

# Applied Cryptography

## Week #5 Extra

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### Important

- Your answers must **always** be accompanied by a justification. Presenting the final result (e.g. the result of a calculation) without the rationale that laid to said result will result in a grade of 0.
- Submit your answers via e-mail to *bernardo.portela@fc.up.pt*, with adequate identification of the group and its members.

### Q1: Collision resistant Hash Functions

Consider  $H : M \rightarrow T$  a collision resistant hash function that takes messages of any size  $m \in M = \{0, 1\}^*$  and produces outputs with 64 bit length  $t \in T = \{0, 1\}^{64}$ .

1.  $H' = (H(m) || H(m) || H(m))$
2.  $H' = H(m || m || m)$
3.  $H' = H(64)$
4.  $H' = H(m || 64)$
5.  $H' = H(m)[0 \dots 10]$  // truncate the output to 10 bits
6.  $H' = H(m[0 \dots |m|-2])$  // hash  $m$  without its last bit
7.  $H' = H(m) || H(m \oplus 1^{|m|})$
8.  $H' = H(m)$  if  $m = 0^{64} \wedge m = 1^{64}$ ,  $H(m \oplus 1^{|m|})$  otherwise

**Question:** Which of the proposed hash constructions  $H'$  are also collision resistant?

### Q2: Rho method to find Hash collisions

As described in [1], the Rho method is an algorithm for finding collisions that, unlike the naive birthday attack, requires only a small amount of memory. To find collision in hash function  $H(m)$ , it works as follows.

1. Given a hash function with  $n$ -bit values, pick some random hash value  $h_1$  and define  $h'_1 = h_1$ .
2. Compute  $h_2 = H(h_1)$  and  $h'_2 = H(H(h'_1))$ . In the first case, we apply the hash function once. In the second, we apply it twice.
3. Iterate the process and compute  $h_{i+1} = H(h_i)$  and  $h'_{i+1} = H(H(h'_i))$ , until you reach a  $i$  such that  $h'_{i+1} = h_{i+1}$
4. If this is the case, then you have found a loop within the possible hash values. How can we find the collision now? Check out this proof.

Complete the code in `rho_exercise.py` to do this.

- You must complete function `rho`, which is parametrized by an initial value

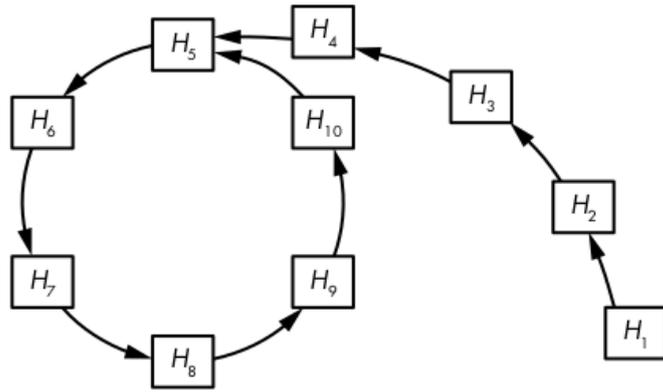


Figure 1: Rho Method

- Function  $H$  computes hashes truncated as necessary.
- You can adjust the global parameter during testing, but the goal is to find a collision in  $L = 5$ .

Also include a succinct analysis of how long it takes to find these collisions, both in cycle iterations and real time. How does this scale with  $L$ ?

### Q3: Weak ciphers

The code in `ciphersuite_fsr.py` contains a very poorly implemented “stream cipher”.

1. Consider the IND-CPA security experiment. How many calls to the encryption oracle do you have to do to succeed?
2. Describe how one can construct an attacker against the IND-CPA experiment running this encryption scheme.

[1] Jean-Philippe Aumasson; Serious Cryptography: A Practical Introduction to Modern Encryption, No Startch Press, 2017. ISBN: 9781593278267