 8  
 importFromGrailFile() (*in module grail*), 130  
 inDegree() (*fa.DFA method*), 22  
 indexList() (*fa.FA method*), 8  
 infix() (*fa.DFA method*), 23  
 inIntersection() (*transducers.SFT method*), 88

inIntersectionSlow() (*transducers.SFT method*), 88  
 Initial (*fa.FA attribute*), 5  
 initialComp() (*fa.DFA method*), 23  
 initialComp() (*fa.GFA method*), 42  
 initialComp() (*fa.NFA method*), 35  
 initialComp() (*fa.OFA method*), 14  
 initialP() (*fa.DFA method*), 23  
 initialP() (*fa.FA method*), 8  
 initialSet() (*fa.DFA method*), 23  
 initialSet() (*fa.FA method*), 9  
 inputs() (*fa.FA method*), 9  
 intersection() (*fl.FL method*), 94  
 interWStar() (*in module comboperations*), 119  
 inverse() (*graphs.DiGraph method*), 105  
 inverse() (*transducers.SFT method*), 88  
 IPTProp (*class in codes*), 122

## J

joinStates() (*fa.DFA method*), 23

## L

last() (*reex.atom method*), 72  
 last() (*reex.concat method*), 64  
 last() (*reex.connective method*), 61  
 last() (*reex.disj method*), 65  
 last() (*reex.option method*), 68  
 last() (*reex.power method*), 67  
 last() (*reex.regexp method*), 53  
 last() (*reex.sconnective method*), 77  
 last() (*reex.sdisj method*), 80  
 last() (*reex.snot method*), 82  
 last() (*reex.specialConstant method*), 57  
 last() (*reex.star method*), 62  
 length (*fl.DFCA attribute*), 95  
 lEquivNFA() (*fa.NFA method*), 35  
 level() (*fl.ADFA method*), 97  
 linearForm() (*reex.atom method*), 73  
 linearForm() (*reex.concat method*), 64  
 linearForm() (*reex.conj method*), 70  
 linearForm() (*reex.connective method*), 61  
 linearForm() (*reex.disj method*), 65  
 linearForm() (*reex.option method*), 68  
 linearForm() (*reex.power method*), 67  
 linearForm() (*reex.regexp method*), 53  
 linearForm() (*reex.sconcat method*), 78  
 linearForm() (*reex.sconj method*), 81  
 linearForm() (*reex.sconnective method*), 77  
 linearForm() (*reex.sdisj method*), 80  
 linearForm() (*reex.shuffle method*), 70  
 linearForm() (*reex.sigmaP method*), 60  
 linearForm() (*reex.sigmaS method*), 60  
 linearForm() (*reex.snot method*), 82  
 linearForm() (*reex.specialConstant method*), 57

linearForm() (*reex.sstar method*), 79  
 linearForm() (*reex.star method*), 63  
 linearFormC() (*reex.atom method*), 73  
 linearFormC() (*reex.sconcat method*), 78  
 linearFormC() (*reex.sdisj method*), 80  
 linearFormC() (*reex.sigmaP method*), 60  
 linearFormC() (*reex.sigmaS method*), 61  
 linearFormC() (*reex.snot method*), 82  
 linearP() (*reex.atom method*), 73  
 lrEquivNFA() (*fa.NFA method*), 35

## M

MADFA() (*fl.FL method*), 93  
 makeCode() (*codes.IPTProp method*), 122  
 makeCodeO() (*codes.IPTProp method*), 122  
 makenonterminals() (*cfg.CFGGrammar method*), 107  
 makeReversible() (*fa.DFA method*), 23  
 maketerminals() (*cfg.CFGGrammar method*), 107  
 mark() (*reex.atom method*), 73  
 mark() (*reex.concat method*), 64  
 mark() (*reex.conj method*), 70  
 mark() (*reex.connective method*), 61  
 mark() (*reex.disj method*), 65  
 mark() (*reex.option method*), 68  
 mark() (*reex.power method*), 67  
 mark() (*reex.regexp method*), 53  
 mark() (*reex.sconnective method*), 77  
 mark() (*reex.shuffle method*), 70  
 mark() (*reex.snot method*), 82  
 mark() (*reex.specialConstant method*), 57  
 mark() (*reex.star method*), 63  
 marked() (*reex.regexp method*), 53  
 markNonEquivalent() (*fa.DFA method*), 23  
 markVertex() (*graphs.DiGraphVm method*), 105  
 maximalP() (*codes.IPTProp method*), 123  
 measure() (*reex.atom static method*), 73  
 measure() (*reex.emptyset static method*), 59  
 measure() (*reex.epsilon static method*), 58  
 mergeInitial() (*fl.ANFA method*), 99  
 mergeLeaves() (*fl.ANFA method*), 99  
 mergeStates() (*fa.DFA method*), 23  
 mergeStates() (*fa.NFAr method*), 40  
 mergeStates() (*fl.ANFA method*), 99  
 mergeStatesSet() (*fa.NFAr method*), 40  
 minDFCA() (*fl.ADFA method*), 97  
 minimal() (*fa.DFA method*), 24  
 minimal() (*fa.NFA method*), 36  
 minimal() (*fl.ADFA method*), 98  
 minimalBrzozowski() (*fa.OFA method*), 14  
 minimalBrzozowskiP() (*fa.OFA method*), 14  
 minimalDFA() (*fa.NFA method*), 36  
 minimalHopcroft() (*fa.DFA method*), 24  
 minimalHopcroftP() (*fa.DFA method*), 24

minimalIncremental() (*fa.DFA method*), 24  
 minimalIncrementalP() (*fa.DFA method*), 24  
 minimalMoore() (*fa.DFA method*), 24  
 minimalMooreSq() (*fa.DFA method*), 24  
 minimalMooreSqP() (*fa.DFA method*), 25  
 minimalNCompleteP() (*fa.DFA method*), 25  
 minimalNotEquivP() (*fa.DFA method*), 25  
 minimalP() (*fa.DFA method*), 25  
 minimalP() (*fl.ADFA method*), 98  
 minimalWatson() (*fa.DFA method*), 25  
 minimalWatsonP() (*fa.DFA method*), 25  
 minReversible() (*fl.ADFA method*), 98  
 moveFinal() (*fl.ANFA method*), 100  
 multiLineAutomaton() (*fl.FL method*), 94  
 MyhillNerodePartition() (*fa.DFA method*), 17

## N

next() (*fl.RndWGen method*), 100  
 next() (*rndadfa.ADFArnd method*), 114  
 next() (*rndfa.ICDFArgen method*), 111  
 NFA (*class in fa*), 30  
 nfaFollow() (*reex.regexp method*), 53  
 nfaFollowEpsilon() (*reex.regexp method*), 53  
 nfaGlushkov() (*reex.regexp method*), 54  
 nfaNaiveFollow() (*reex.regexp method*), 54  
 nfaPD() (*reex.regexp method*), 54  
 nfaPDO() (*reex.regexp method*), 54  
 nfaPosition() (*reex.regexp method*), 54  
 nfaPre() (*reex.regexp method*), 55  
 nfaPSNF() (*reex.regexp method*), 54  
 NFAr (*class in fa*), 39  
 nfaThompson() (*reex.atom method*), 73  
 nfaThompson() (*reex.disj method*), 65  
 nfaThompson() (*reex.epsilon method*), 58  
 nfaThompson() (*reex.option method*), 68  
 nfaThompson() (*reex.star method*), 63  
 noBlankNames() (*fa.FA method*), 9  
 nonEmptyW() (*transducers.SFT method*), 88  
 nonFunctionalW() (*transducers.SFT method*), 89  
 normalize() (*fa.GFA method*), 42  
 notEmptyW() (*reex.regexp method*), 55  
 notequal() (*fa.DFA method*), 25  
 notMaximalW() (*codes.ErrCorrectProp method*), 125  
 notMaximalW() (*codes.IPTProp method*), 123  
 notMaxStatW() (*codes.IPTProp method*), 123  
 notSatisfiesW() (*codes.ErrCorrectProp method*), 125  
 notSatisfiesW() (*codes.IATProp method*), 124  
 notSatisfiesW() (*codes.IPTProp method*), 123  
 NULLABLE() (*cfg.CFGGrammar method*), 107

## O

OFA (*class in fa*), 12  
 oldAnd() (*fa.NFA method*), 36

option (*class in reex*), 68  
 ordered() (*fl.AFA method*), 96  
 orderedStrConnComponents() (*fa.DFA method*), 26  
 outIntersection() (*transducers.SFT method*), 89  
 outIntersectionDerived() (*transducers.SFT method*), 89  
 outputs() (*transducers.SFT method*), 89

## P

pairGraph() (*fa.DFA method*), 26  
 ParseReg (*class in reex*), 76  
 ParserGrail (*class in grail*), 129  
 partialDerivatives() (*reex.atom method*), 73  
 partialDerivatives() (*reex.epsilon static method*), 58  
 partialDerivatives() (*reex.sconcat method*), 78  
 partialDerivatives() (*reex.sconj method*), 81  
 partialDerivatives() (*reex.sdisj method*), 80  
 partialDerivatives() (*reex.sigmaP method*), 60  
 partialDerivatives() (*reex.sigmaS method*), 61  
 partialDerivatives() (*reex.snot method*), 82  
 partialDerivatives() (*reex.sstar method*), 79  
 partialDerivativesC() (*reex.atom method*), 74  
 partialDerivativesC() (*reex.emptyset method*), 59  
 partialDerivativesC() (*reex.epsilon method*), 58  
 partialDerivativesC() (*reex.sconcat method*), 78  
 partialDerivativesC() (*reex.sconj method*), 81  
 partialDerivativesC() (*reex.sdisj method*), 80  
 partialDerivativesC() (*reex.sigmaP static method*), 60  
 partialDerivativesC() (*reex.sigmaS method*), 61  
 partialDerivativesC() (*reex.snot method*), 82  
 partialDerivativesC() (*reex.specialConstant method*), 57  
 partialDerivativesC() (*reex.sstar method*), 79  
 PD() (*reex.atom method*), 71  
 plus() (*fa.FA method*), 9  
 position (*class in reex*), 75  
 possibleToReverse() (*fa.DFA method*), 26  
 possibleToReverse() (*fl.ADFA method*), 98  
 power (*class in reex*), 66  
 pref() (*fa.DFA method*), 26  
 PrefixProp (*class in codes*), 124  
 print\_data() (*fa.DFA method*), 26  
 product() (*fa.DFA method*), 26  
 product() (*fa.NFA method*), 36  
 productInput() (*transducers.SFT method*), 89  
 productInputSlow() (*transducers.SFT method*), 89  
 productSlow() (*fa.DFA method*), 26  
 PSP (*class in sst*), 131

## R

re\_stateElimination() (*fa.OFA method*), 15  
 re\_stateElimination\_nn() (*fa.OFA method*), 15  
 readFromFile() (*in module fio*), 49  
 reCG() (*fa.OFA method*), 14  
 reCG\_nn() (*fa.OFA method*), 15  
 reduced() (*reex.atom method*), 74  
 reDynamicCycleHeuristic() (*fa.OFA method*), 15  
 reex (*module*), 51  
 regexp (*class in reex*), 51  
 regexp() (*fa.DFA method*), 26  
 regexpSE() (*fa.OFA method*), 15  
 RegularExpression (*class in reex*), 51  
 renameState() (*fa.FA method*), 9  
 renameStates() (*fa.FA method*), 9  
 renameStatesFromPosition() (*fa.NFA method*), 36  
 reorder() (*fa.DFA method*), 27  
 reorder() (*fa.GFA method*), 42  
 reorder() (*fa.NFA method*), 37  
 rEquivNFA() (*fa.NFA method*), 36  
 reStaticCycleHeuristic() (*fa.OFA method*), 15  
 reStringRGenerator (*class in cfg*), 108  
 reversal() (*fa.FA method*), 10  
 reversal() (*fa.NFA method*), 37  
 reversal() (*reex.atom method*), 74  
 reversal() (*reex.concat method*), 64  
 reversal() (*reex.disj method*), 66  
 reversal() (*reex.option method*), 69  
 reversal() (*reex.power method*), 67  
 reversal() (*reex.specialConstant method*), 57  
 reversal() (*reex.star method*), 63  
 reversal() (*transducers.SFT method*), 89  
 reverseTransitions() (*fa.DFA method*), 27  
 reverseTransitions() (*fa.NFA method*), 37  
 reversibleP() (*fa.DFA method*), 27  
 rndadfa (*module*), 113  
 rndAdfa() (*rndadfa.ADFArnd method*), 114  
 rnddfa (*module*), 111  
 rndNumberSecondSources() (*rndadfa.ADFArnd method*), 115  
 rndTransitionsFromSources() (*rndadfa.ADFArnd method*), 115  
 RndWGen (*class in fl*), 100  
 rpn() (*reex.atom method*), 74  
 rpn() (*reex.concat method*), 64  
 rpn() (*reex.conj method*), 70  
 rpn() (*reex.connective method*), 62  
 rpn() (*reex.disj method*), 66  
 rpn() (*reex.emptyset method*), 59  
 rpn() (*reex.epsilon method*), 58  
 rpn() (*reex.option method*), 69  
 rpn() (*reex.power method*), 67

rpn () (*reex.regex* method), 55  
 rpn () (*reex.sconnective* method), 77  
 rpn () (*reex.shuffle* method), 70  
 rpn () (*reex.snot* method), 82  
 rpn () (*reex.specialConstant* method), 57  
 rpn () (*reex.star* method), 63  
 rpn2regex () (*in module reex*), 83  
 runOnNFA () (*transducers.SFT* method), 89  
 runOnWord () (*transducers.SFT* method), 90

## S

same\_nullability () (*fa.FA* method), 10  
 satisfiesP () (*codes.ErrCorrectProp* method), 125  
 satisfiesP () (*codes.IPTProp* method), 124  
 satisfiesPrefixP () (*codes.PrefixProp* method), 124  
 saveToFile () (*in module fio*), 50  
 saveToString () (*in module fa*), 44  
 sconcat (*class in reex*), 77  
 sconj (*class in reex*), 80  
 sconnective (*class in reex*), 76  
 sdisj (*class in reex*), 79  
 SemiDFA (*class in fa*), 11  
 setDeadState () (*fl.AFA* method), 96  
 setExecPath () (*grail.Grail* method), 130  
 setFinal () (*fa.FA* method), 10  
 setInitial () (*fa.FA* method), 10  
 setInitial () (*fa.NFA* method), 37  
 setInitial () (*transducers.SFT* method), 90  
 setOfSymbols () (*reex.atom* method), 74  
 setOfSymbols () (*reex.connective* method), 62  
 setOfSymbols () (*reex.option* method), 69  
 setOfSymbols () (*reex.position* method), 76  
 setOfSymbols () (*reex.power* method), 67  
 setOfSymbols () (*reex.regex* method), 55  
 setOfSymbols () (*reex.sconnective* method), 77  
 setOfSymbols () (*reex.snot* method), 82  
 setOfSymbols () (*reex.specialConstant* static method), 57  
 setOfSymbols () (*reex.star* method), 63  
 setOutput () (*transducers.Transducer* method), 85  
 setSigma () (*fa.FA* method), 10  
 setSigma () (*fl.FL* method), 94  
 setSigma () (*reex.regex* method), 55  
 SFT (*class in transducers*), 85  
 shuffle (*class in reex*), 70  
 shuffle () (*fa.DFA* method), 27  
 shuffle () (*fa.NFA* method), 37  
 Sigma (*fa.FA* attribute), 5  
 Sigma (*fa.SemiDFA* attribute), 12  
 sigmaInitialSegment () (*in module fl*), 100  
 sigmaP (*class in reex*), 59  
 sigmaS (*class in reex*), 60  
 simDiff () (*fa.DFA* method), 27  
 smallAlphabet () (*in module cfg*), 109  
 sMonoid () (*fa.DFA* method), 27  
 snf () (*reex.atom* method), 74  
 snf () (*reex.epsilon* method), 58  
 snot (*class in reex*), 81  
 sop () (*fa.DFA* method), 27  
 specialConstant (*class in reex*), 56  
 SPRegExp () (*fa.OFA* method), 12  
 square () (*transducers.SFT* method), 90  
 square\_fv () (*transducers.SFT* method), 90  
 SSemiGroup (*class in fa*), 43  
 sSemigroup () (*fa.DFA* method), 27  
 sst (*module*), 131  
 sstar (*class in reex*), 78  
 star (*class in reex*), 62  
 star () (*fa.DFA* method), 28  
 star () (*fa.NFA* method), 37  
 star () (*transducers.SFT* method), 90  
 starConcat () (*in module comboperations*), 117  
 starDisj () (*in module comboperations*), 118  
 starHeight () (*reex.atom* static method), 74  
 starHeight () (*reex.connective* method), 62  
 starHeight () (*reex.option* method), 69  
 starHeight () (*reex.power* method), 67  
 starHeight () (*reex.regex* method), 55  
 starHeight () (*reex.sconnective* method), 77  
 starHeight () (*reex.snot* method), 82  
 starHeight () (*reex.star* method), 63  
 starI () (*fa.DFA* method), 28  
 starInter () (*in module comboperations*), 118  
 starInter0 () (*in module comboperations*), 118  
 starWConcat () (*in module comboperations*), 117  
 stateAlphabet () (*fa.FA* method), 10  
 stateChildren () (*fa.DFA* method), 28  
 stateChildren () (*fa.GFA* method), 43  
 stateChildren () (*fa.NFA* method), 37  
 stateChildren () (*fa.OFA* method), 15  
 stateIndex () (*fa.FA* method), 10  
 stateName () (*fa.FA* method), 11  
 statePairEquiv () (*fl.ADFA* method), 98  
 States (*fa.FA* attribute), 5  
 States (*fa.SemiDFA* attribute), 11  
 str2regex () (*in module reex*), 83  
 str2sre () (*in module reex*), 83  
 stringLength () (*reex.atom* method), 75  
 stringToADFA () (*in module fl*), 101  
 stringToDFA () (*in module fa*), 45  
 stronglyConnectedComponents () (*fa.DFA* method), 28  
 stronglyConnectedComponents () (*fa.NFA* method), 37  
 subword () (*fa.DFA* method), 28  
 subword () (*fa.NFA* method), 37  
 succinctTransitions () (*fa.DFA* method), 28

succinctTransitions() (*fa.FA method*), 11  
 succinctTransitions() (*fa.GFA method*), 43  
 succinctTransitions() (*fa.NFA method*), 37  
 succinctTransitions() (*fa.OFA method*), 16  
 succinctTransitions() (*transducers.Transducer method*), 85  
 suff() (*fa.DFA method*), 28  
 suffixClosedP() (*fl.FL method*), 94  
 support() (*reex.atom method*), 75  
 support() (*reex.conj method*), 70  
 support() (*reex.sconcat method*), 78  
 support() (*reex.sconj method*), 81  
 support() (*reex.sdisj method*), 80  
 support() (*reex.shuffle method*), 70  
 support() (*reex.sigmaP method*), 60  
 support() (*reex.sigmaS method*), 61  
 support() (*reex.snot method*), 82  
 support() (*reex.specialConstant method*), 57  
 support() (*reex.sstar method*), 79  
 supportlast() (*reex.atom method*), 75  
 supportlast() (*reex.shuffle method*), 70  
 supportlast() (*reex.specialConstant method*), 57  
 syncPower() (*fa.DFA method*), 28  
 syncWords() (*fa.DFA method*), 29  
 syntacticLength() (*reex.atom static method*), 75  
 syntacticLength() (*reex.sconnective method*), 77  
 syntacticLength() (*reex.snot method*), 82

## T

tail() (*reex.sconcat method*), 78  
 tail\_rev() (*reex.sconcat method*), 78  
 tailForm() (*reex.atom method*), 75  
 tailForm() (*reex.concat method*), 65  
 tailForm() (*reex.disj method*), 66  
 tailForm() (*reex.regexp method*), 55  
 tailForm() (*reex.specialConstant method*), 57  
 tailForm() (*reex.star method*), 64  
 toADFA() (*fa.DFA method*), 29  
 toANFA() (*fl.ADFA method*), 98  
 toDFA() (*fa.DFA method*), 29  
 toDFA() (*fa.NFA method*), 38  
 toDFA() (*fl.FL method*), 94  
 toDFA() (*reex.regexp method*), 55  
 toGFA() (*fa.DFA method*), 29  
 toGFA() (*fa.GFA method*), 43  
 toGFA() (*fa.NFA method*), 38  
 toGFA() (*fa.OFA method*), 16  
 toInNFA() (*transducers.SFT method*), 90  
 toNFA() (*fa.DFA method*), 29  
 toNFA() (*fa.NFA method*), 38  
 toNFA() (*fa.NFAr method*), 40  
 toNFA() (*fl.ADFA method*), 98  
 toNFA() (*fl.FL method*), 94  
 toNFA() (*reex.regexp method*), 55

toNFAr() (*fa.NFA method*), 38  
 toNFT() (*transducers.SFT method*), 90  
 toOutNFA() (*transducers.SFT method*), 90  
 topoSort() (*fa.OFA method*), 16  
 toSFT() (*transducers.SFT method*), 90  
 TrajProp (*class in codes*), 121  
 trajToTransducer() (*codes.TrajProp static method*), 121  
 Transducer (*class in transducers*), 85  
 transducers (*module*), 85  
 transitions() (*fa.DFA method*), 29  
 transitionsA() (*fa.DFA method*), 29  
 treeLength() (*reex.atom static method*), 75  
 treeLength() (*reex.connective method*), 62  
 treeLength() (*reex.option method*), 69  
 treeLength() (*reex.power method*), 67  
 treeLength() (*reex.regexp method*), 55  
 treeLength() (*reex.sconnective method*), 77  
 treeLength() (*reex.snot method*), 82  
 treeLength() (*reex.star method*), 64  
 trieFA() (*fl.FL method*), 94  
 trim() (*fa.OFA method*), 16  
 trim() (*fl.ADFA method*), 98  
 trim() (*transducers.SFT method*), 90  
 trimP() (*fa.OFA method*), 16

## U

union() (*fa.FA method*), 11  
 union() (*fl.FL method*), 94  
 union() (*transducers.SFT method*), 91  
 unionSigma() (*reex.regexp method*), 55  
 uniqueRepr() (*fa.DFA method*), 29  
 uniqueRepr() (*fa.GFA method*), 43  
 uniqueRepr() (*fa.NFA method*), 38  
 uniqueRepr() (*fa.OFA method*), 16  
 universalP() (*fa.DFA method*), 29  
 unlinkSoleIncoming() (*fa.NFAr method*), 40  
 unlinkSoleOutgoing() (*fa.NFAr method*), 41  
 unmark() (*fa.DFA method*), 30  
 unmark() (*reex.concat method*), 65  
 unmark() (*reex.disj method*), 66  
 unmark() (*reex.specialConstant method*), 57  
 unmark() (*reex.star method*), 64  
 unmarked() (*reex.atom method*), 75  
 unmarked() (*reex.position method*), 76  
 unmarked() (*reex.specialConstant method*), 57  
 usefulStates() (*fa.DFA method*), 30  
 usefulStates() (*fa.GFA method*), 43  
 usefulStates() (*fa.NFA method*), 38  
 usefulStates() (*fa.OFA method*), 16

## V

vDescription() (*fa.DFA static method*), 30  
 vDescription() (*fa.NFA static method*), 38

vertexIndex() (*graphs.Graph method*), 103

## W

weight() (*fa.GFA method*), 43

weightWithCycles() (*fa.GFA method*), 43

witness() (*fa.DFA method*), 30

witness() (*fa.NFA method*), 38

witnessDiff() (*fa.DFA method*), 30

Word (*class in common*), 47

wordDerivative() (*reex.regex method*), 55

wordDerivative() (*reex.specialConstant method*),  
57

wordGenerator() (*fl.ADFA method*), 99

WordI() (*fa.SSemiGroup method*), 44

wordImage() (*fa.NFA method*), 38

WordPS() (*fa.SSemiGroup method*), 44

words() (*fa.FA method*), 11